



Effect Analysis for Programs with Callbacks

Etienne Kneuss, Viktor Kuncak, Philippe Suter



```
class Cell {  
  var visited = false  
}  
def toggle(c: Cell) {  
  c.visited = !c.visited  
}
```

What does this function do?

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*“Updates the field **c.visited**”*

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  f(c)  
}
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*“Calls function **f** on cell **c**”*

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  cs.foreach( _.visited = true )  
}
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*“Calls function **f** on cell **c**”*

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What does this function do?

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*“Updates the field **c.visited**”*

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def apply(c: Cell, f: Cell=>Unit) {  
  f(c)  
}
```

*“Calls function **f** on cell **c**”*

```
def visitAll(cs: List[Cell]) {  
  cs.foreach( _.visited = true )  
}
```

*“Sets the **visited** field on
all cells of **cs**”*

Motivation

- Goal: Precise effect analysis
 - Important for automated reasoning
 - Enables e.g. compiler optimizations
 - *Additional goal*: improve program understanding
- Challenges:
 - Functions cannot be analyzed in isolation
 - Naïve approaches fall short on dynamic dispatch
 - Analysis results can be hard to interpret

Contributions

- A precise pointer and effect analysis
flow-sensitive, modular, supports higher-order functions, requires no annotations
- A translation of effects to readable summaries

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Contributions

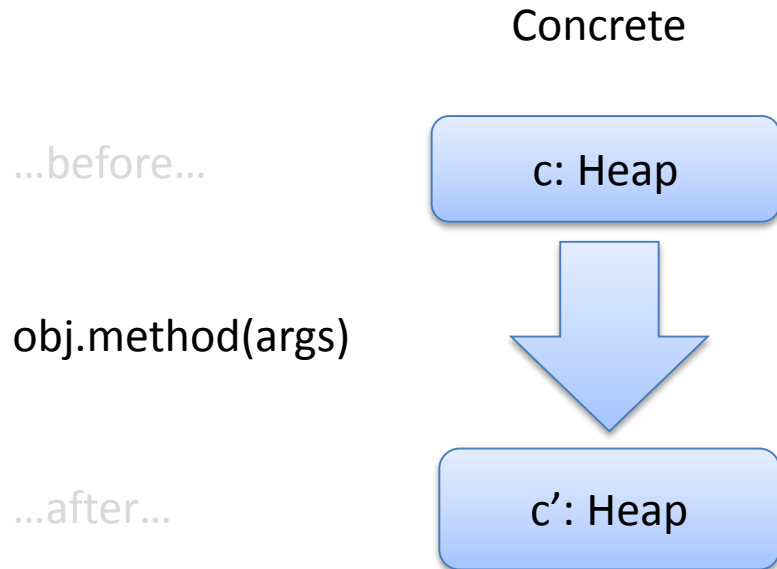
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- A translation of effects to readable summaries

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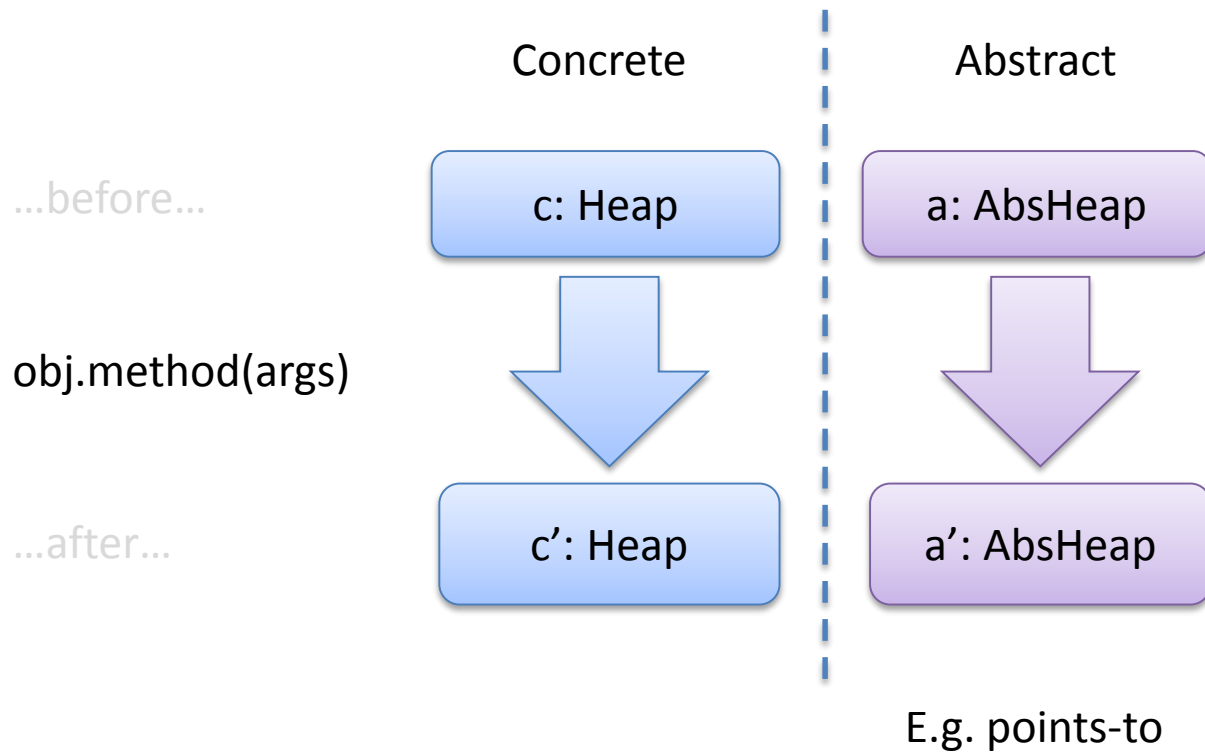


cs.tl*.hd.visited

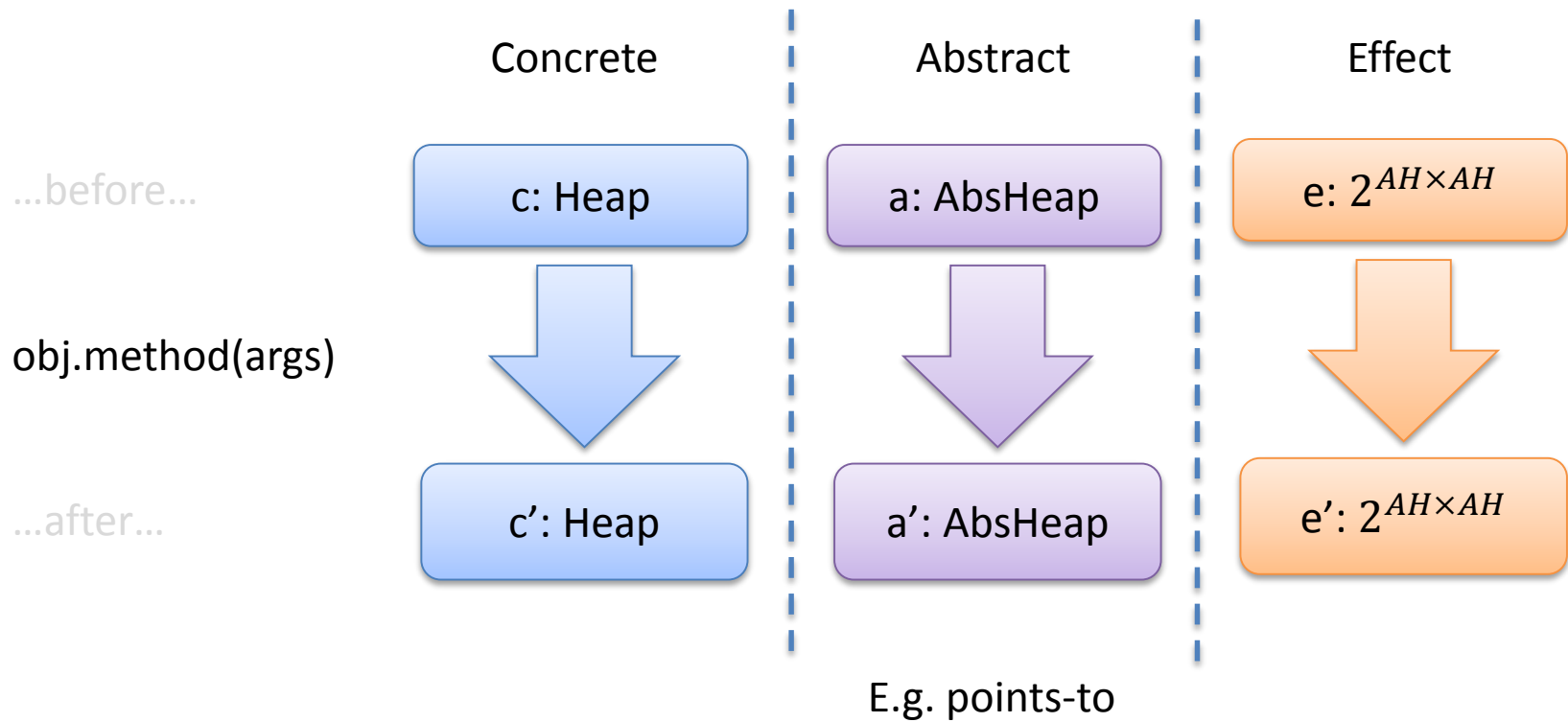
Relational Analysis



Relational Analysis



Relational Analysis

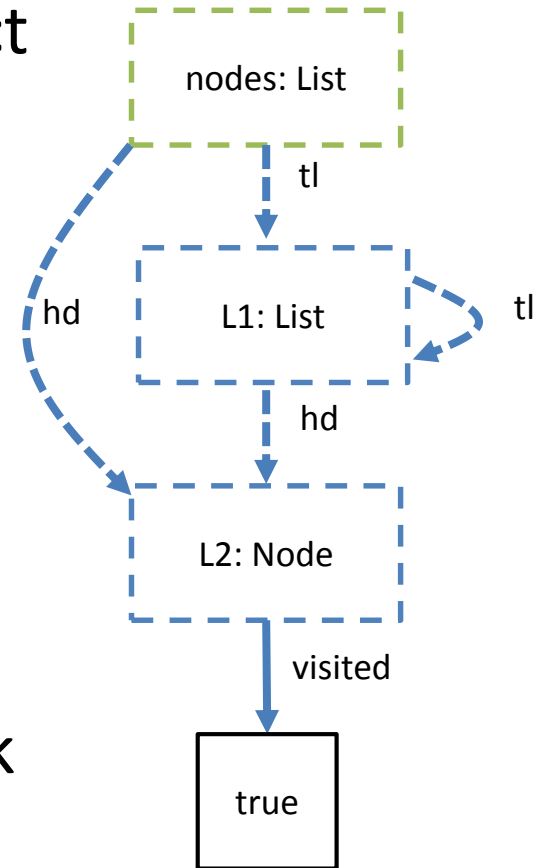


Effects as Graphs

- Graphs describe relations on abstract heaps:

$$E: 2^{AH \times AH}$$

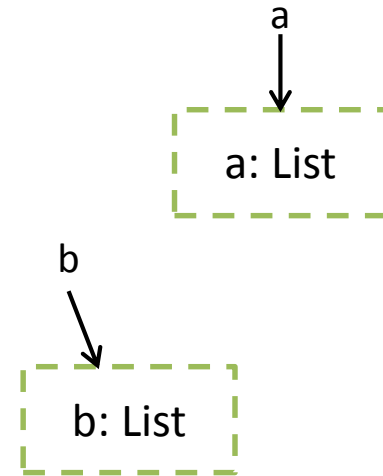
- Nodes represent objects.
- Edges encode read or write effects.
- Nodes may be unresolved:
 - parameters, fields, **this**
- Domain adapted from previous work by Salcianu et al.



Example

```
case class List(var head: Int,  
                var tail: List)
```

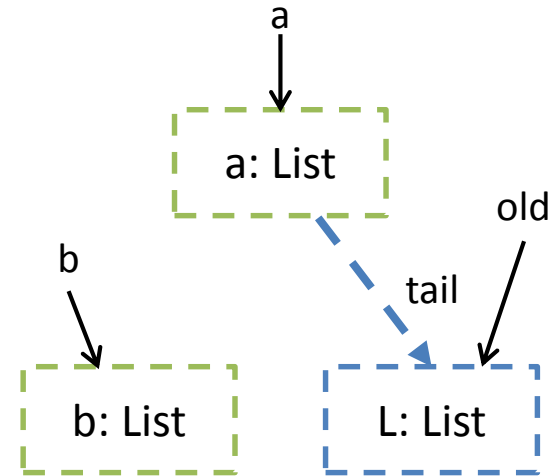
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def setTail(a: List, b: List): List = {  
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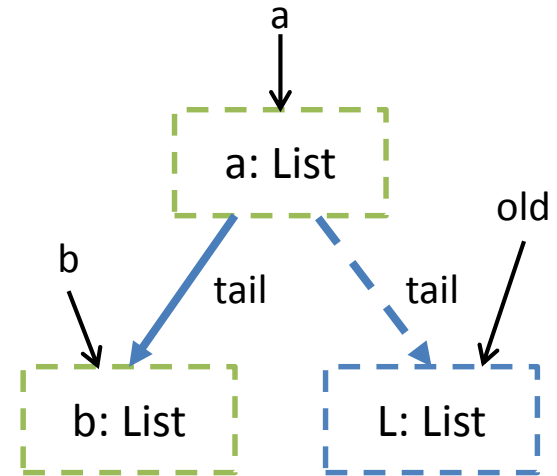
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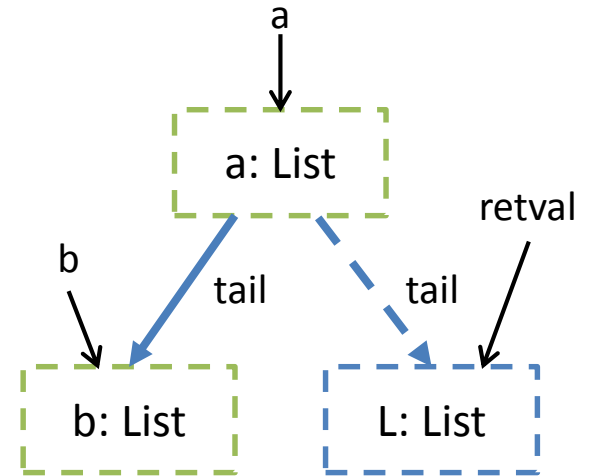
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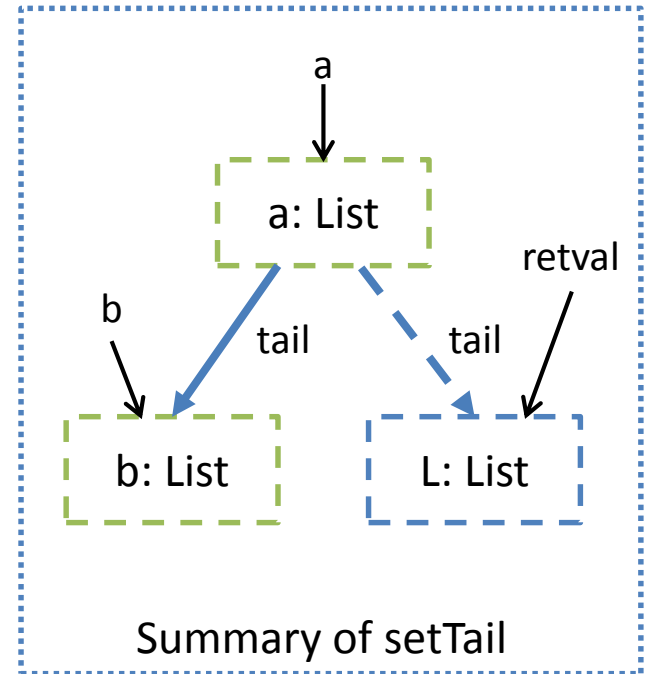
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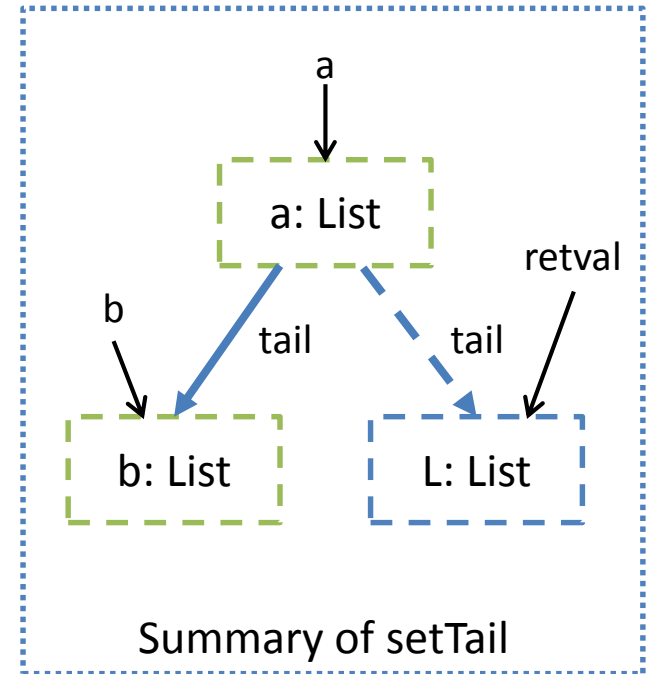
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def example() {  
  val list = new List(0,  
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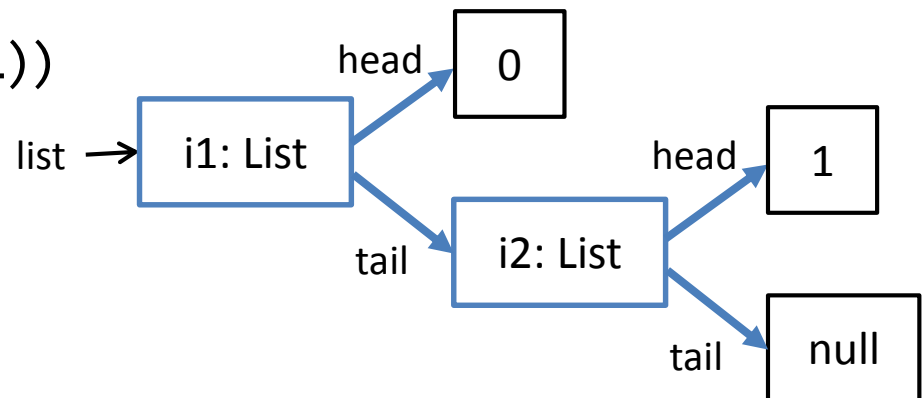
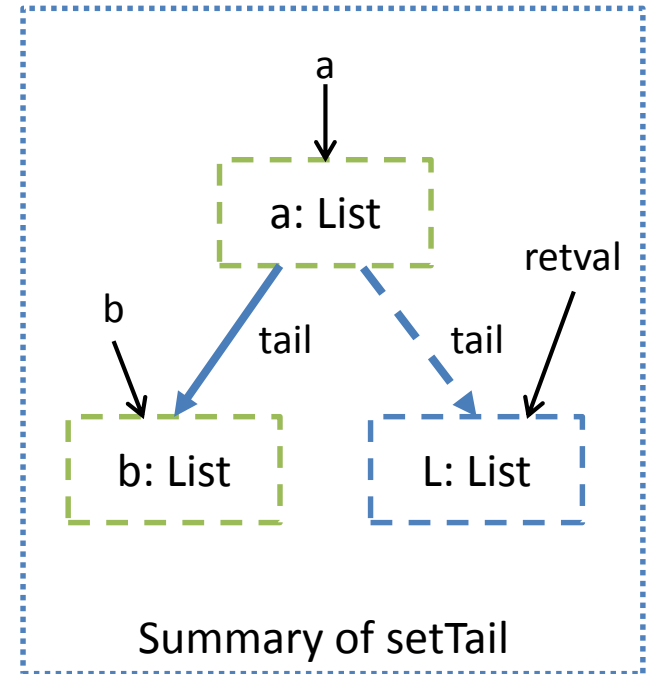


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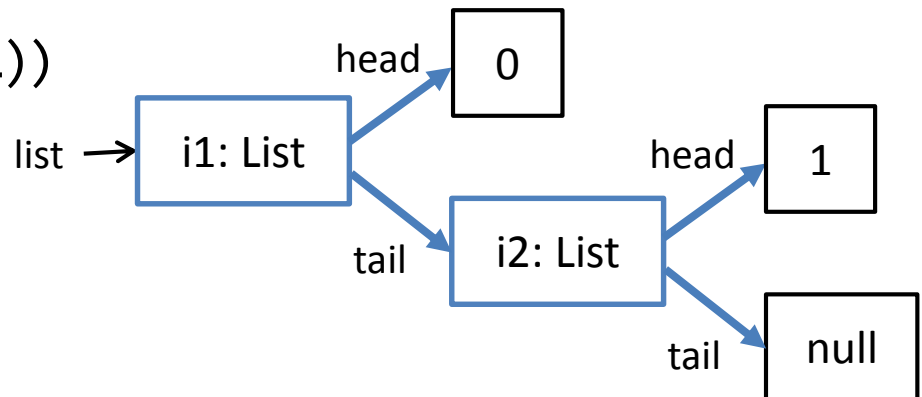
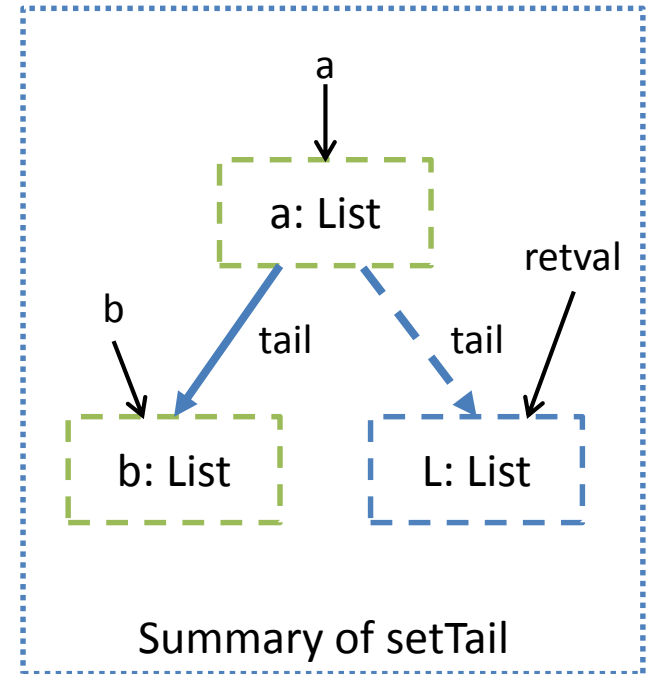
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Composition

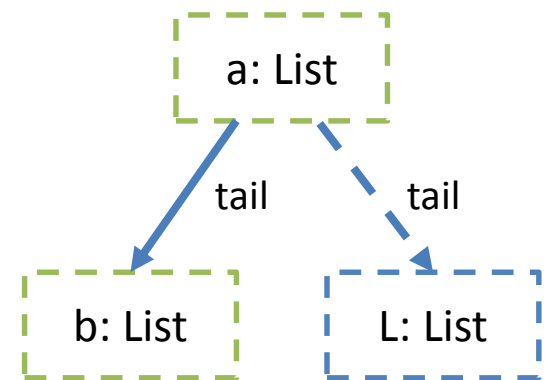
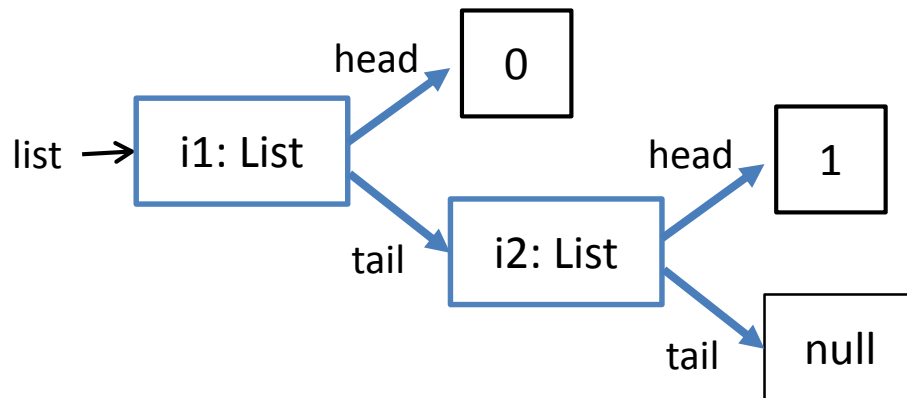
→ map parameters to arguments;

do:

resolve nodes;

import write effects;

until fix-point;



Composition

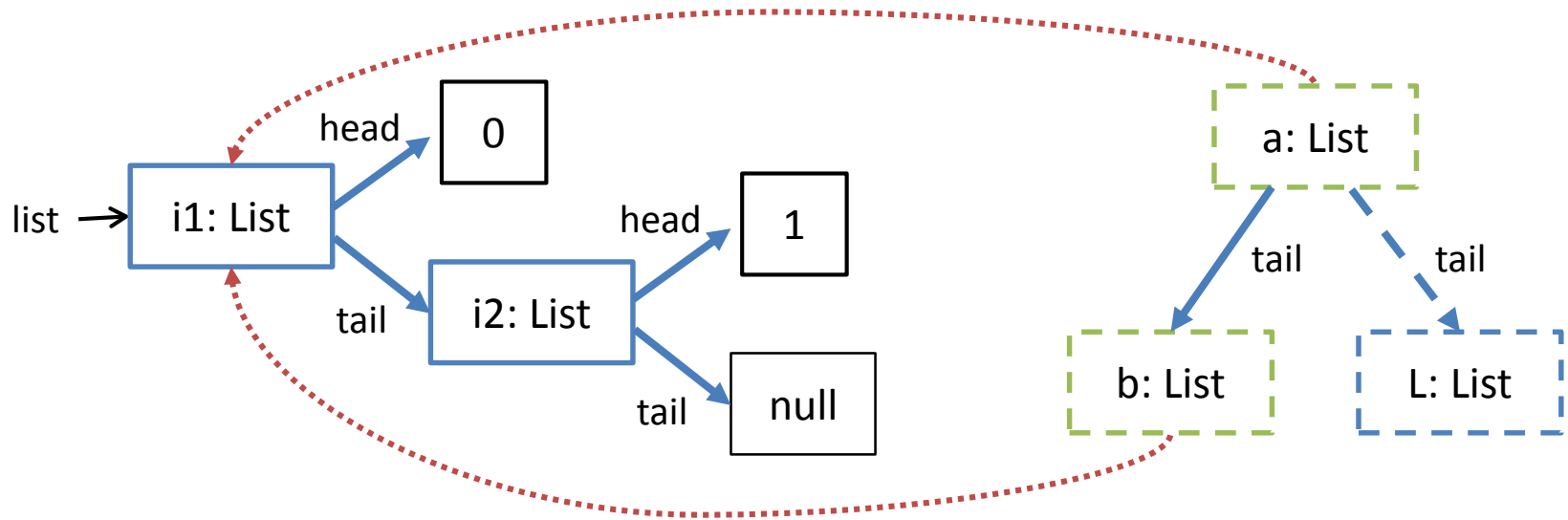
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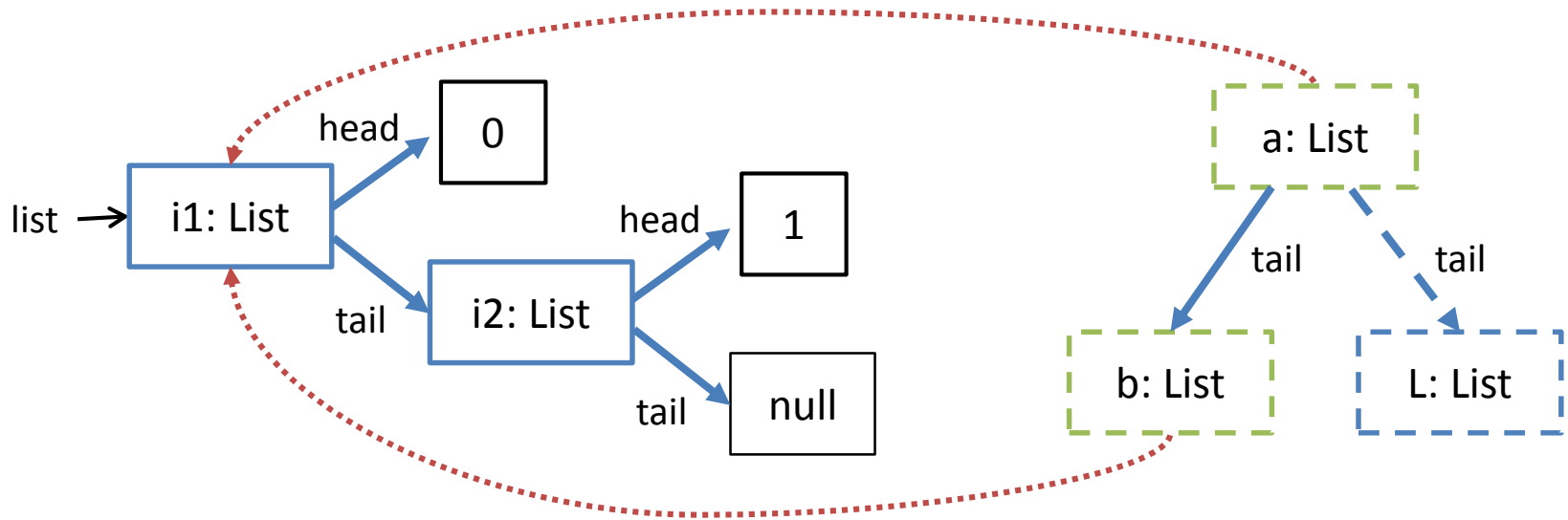


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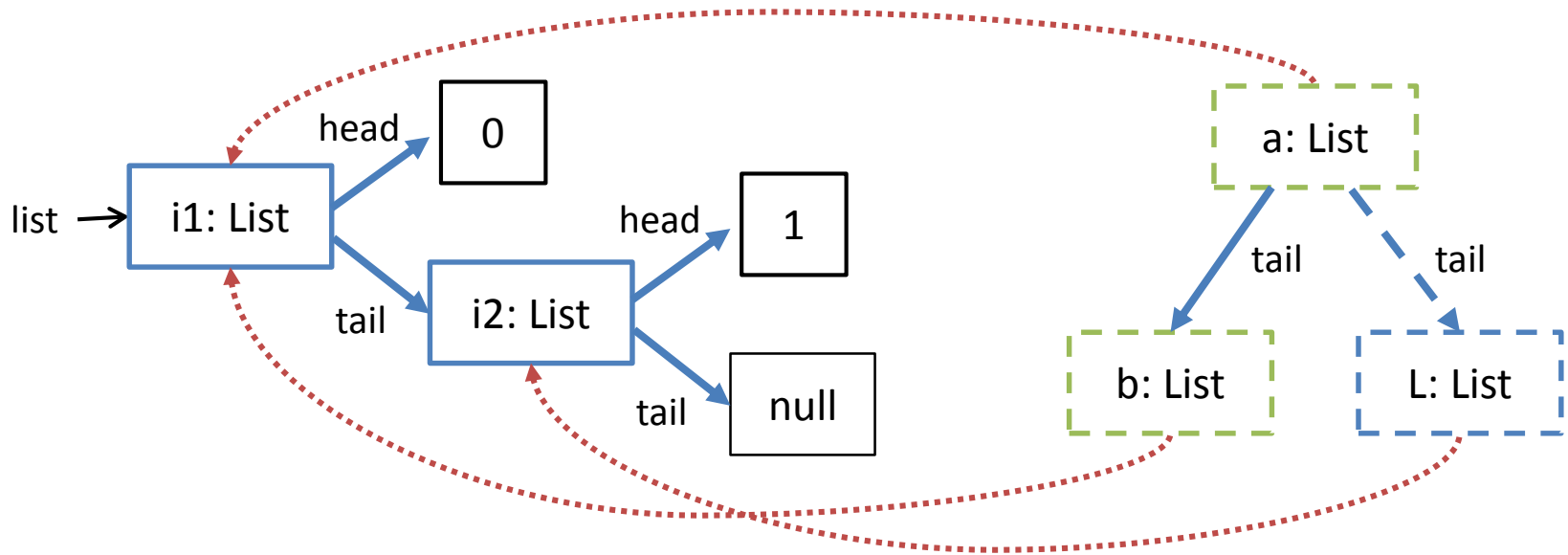


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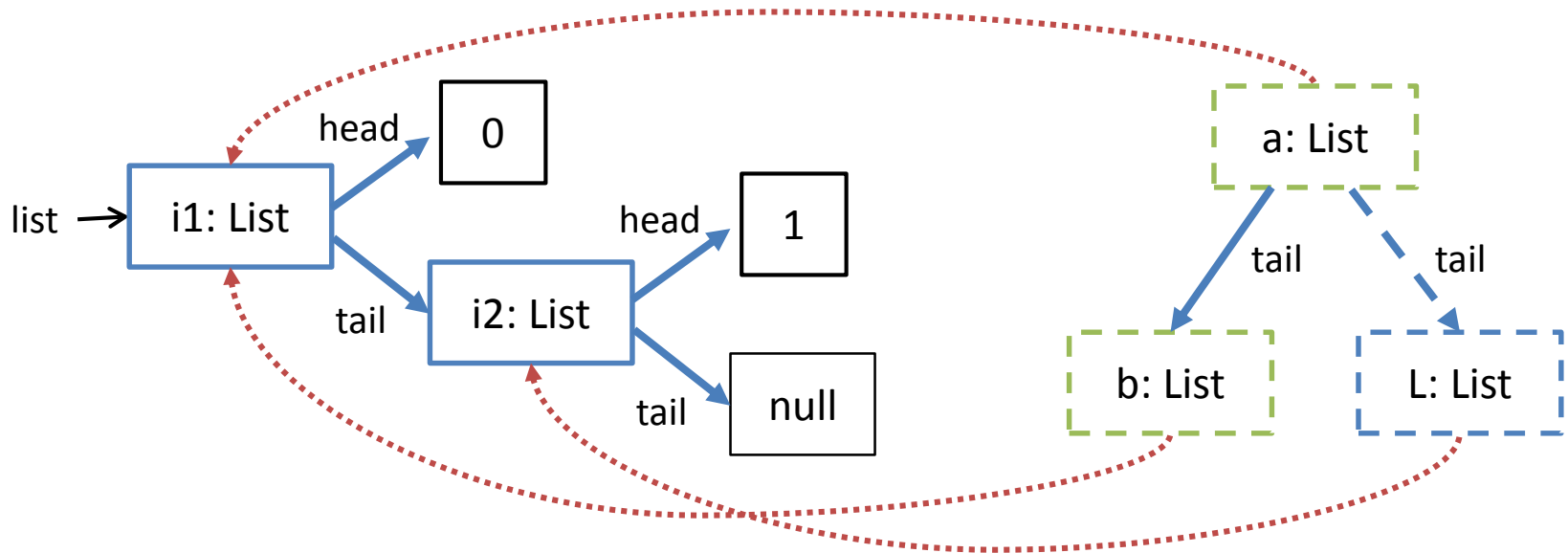
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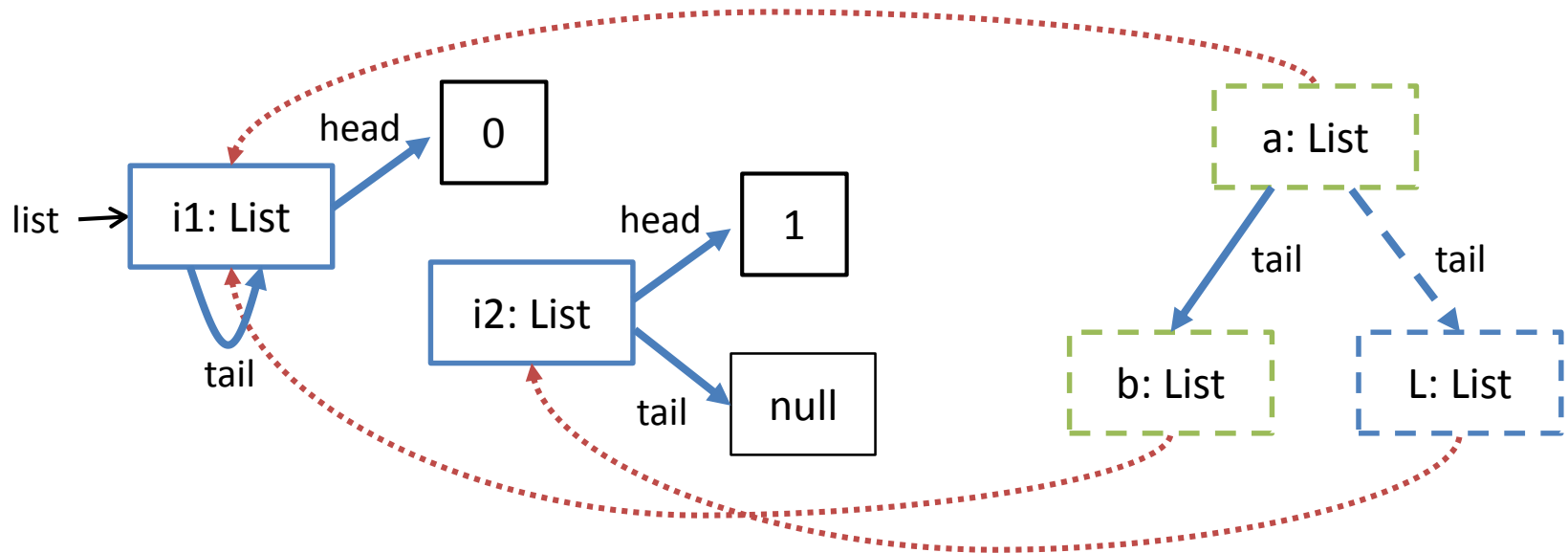
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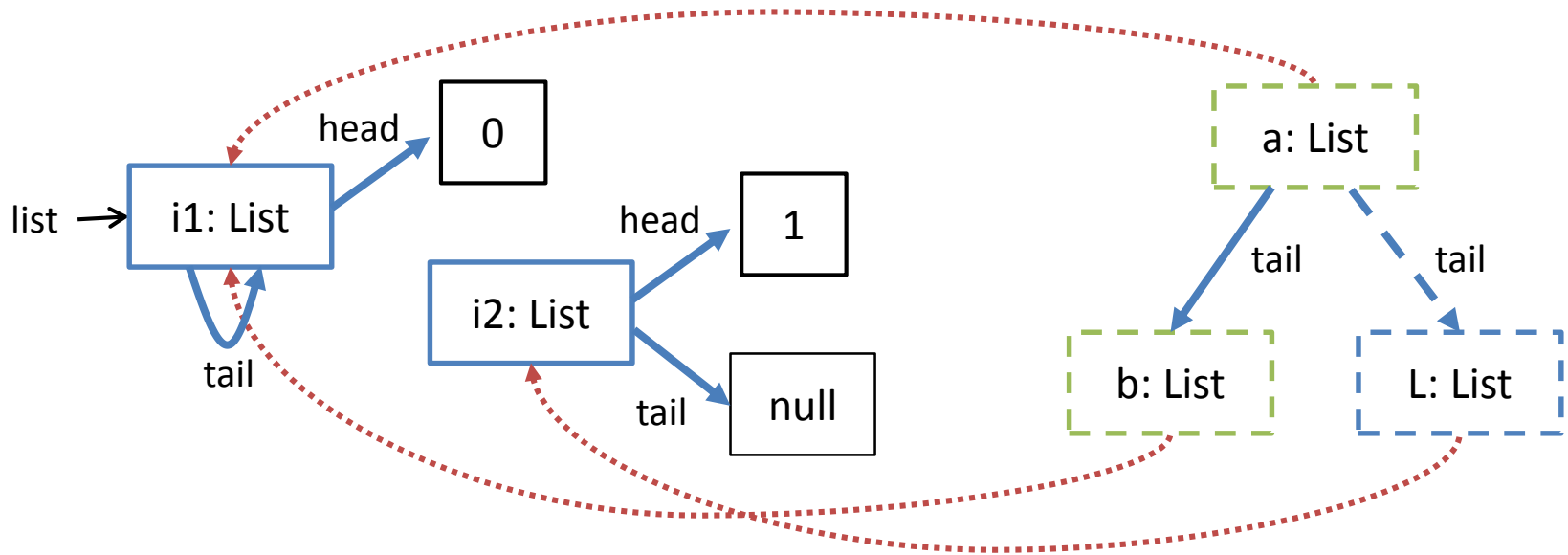


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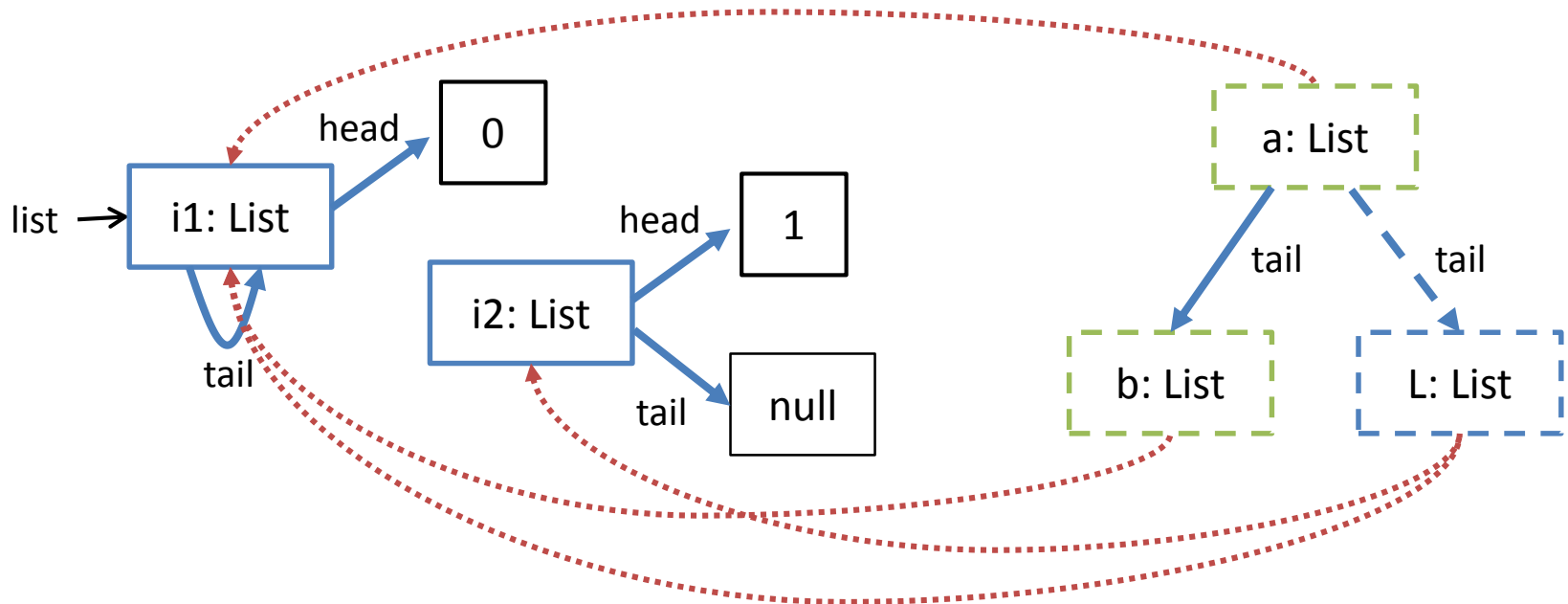


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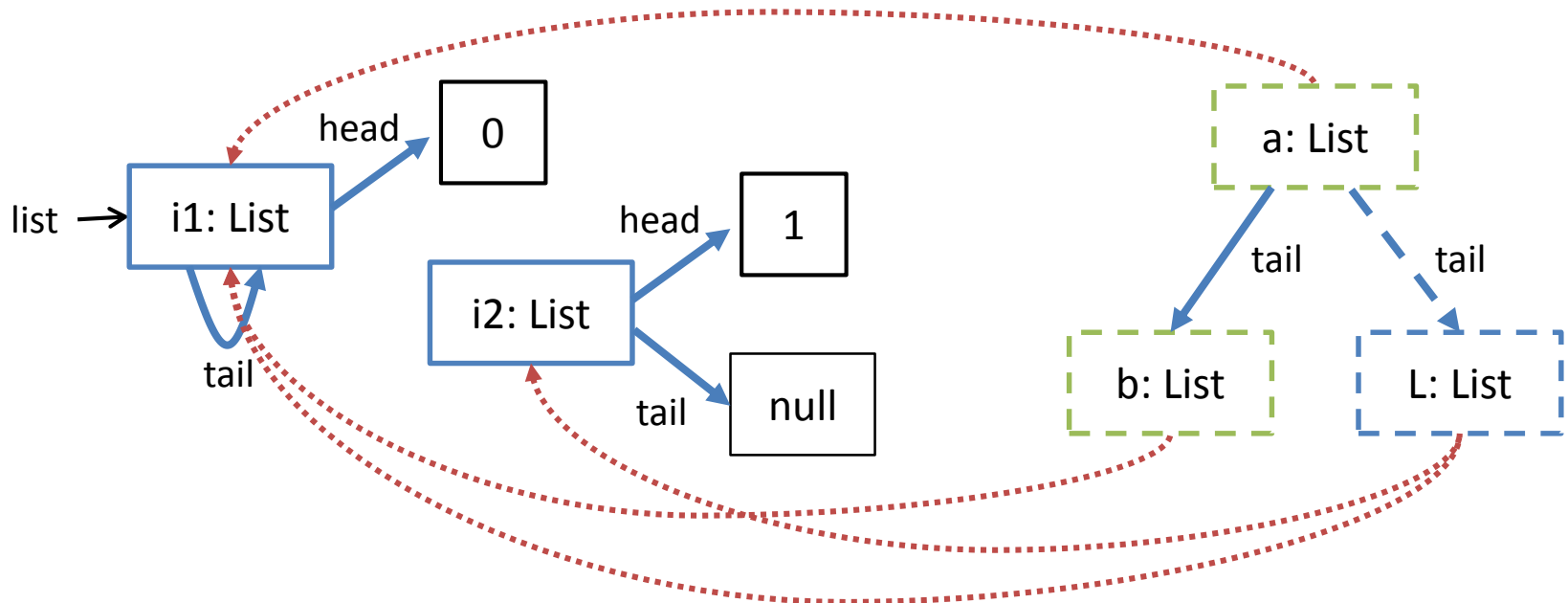
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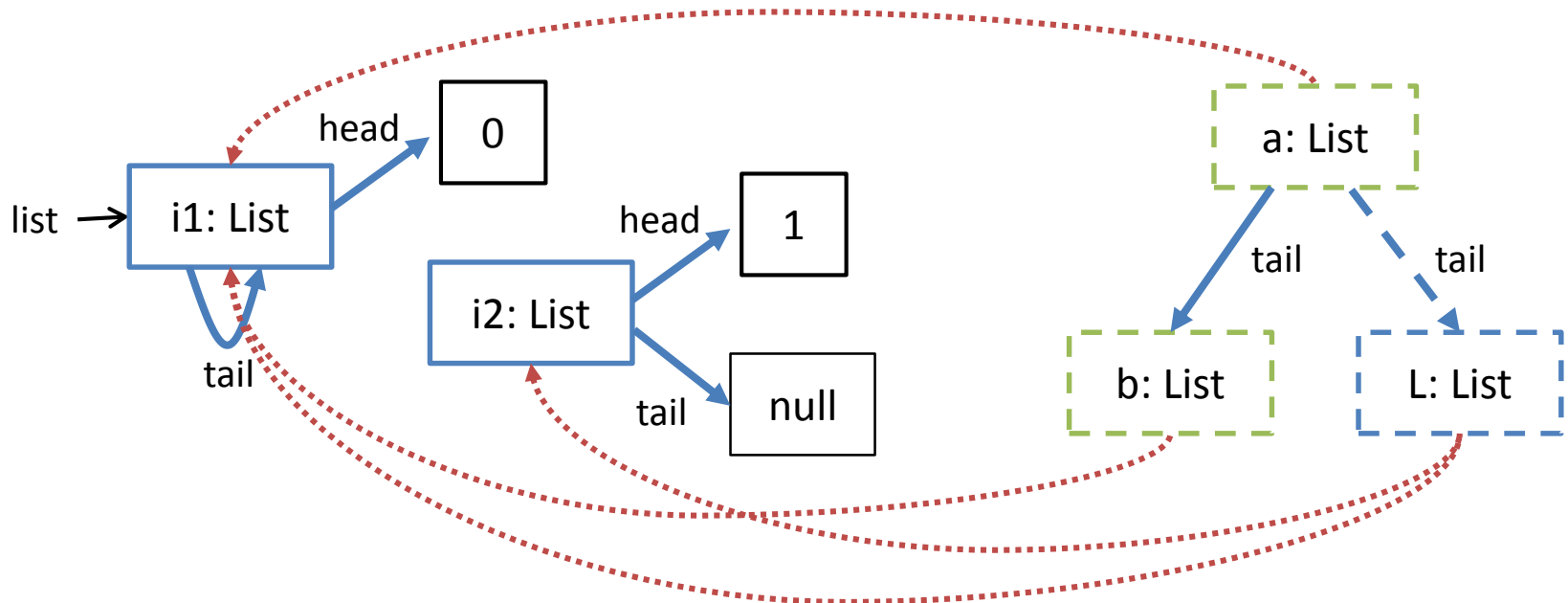
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Effects as Graphs

- Compact representation of abstract heap transformers.
- Unresolved nodes offer a flexible solution to aliasing problems.
- Composition expressed as a graph manipulation algorithm.
- ...but potentially difficult to interpret.
 - best suited as an internal representation

Handling Callbacks

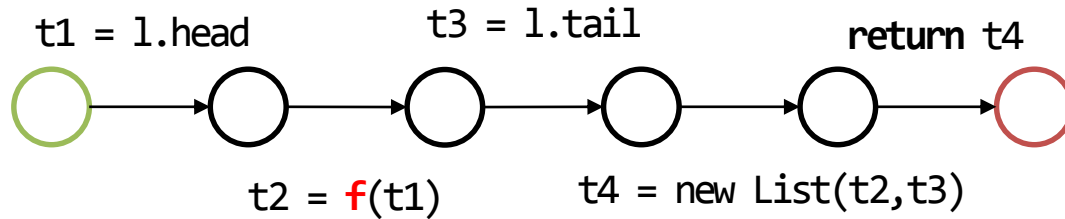
- Dynamic dispatch in practice:
 - Function1 in Scala library has >1000 subclasses
- Union of all potential targets not an option.
- *Idea*: delay analysis of method call until more information is available

Delaying Effect Composition

```
def mapHead(l: List, f: Int=>Int): List = {  
  new List(f(l.head), l.tail)  
}
```

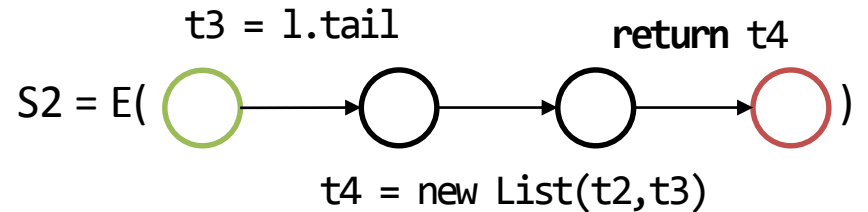
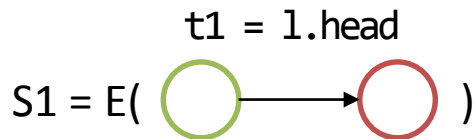
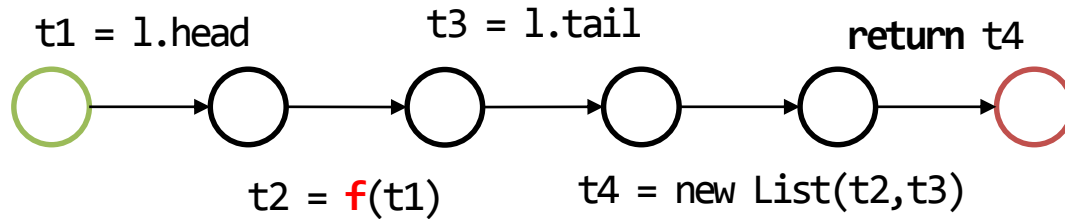
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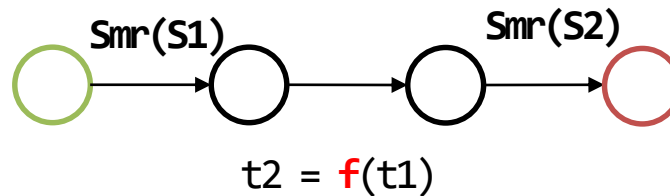
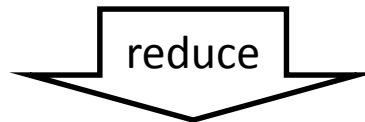
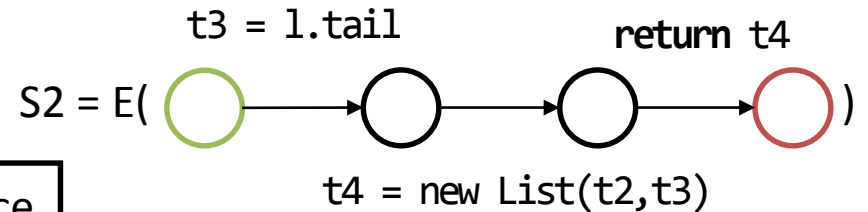
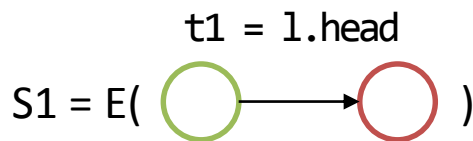
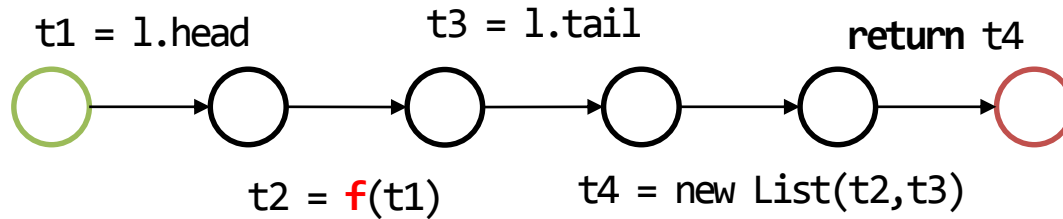
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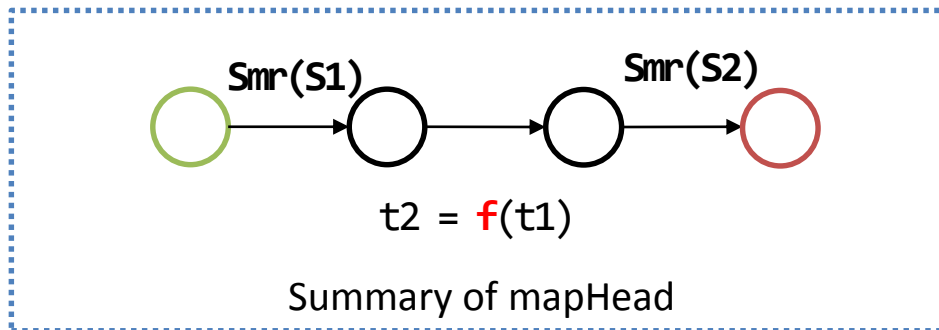
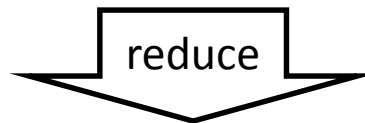
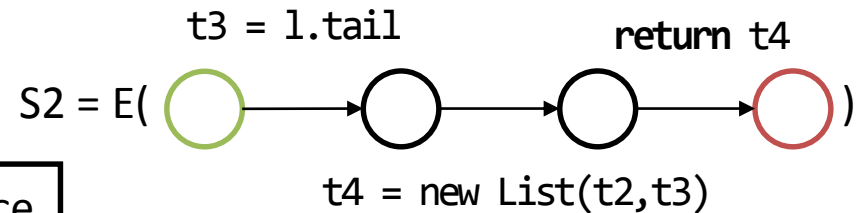
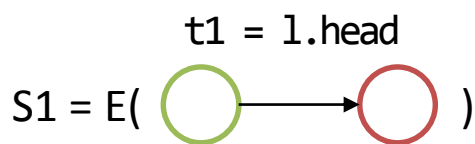
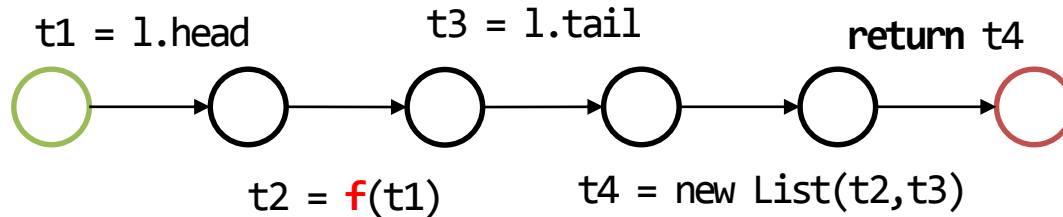
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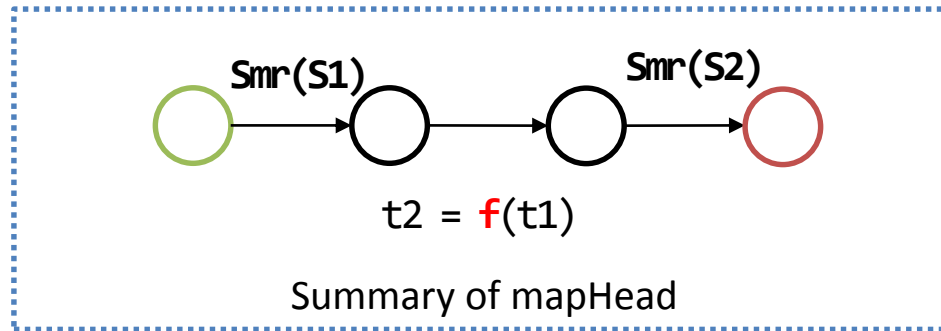


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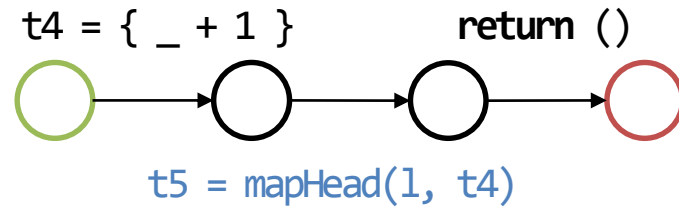
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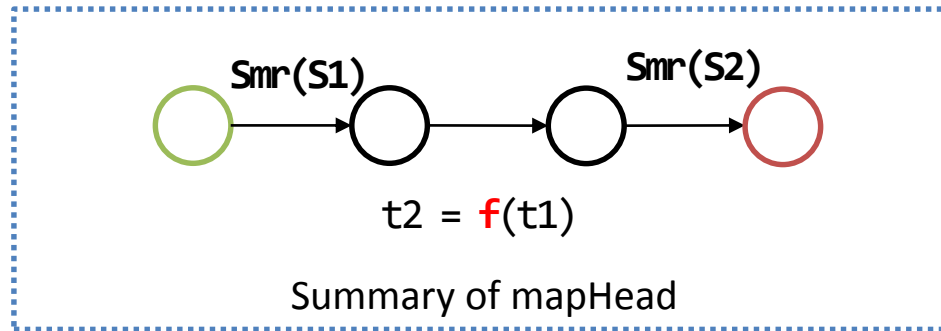
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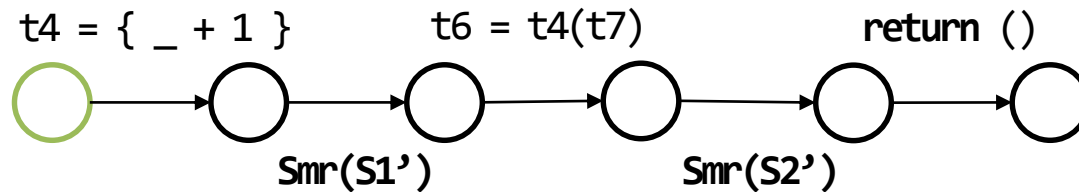
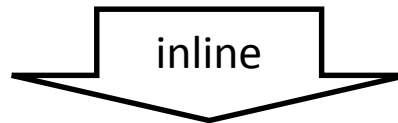
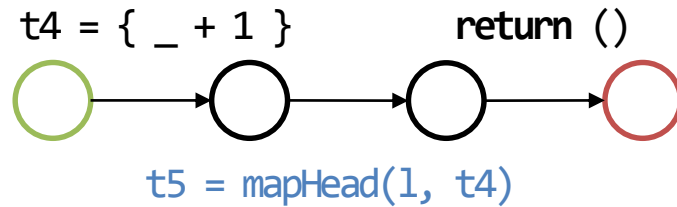
```
def test(l: List) {  
  mapHead(l, {_ + 1})  
}
```



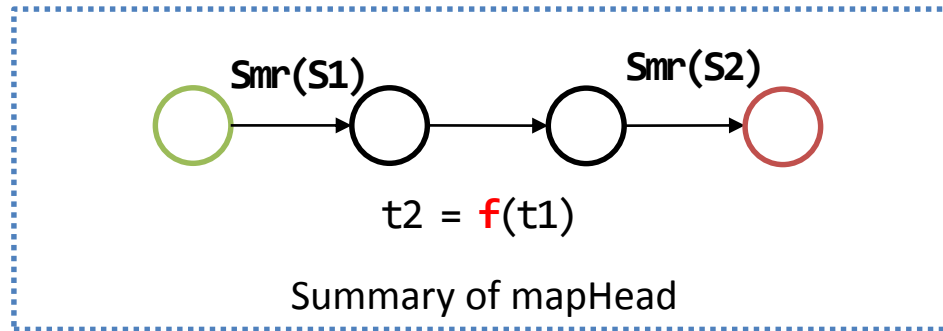
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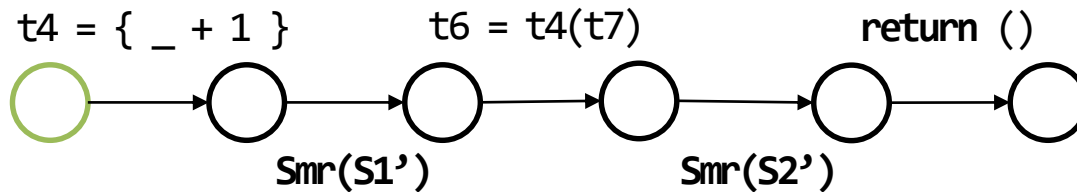
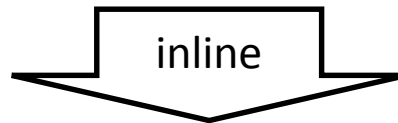
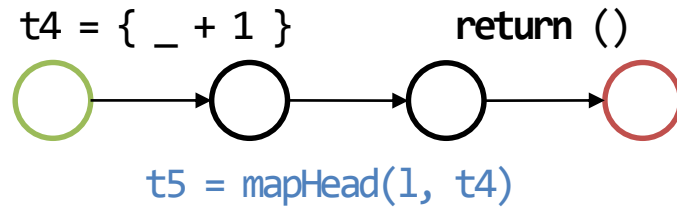
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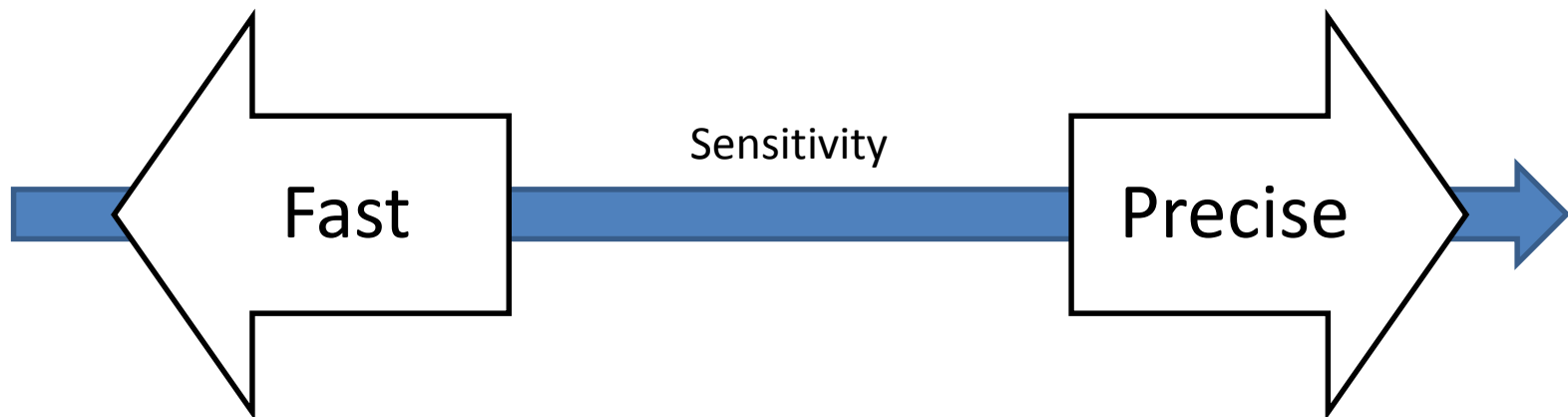


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Delaying Decision

- We base the decision of delaying a method call on several factors:
 - Number of targets
 - Calling context
 - Escaping receiver





Interprocedural Static Analysis of Effects

- Analysis implemented for Scala
- Plugin for the reference compiler
- Publicly available from:

<https://github.com/epfl-lara/insane>

Evaluation

- Characterize the effects:

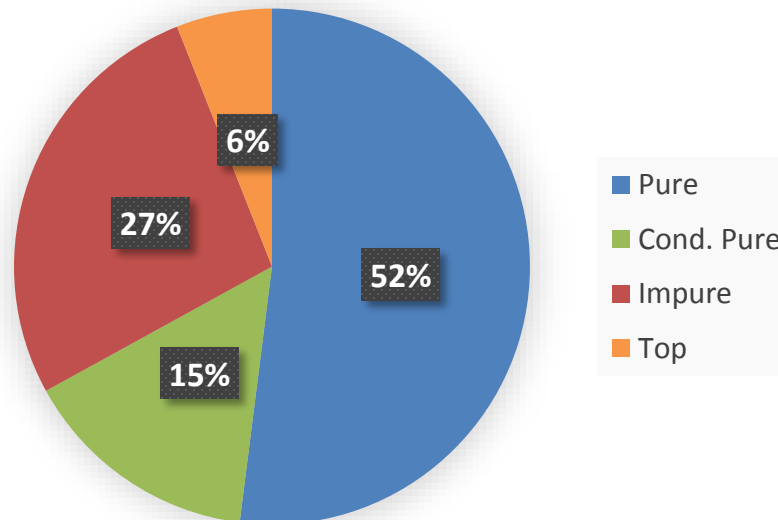
pure \sqsubseteq *conditionally pure* \sqsubseteq *impure* \sqsubseteq \top

Evaluation

- Characterize the effects:

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- Run on the Scala 2.10 library:

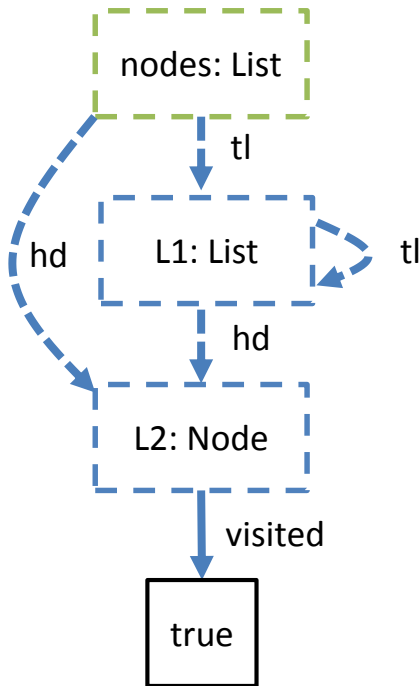


Results

Package	#Methods	Pure	Cond. Pure	Impure	T
scala	5721	79%	11%	10%	1%
scala.annotation	41	93%	2%	2%	2%
scala.beans	25	64%	8%	29%	8%
scala.collection	34810	46%	17%	29%	8%
...
scala.util	1786	51%	11%	32%	6%
scala.util.parsing	2206	56%	12%	27%	5%
scala.xml	2860	56%	11%	30%	3%
Total	58410	52%	15%	27%	6%

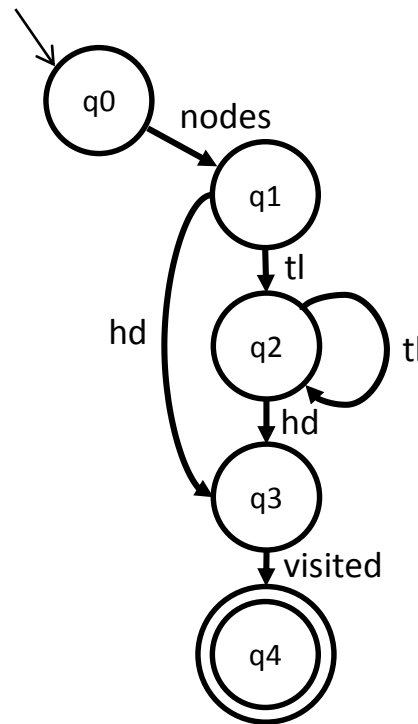
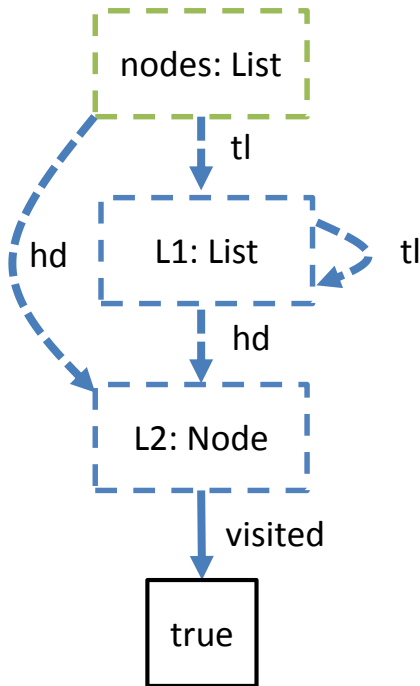
Producing Readable Summaries

- Translating effect graphs into automata



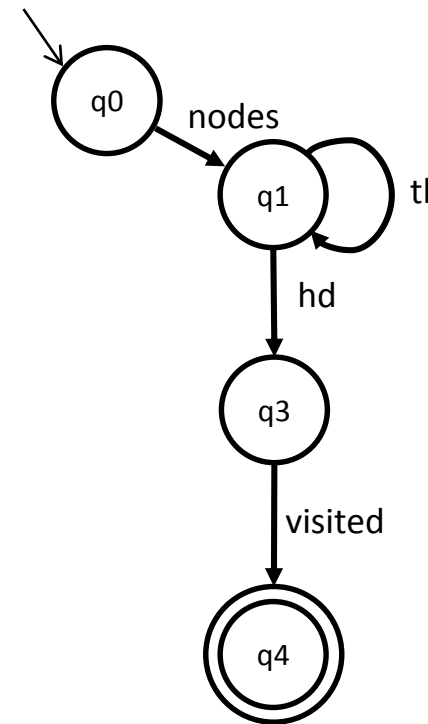
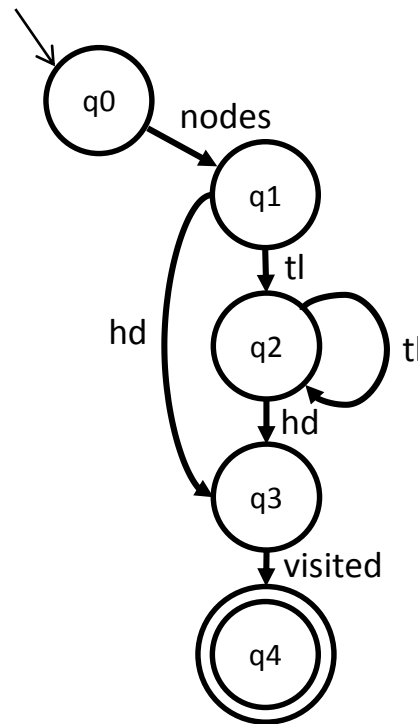
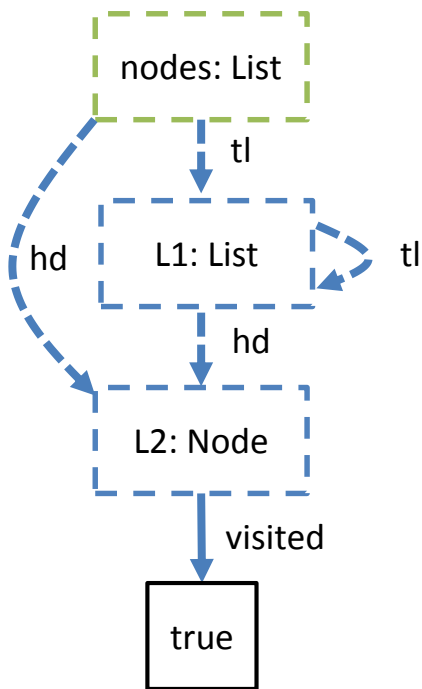
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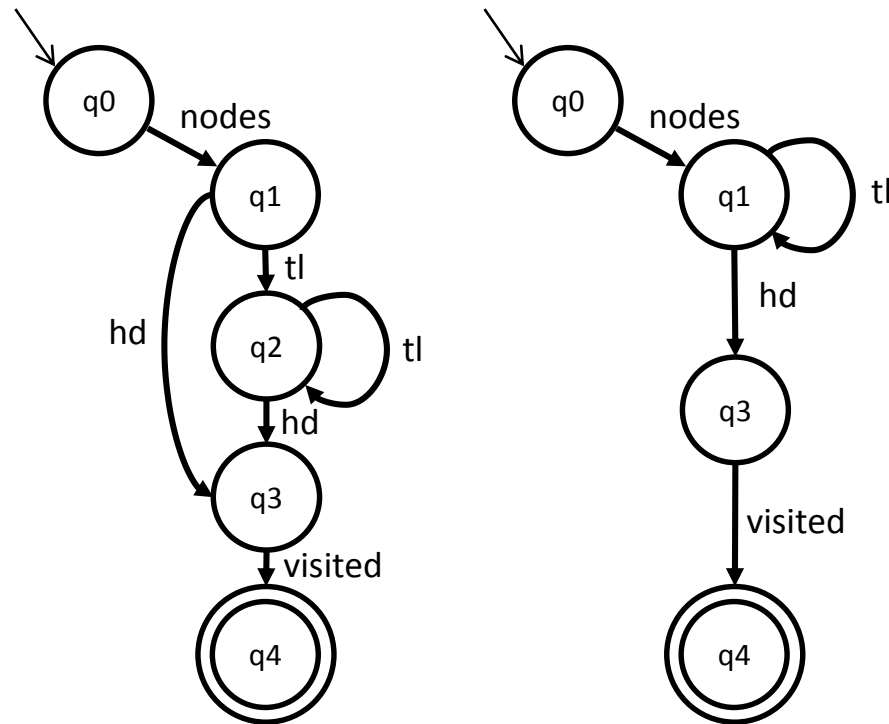
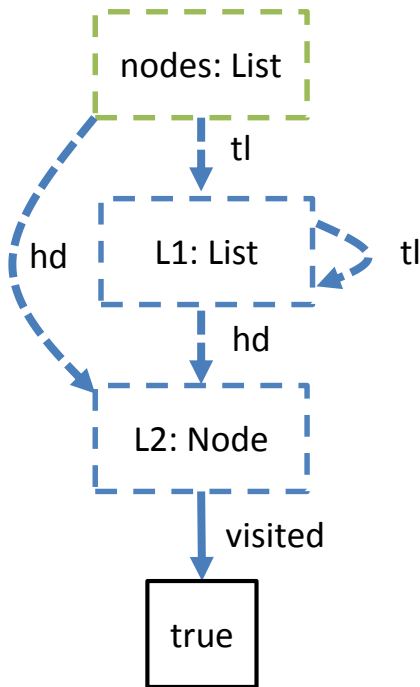
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- Translating effect graphs into automata



Producing Readable Summaries

- Translating effect graphs into automata



`nodes.tl*.hd.visited`

Analyzing Collections

Two operations:

Impure Traversal:	<code>col.foreach{ _.visited = true }</code>
Grow:	<code>e1 => col.append(e1)</code>

On four Scala collections:

- `immutable.TreeSet`
- `immutable.List`
- `mutable.HashSet`
- `mutable.LinkedList`

Analyzing Collections

- `immutable.TreeSet`:

Impure Traversal:	<code>es.tree(.right .left)*.key.visited</code>
Grow:	Pure

- `immutable.List`:

Impure Traversal:	<code>es.tl*.hd.visited</code>
Grow:	Pure

- `mutable.HashSet`:

Impure Traversal:	<code>es.table.store.visited</code>
Grow:	<code>es.tableSize es.table.store es.sizemap.store es.sizemap es.table</code>

- `mutable.LinkedList`:

Impure Traversal:	<code>es.next*.elem.visited</code>
Grow:	<code>es.next.next*</code>

Selected Related Work

- Salcianu, A.D.: **Pointer Analysis for Java Programs: Novel Techniques and Applications**. Ph.D thesis, MIT (2006)
- Madhavan, R., Ramalingam, G. Waswani, K.: **Modular heap analysis for higher-order programs**. SAS 2012
- Rytz, L., Odersky, M., Haller, P.: **Lightweight polymorphic effects**. ECOOP 2012

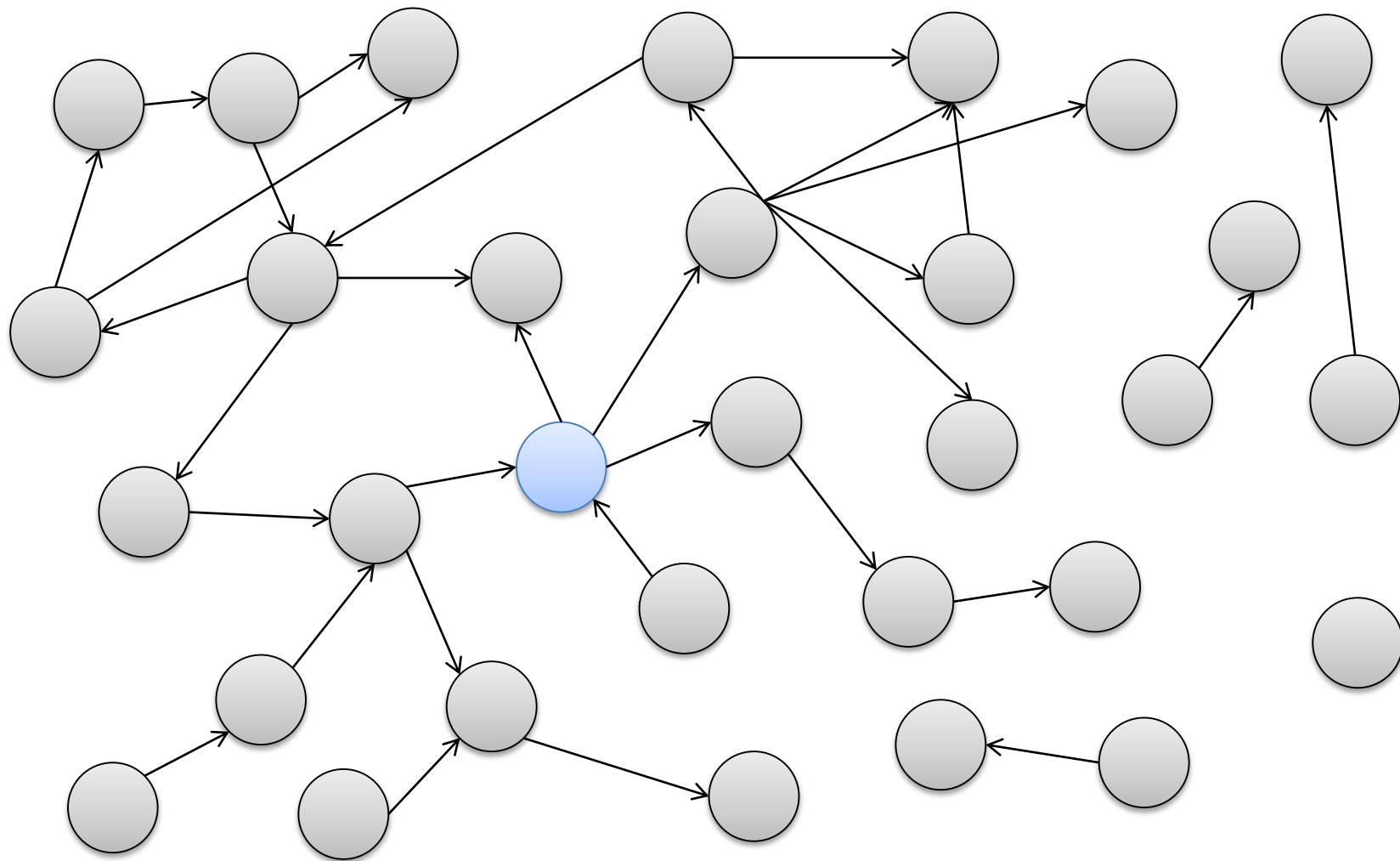
Contributions

- A precise pointer and effect analysis
flow-sensitive, modular, supports higher-order functions, requires no annotations
- A translation of effects to readable summaries
- Insane, an analyzer for Scala programs

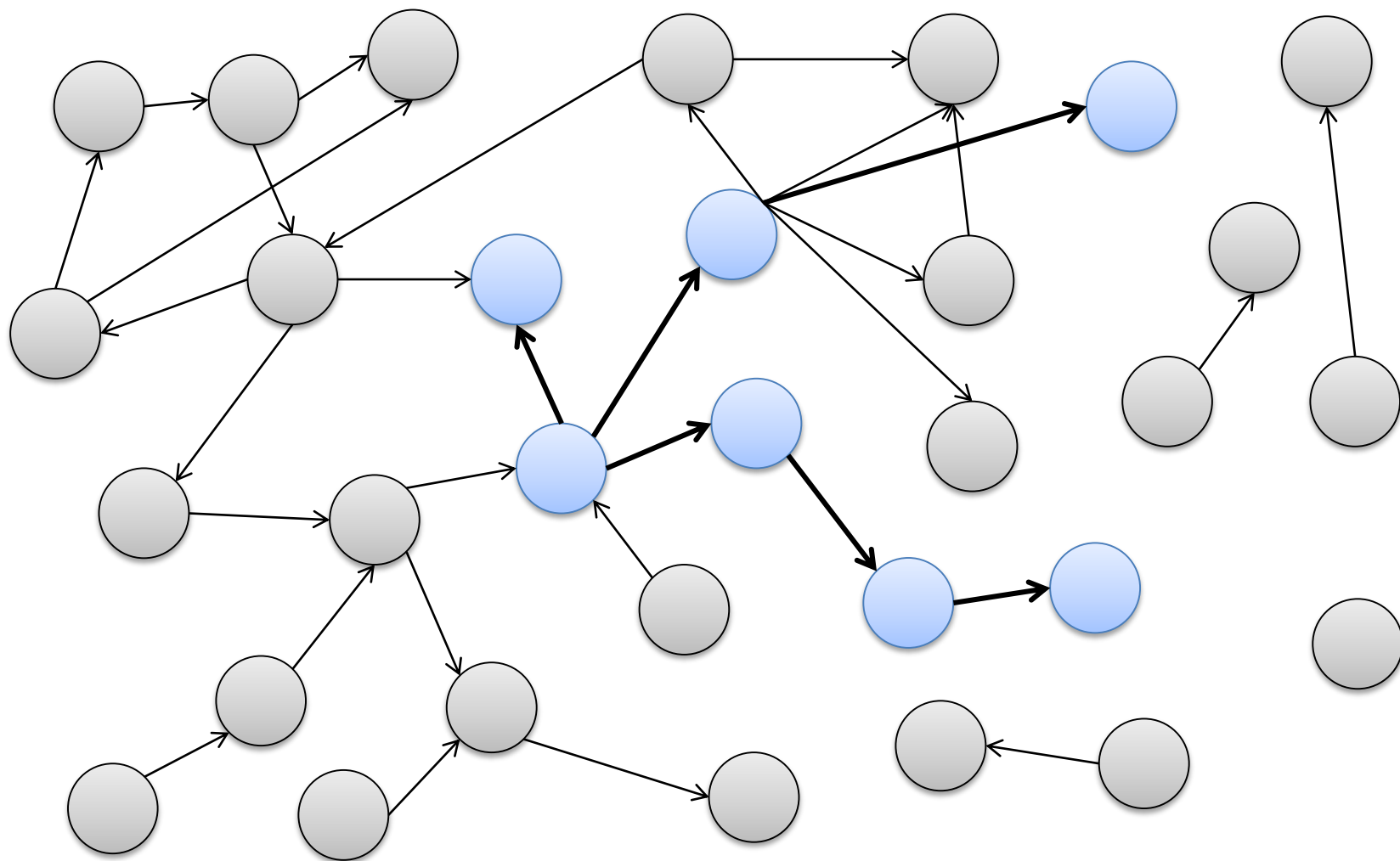


<https://github.com/epfl-lara/insane>

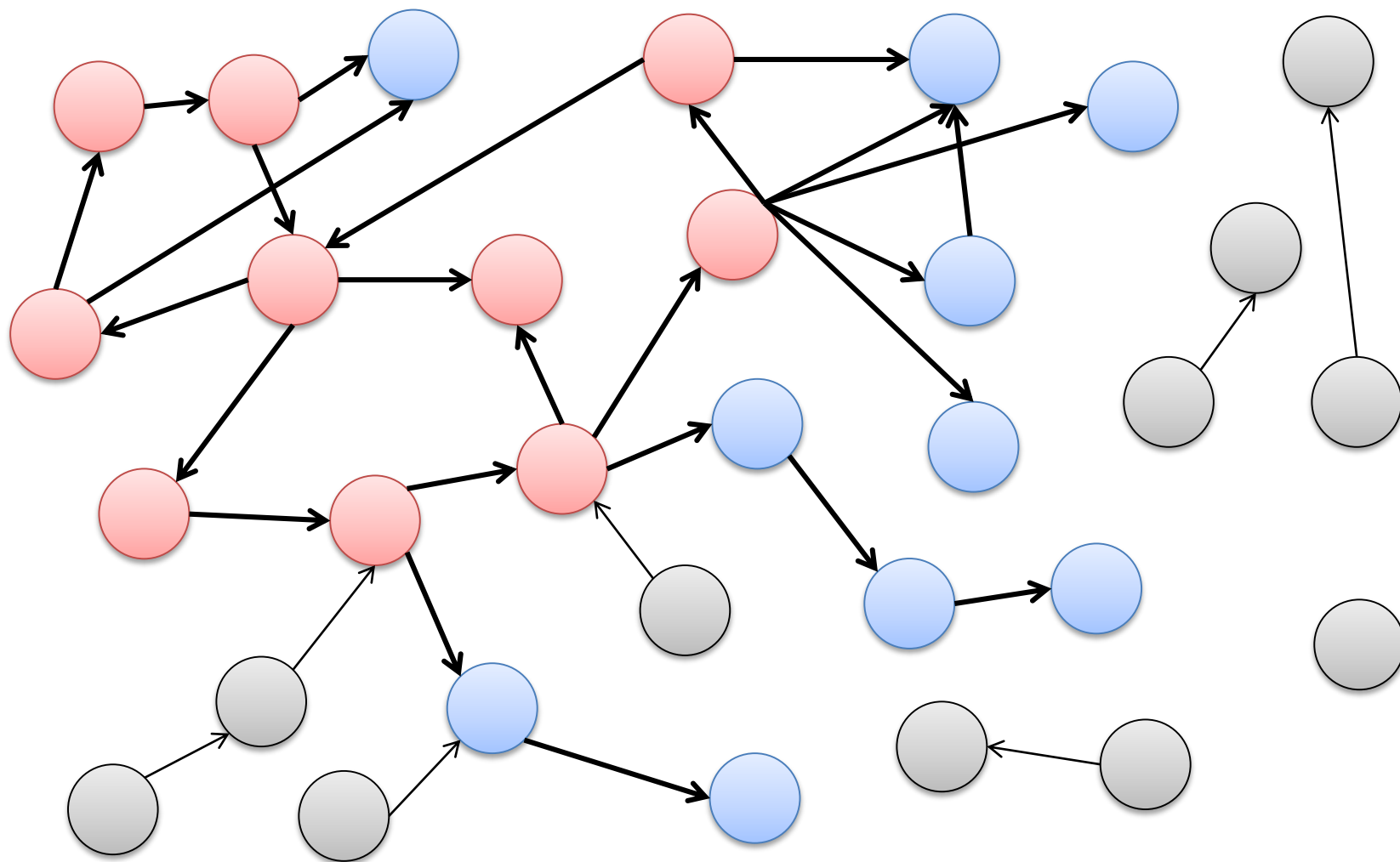
Static Call-Graph



Static Call-Graph



Static Call-Graph



Precision Evaluation

Four operations:

Generic Traversal:	<code>f => col.foreach{f}</code>
Pure Traversal:	<code>col.foreach{ () }</code>
Impure Traversal:	<code>col.foreach{ _.visited = true }</code>
Grow:	<code>el => col.append(el)</code>

Four collections:

- `immutable.TreeSet`
- `immutable.List`
- `mutable.HashSet`
- `mutable.LinkedList`

```
class Cell(var visited = false);
```

Effects Examples

- `immutable.TreeSet`:

Generic Traversal:	T
Pure Traversal:	Pure
Impure Traversal:	<code>es.tree(.right .left)*.key.visited</code>
Grow:	Pure

- `immutable.List`

Generic Traversal:	Pure (conditionally on the closure)
Pure Traversal:	Pure
Impure Traversal:	<code>es.tl*.hd.visited</code>
Grow:	Pure

Effects Examples

- mutable.HashSet

Generic Traversal:	Pure (conditionally on the closure)
Pure Traversal:	Pure
Impure Traversal:	es.table.store.visited
Grow:	es.tableSize es.table.store es.sizemap.store es.sizemap es.table

- mutable.LinkedList

Generic Traversal:	Pure (conditionally on the closure)
Pure Traversal:	Pure
Impure Traversal:	es.next*.elem.visited
Grow:	es.next.next*

Higher-order Functions

```
def mapHead(l: List, f: Int => Int): List = {  
  new List(f(l.head), l.tail)  
}  
def test(l: List) {  
  mapHead(l, x => x+1)  
  mapHead(l, x => {l.tail = null; 0})  
}
```


Higher-order Functions

```
def mapHead(l: List, f: Int => Int): List = {  
  new List(f(l.head), l.tail)  
}  
def test(l: List) {  
  mapHead(l, x => x+1)  
  mapHead(l, x => {l.tail = null; 0})  
}
```

- Reduces to dynamic dispatch:

```
def mapHead(l: List, f: Function1[Int, Int]): List = {  
  new List(f.apply(l.head), l.tail)  
}  
def test(l: List): List = {  
  mapHead(l, new Anon1())  
  mapHead(l, new Anon2(l))  
}  
class Anon1 extends Function1[Int, Int] {  
  def apply(i: Int) = i + 1  
}  
class Anon2(l: List) extends Function1[Int, Int] {  
  def apply(i: Int) = {l.tail = null; 0 }  
}
```

Motivation

```
class Cell {
  var visited = false
}

def toggle(c: Cell) {
  c.visited = !c.visited
}

def apply(c: Cell, f: Function1[Cell, Unit]) {
  f.apply(c)
}

def visitAll(cs: List[Cell]) {
  cs.foreach(new Closure1())
}

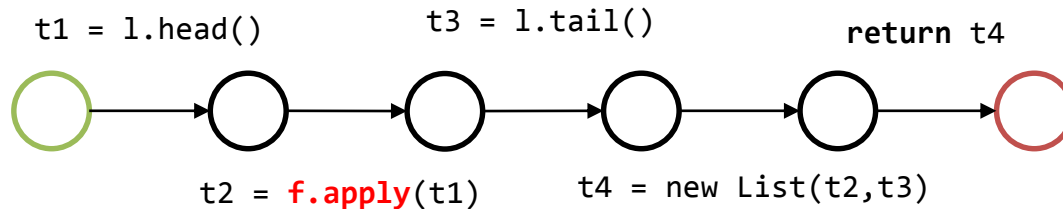
class Closure1() extends Function1[Cell, Unit] {
  def apply(c: Cell) { c.visited = true }
}
```

Delaying Effect Composition

```
def mapHead(l: List, f: Function1[Int, Int]): List = {  
  new List(f.apply(l.head), l.tail)  
}
```

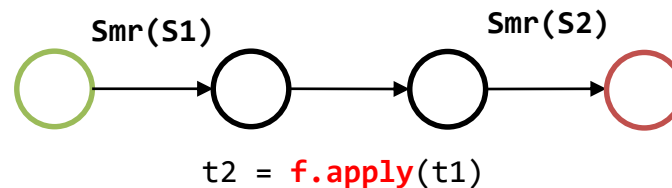
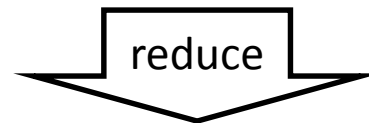
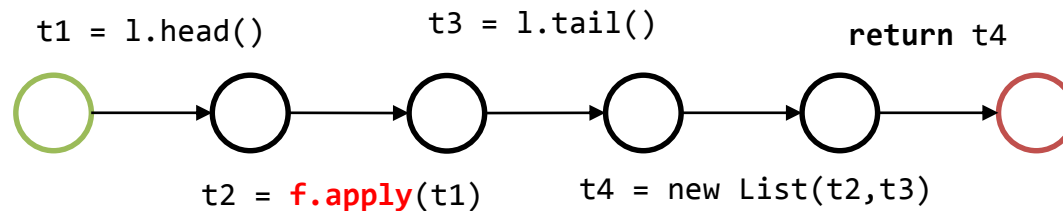
Delaying Effect Composition

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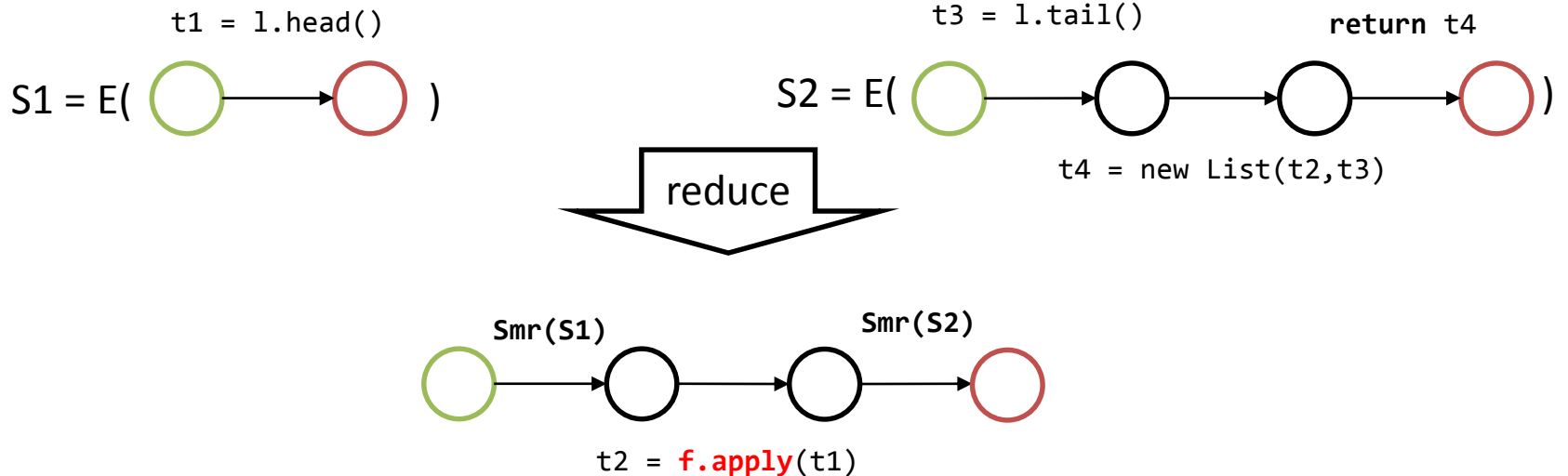
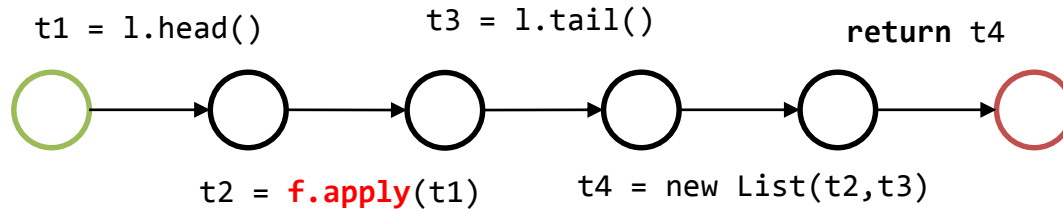
Delaying Effect Composition

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}
```



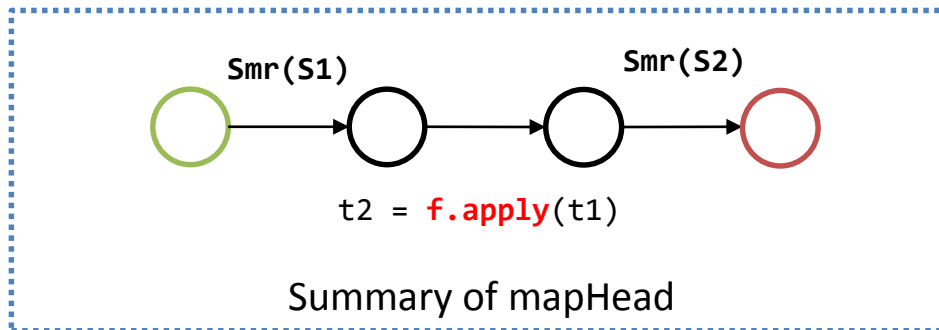
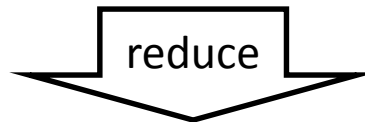
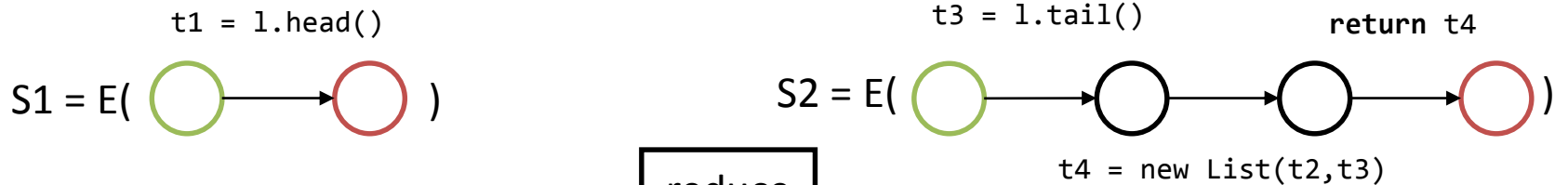
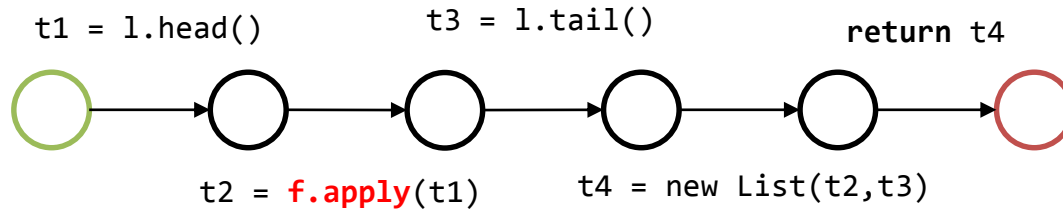
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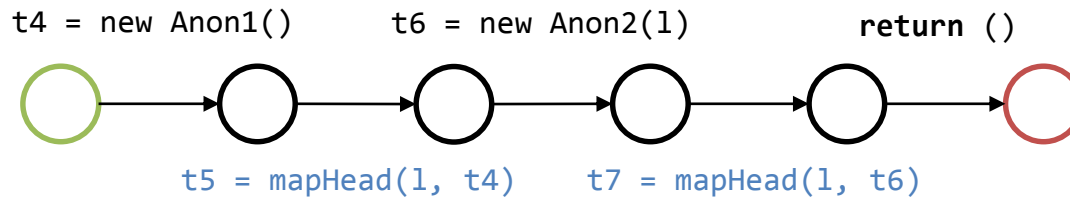
Delaying Effect Composition

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}
```



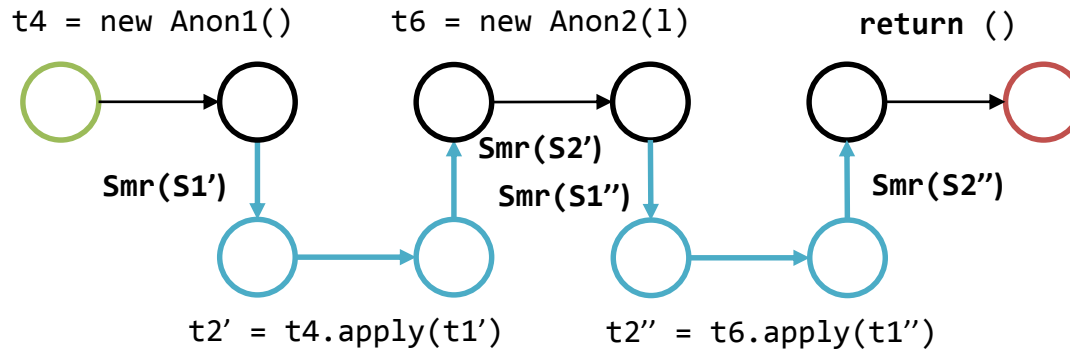
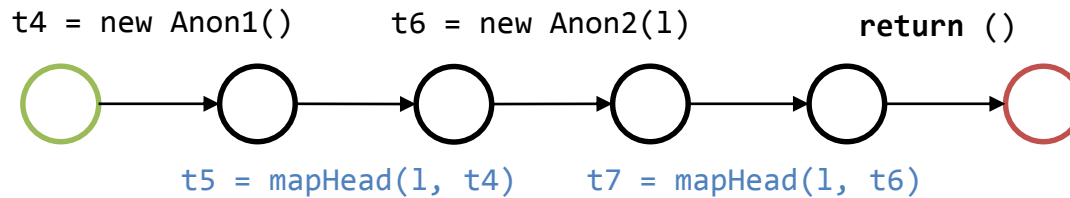
Delaying Effect Composition

```
def test(l: List) {  
  mapHead(l, new Anon1())  
  mapHead(l, new Anon2(l))  
}
```



Delaying Effect Composition

```
def test(l: List) {  
  mapHead(l, new Anon1())  
  mapHead(l, new Anon2(l))  
}
```



Results

Package	#Methods	Pure	Cond. Pure	Impure	T
scala	5721	79%	11%	10%	1%
scala.annotation	41	93%	2%	2%	2%
scala.beans	25	64%	8%	29%	8%
scala.collection	34810	46%	17%	29%	8%
scala.compat	9	22%	33%	44%	0%
scala.io	546	47%	11%	40%	2%
scala.math	1847	67%	28%	5%	0%
scala.parallel	39	77%	23%	0%	0%
scala.runtime	113	58%	3%	39%	0%
scala.sys	5862	50%	9%	40%	1%
scala.testing	44	52%	1%	43%	2%
scala.text	115	87%	0%	11%	2%
scala.util	1786	51%	11%	32%	6%
scala.util.parsing	2206	56%	12%	27%	5%
scala.xml	2860	56%	11%	30%	3%
Total	58410	52%	15%	27%	6%

Composition

- We define composition as applying an effect within another effect:

$$E_{res} = E_{outer} \diamond E_{inner}$$

satisfying:

$$\gamma(E_{res}) \cong \gamma(E_{outer}) \circ \gamma(E_{inner})$$

$$\gamma: E \rightarrow 2^{H \times H}$$