

$$a \leq b \Leftrightarrow (a \leq_1 b \wedge \cdots \wedge a \leq_n b)$$