

$$(x, y) \in \bigcap S \wedge (y, z) \in \bigcap S \rightarrow (x, y) \in r_1, (x, y) \in r_2, (y, z) \in r_1, (y, z) \in r_2$$