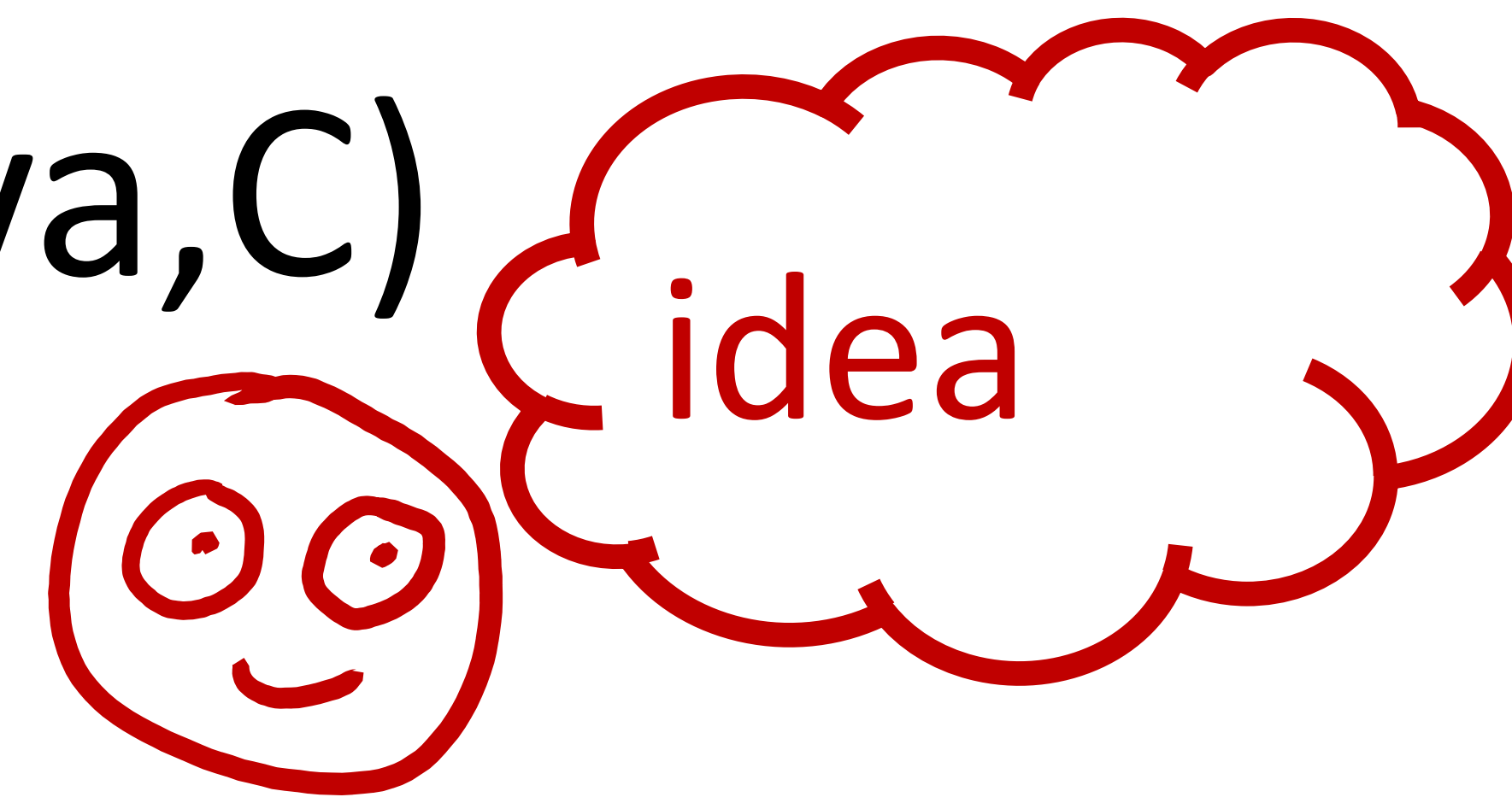


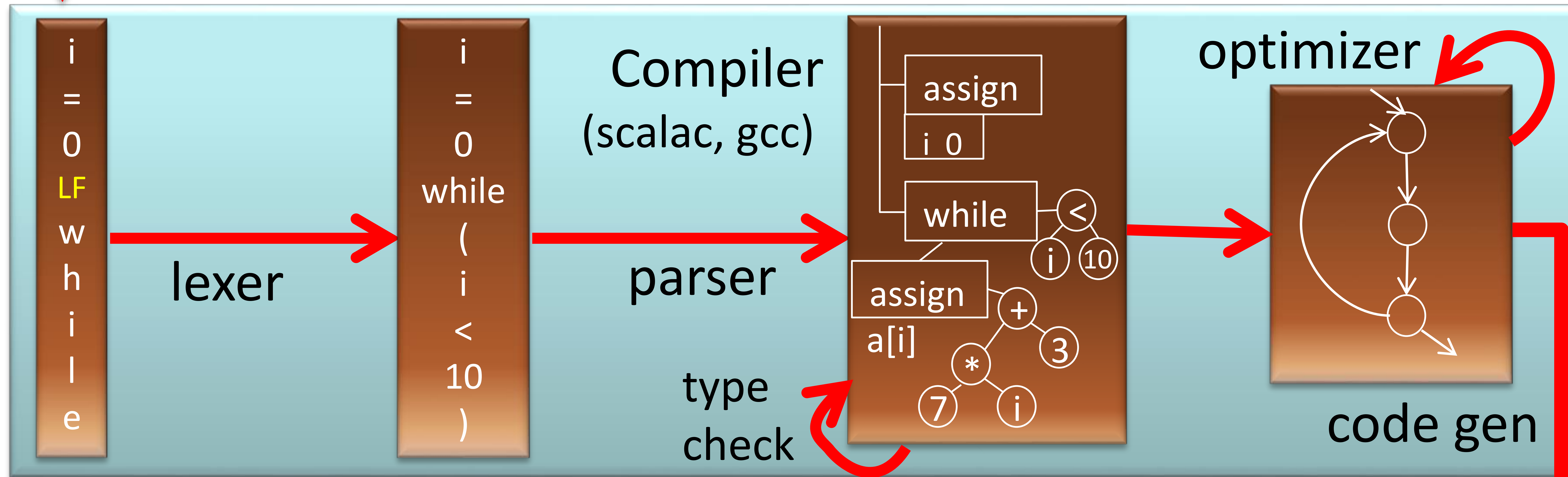
# Code Generation: Introduction

```
i=0
while (i < 10) {
  a[i] = 7*i+3
  i = i + 1
}
```

source code  
(e.g. Scala, Java, C)  
*easy to write*



data-flow graphs



characters

words

trees

machine code  
(e.g. x86, arm, JVM, WebAssembly)  
*efficient to execute*

```
mov R1,#0
mov R2,#40
mov R3,#3
jmp +12
mov (a+R1),R3
add R1, R1, #4
add R3, R3, #7
cmp R1, R2
blt -16
```



# Example: gcc

test.c

```
#include <stdio.h>
int main() {
    int i = 0;
    int j = 0;
    while (i < 10) {
        printf("%d\n", j);
        i = i + 1;
        j = j + 2*i+1;
    }
}
```

gcc test.c -S

test.s

```
        jmp .L2
.L3:    movl -8(%ebp), %eax
        movl %eax, 4(%esp)
        movl $.LC0, (%esp)
        call printf
        addl $1, -12(%ebp)
        movl -12(%ebp), %eax
        addl %eax, %eax
        addl -8(%ebp), %eax
        addl $1, %eax
        movl %eax, -8(%ebp)
.L2:    cmpl $9, -12(%ebp)
        jle .L3
```

What did (i<10) compile to?



# javac example

```
while (i < 10) {  
    System.out.println(j);  
    i = i + 1;  
    j = j + 2*i+1;  
}
```

```
javac Test.java  
javap -c Test
```

```
4: iload_1  
5: bipush 10  
7: if_icmpge 32  
10: getstatic #2; //System.out  
13: iload_2  
14: invokevirtual #3; //println  
17: iload_1  
18: iconst_1  
19: iadd  
20: istore_1  
21: iload_2  
22: iconst_2  
23: iload_1  
24: imul  
25: iadd  
26: iconst_1  
27: iadd  
28: istore_2  
29: goto 4  
32: return
```

Guess what each JVM instruction for the highlighted expression does.

# Java Virtual Machine

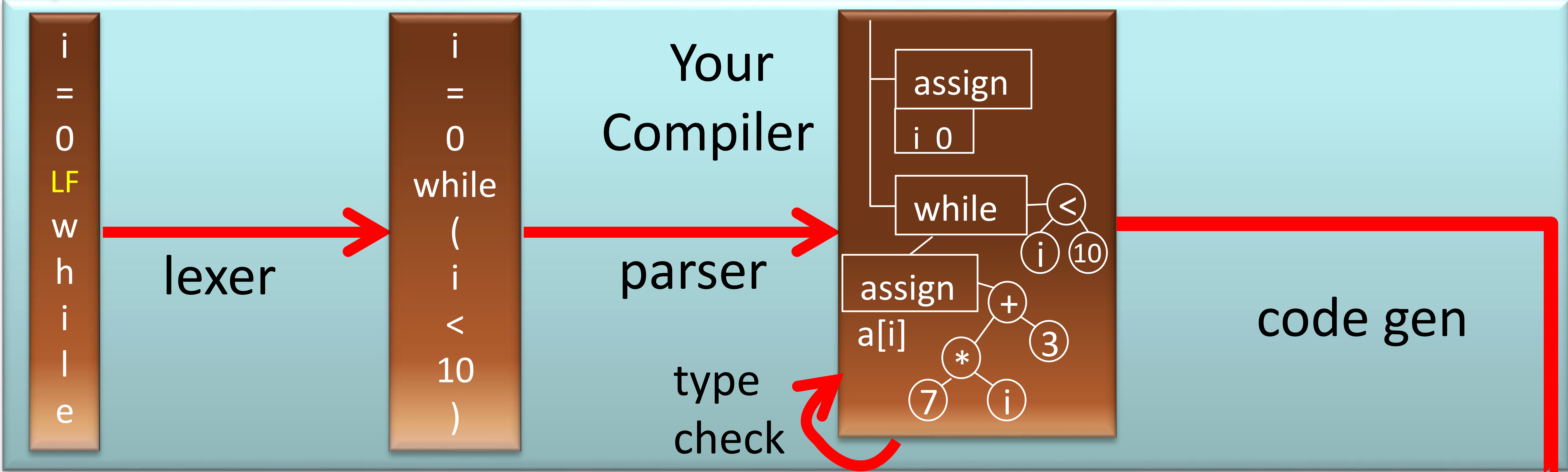
Use: **javac -g \*.java** to compile  
**javap -c -l ClassName** to explore

<https://docs.oracle.com/javase/specs/jvms/se8/html/jvms-2.html#jvms-2.11>

# Your Project

```
i=0  
while (i < 10) {  
  a[i] = 7*i+3  
  i = i + 1  
}
```

source code  
Amy  
language



characters

words

trees

## WebAssembly (WA) Bytecode

```
get_local 0  
get_local 0  
i64.const 1  
i64.sub  
call 0  
i64.mul
```



# WebAssembly

- Overview of bytecodes:  
<http://webassembly.org/docs/semantics/>
- Compiling from C:  
<http://webassembly.org/getting-started/developers-guide/>  
<https://hacks.mozilla.org/2017/03/previewing-the-webassembly-explorer/>
- Research paper and the talk:  
[\*Bringing the Web up to Speed with WebAssembly\*](#)  
[by Andreas Haas, Andreas Rossberg, Derek Schuff, Ben L. Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman.](#)  
[ACM SIGPLAN Conf. Programming Language Design and Implementation \(PLDI\), 2017.](#)

# WebAssembly example

## C++

```
int factorial(int n) {  
    if (n == 0)  
        return 1;  
    else  
        return n * factorial(n-1);  
}
```

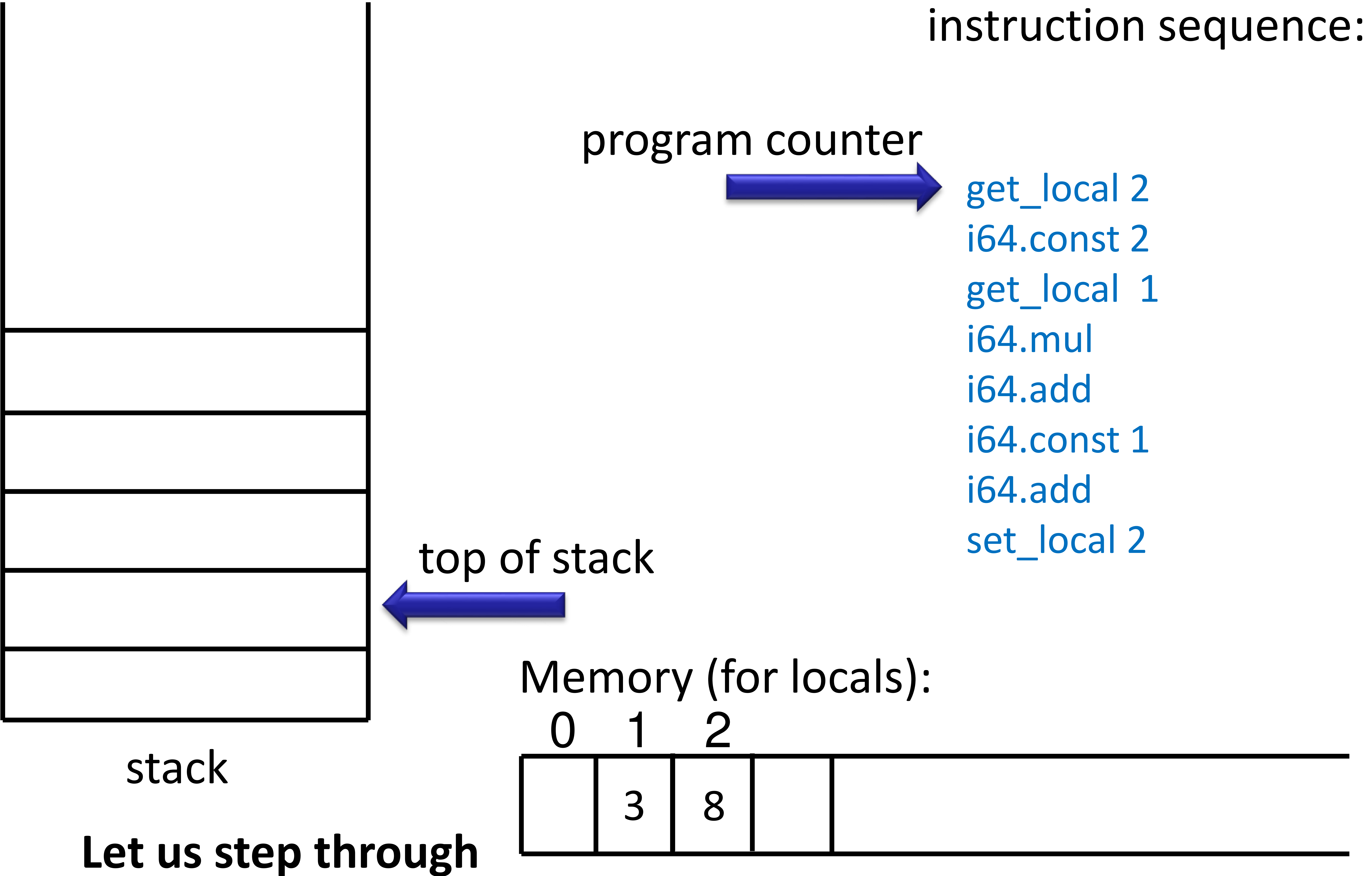
## WebAssembly

```
get_local 0    // n  
i64.const 0    // 0  
i64.eq         // n==0 ?  
if i64  
    i64.const 1 // 1  
else  
    get_local 0 // n  
    get_local 0 // n  
    i64.const 1 // 1  
    i64.sub     // n-1  
    call 0      // f(n-1)  
    i64.mul     // n*f(n-1)  
end
```

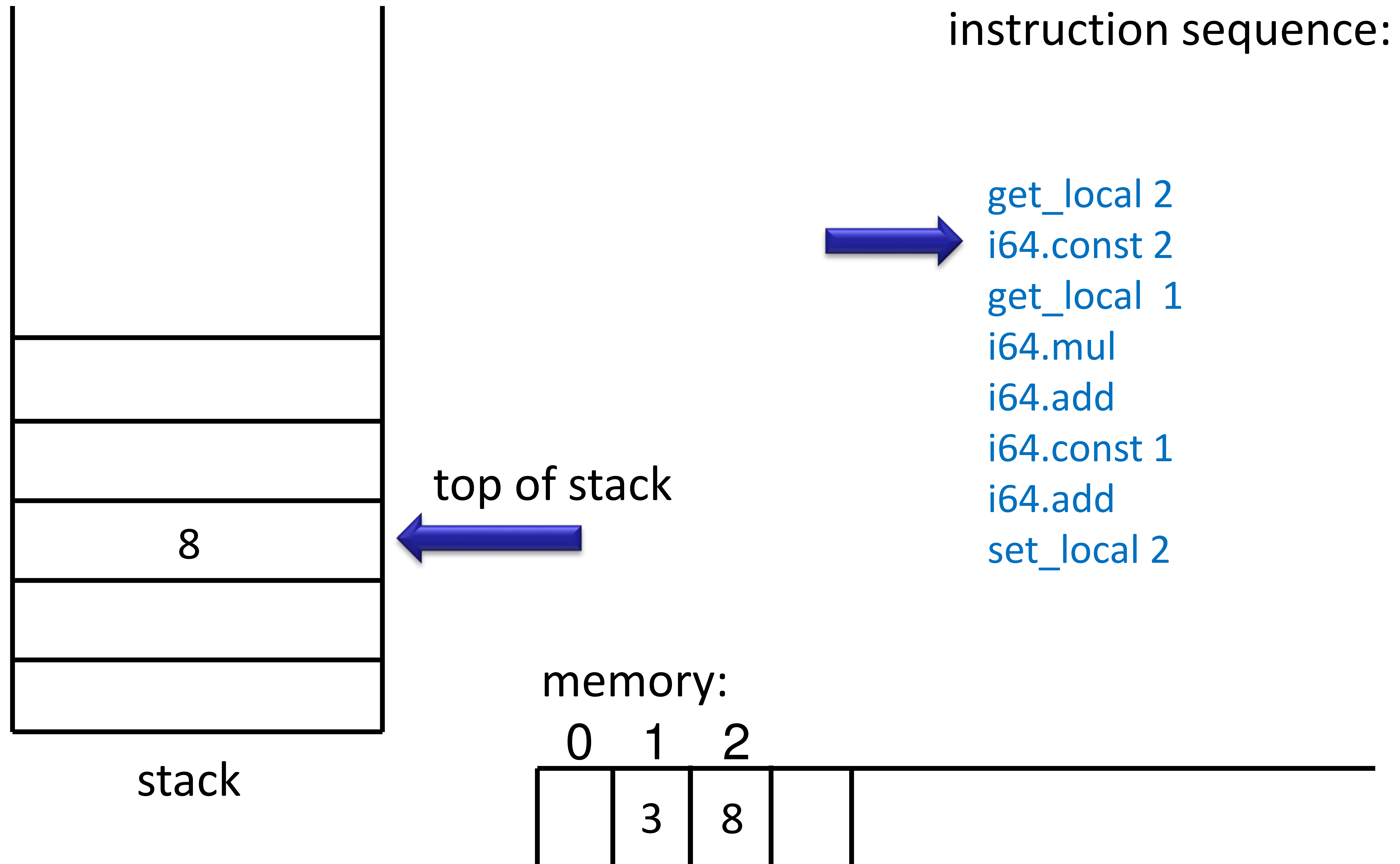
More at: <https://mbebenita.github.io/WasmExplorer/>



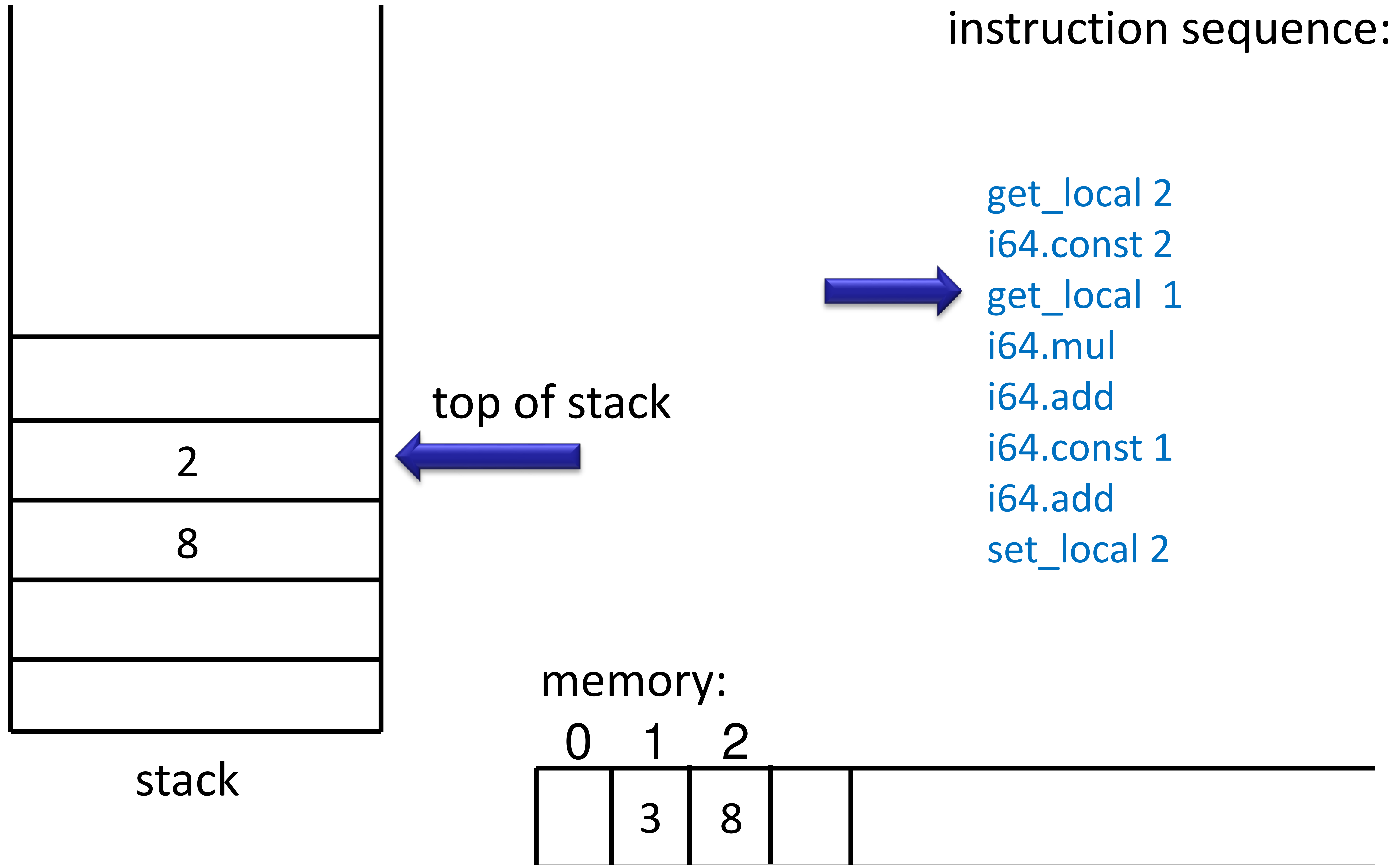
# Stack Machine: High-Level Machine Code



# Operands are consumed from stack and put back onto stack

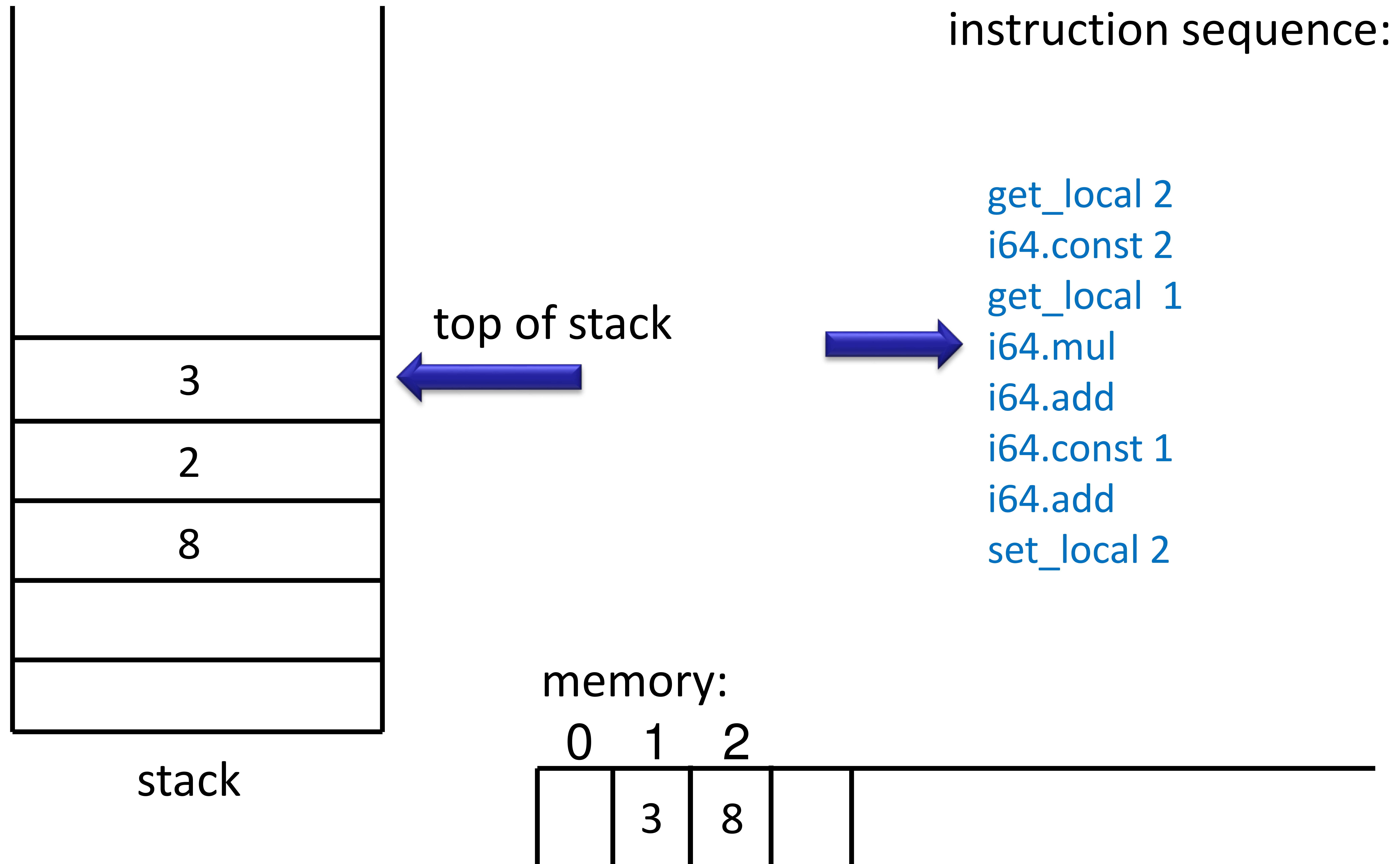


# Operands are consumed from stack and put back onto stack

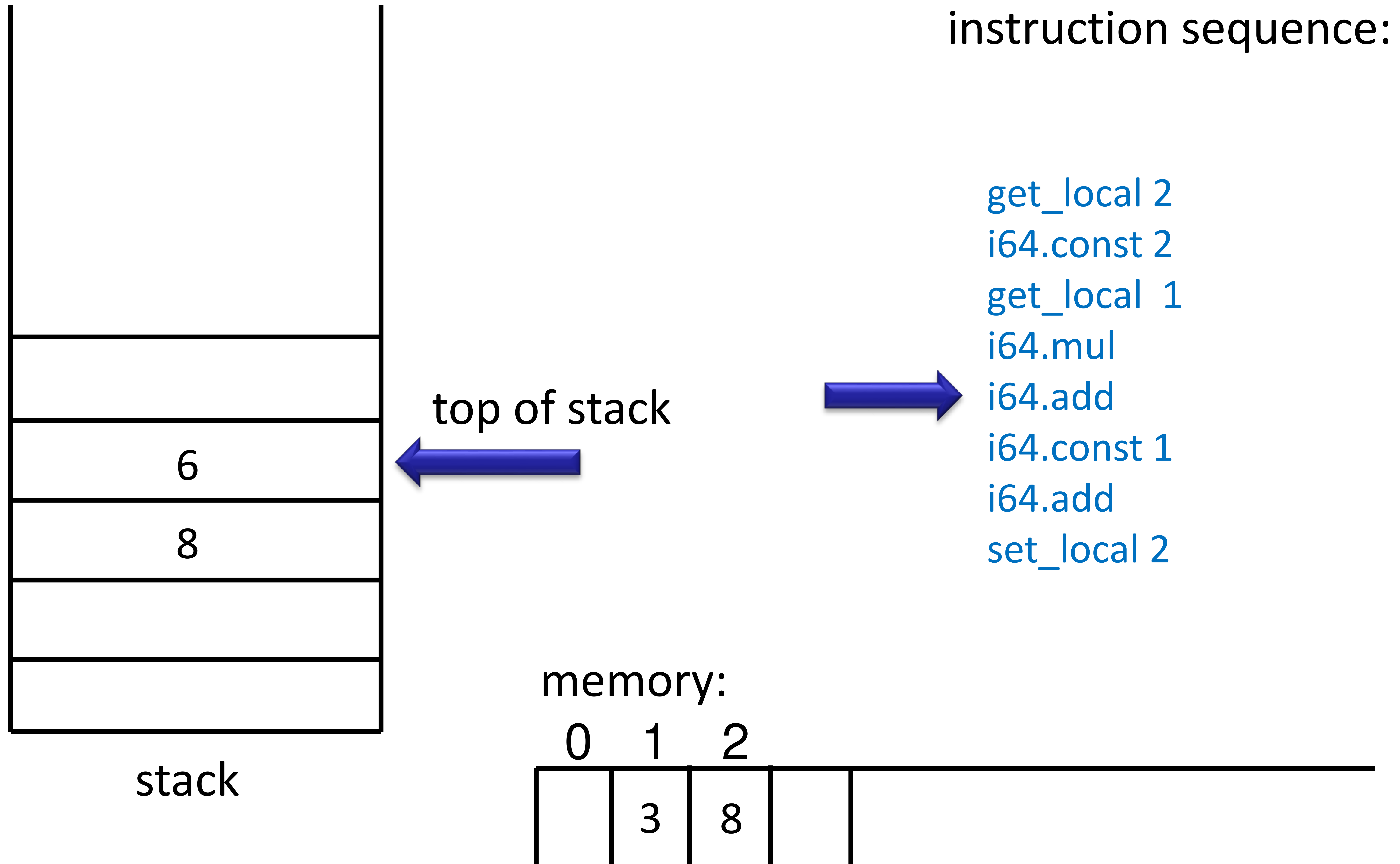




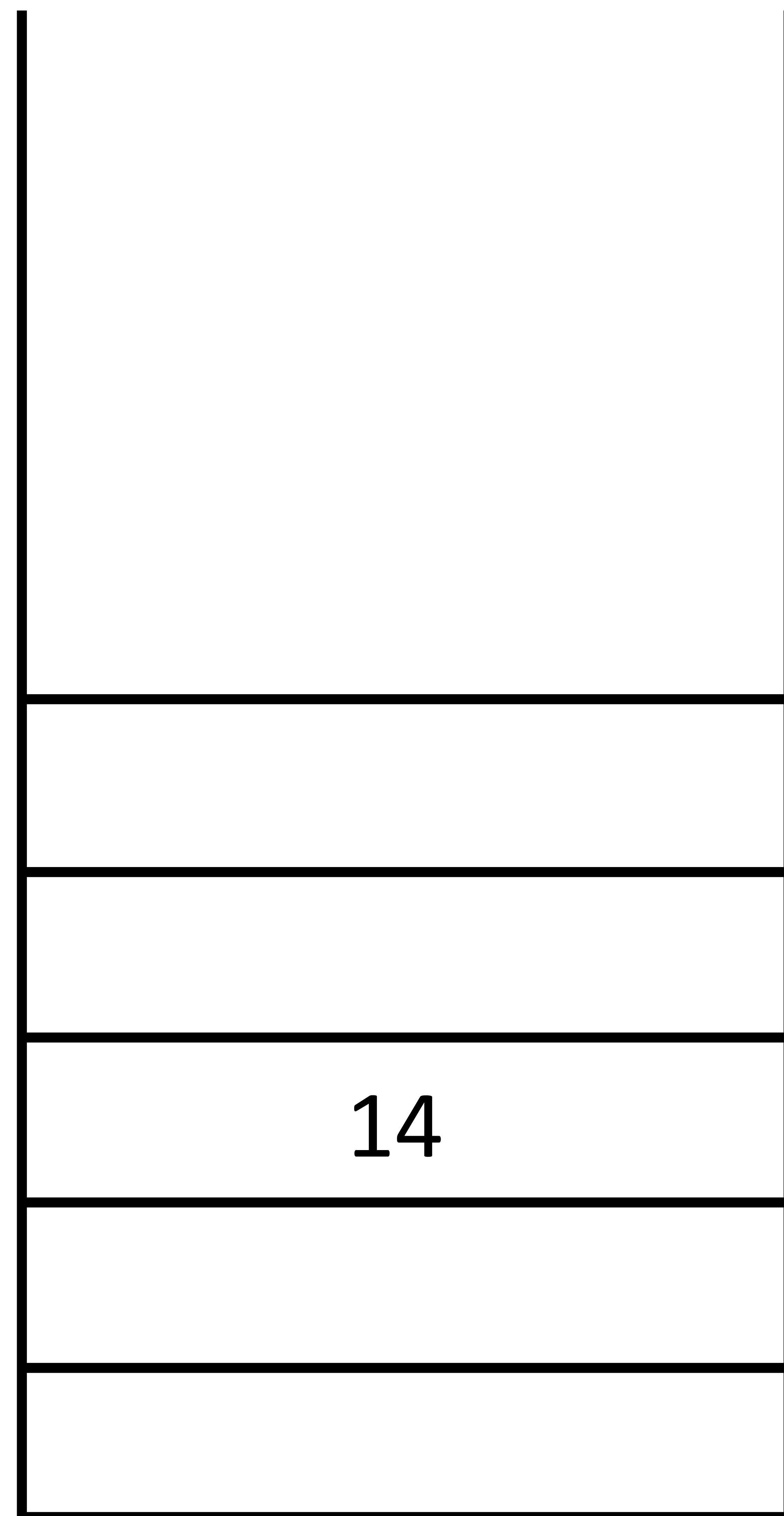
# Operands are consumed from stack and put back onto stack



# Operands are consumed from stack and put back onto stack



# Operands are consumed from stack and put back onto stack



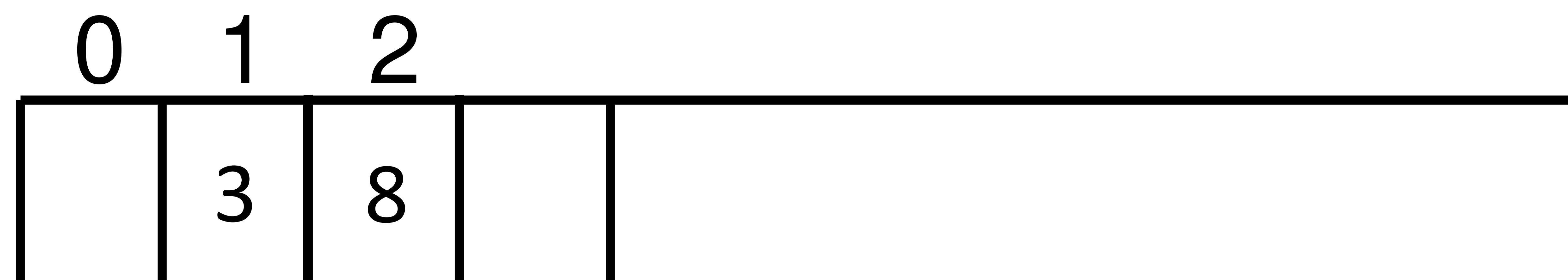
stack

instruction sequence:

```
get_local 2  
i64.const 2  
get_local 1  
i64.mul  
i64.add  
i64.const 1  
i64.add  
set_local 2
```

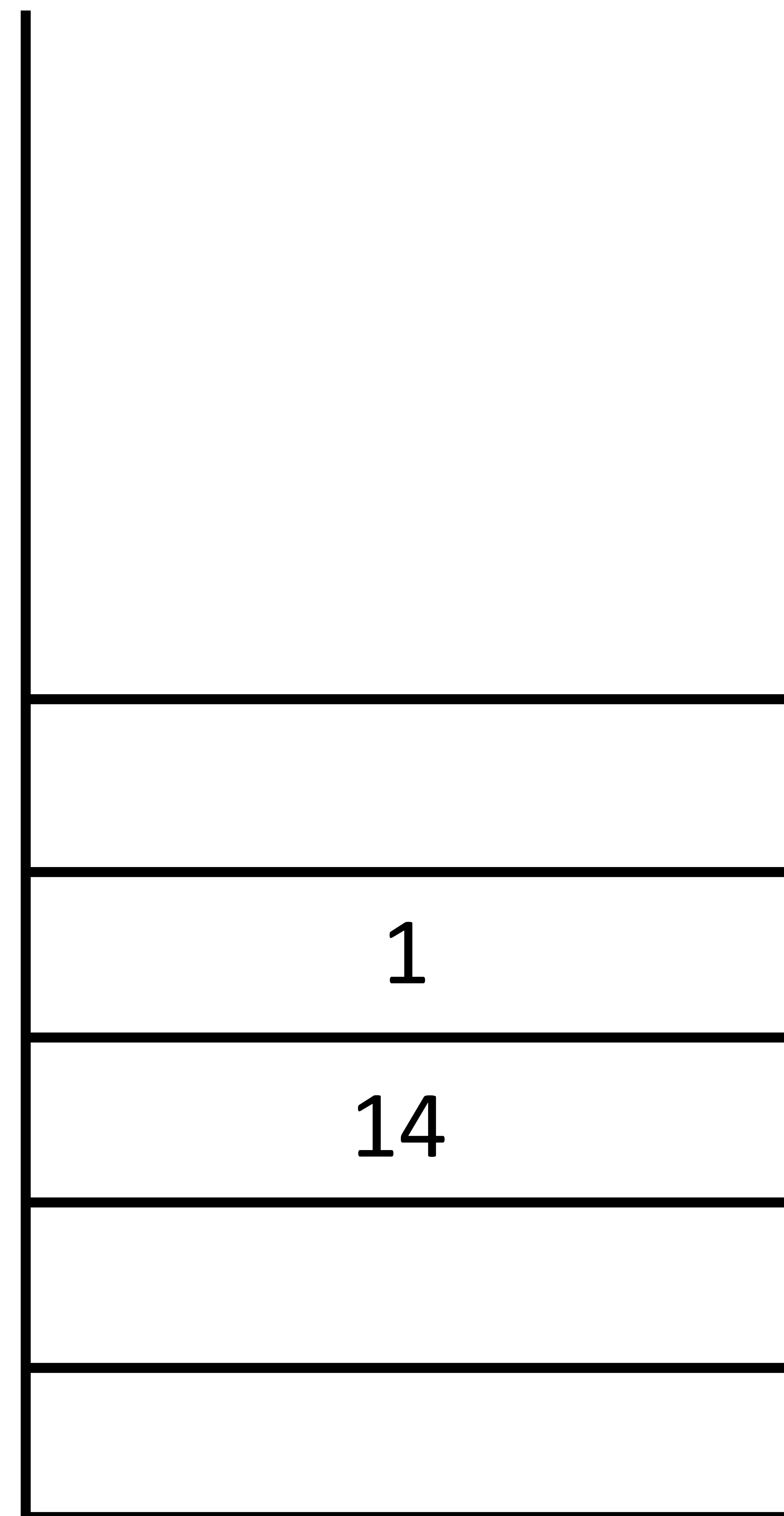


memory:





# Operands are consumed from stack and put back onto stack

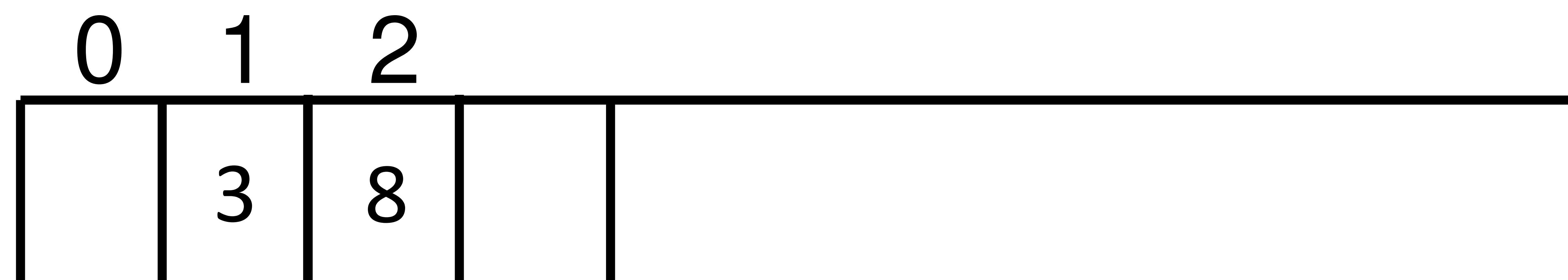


stack

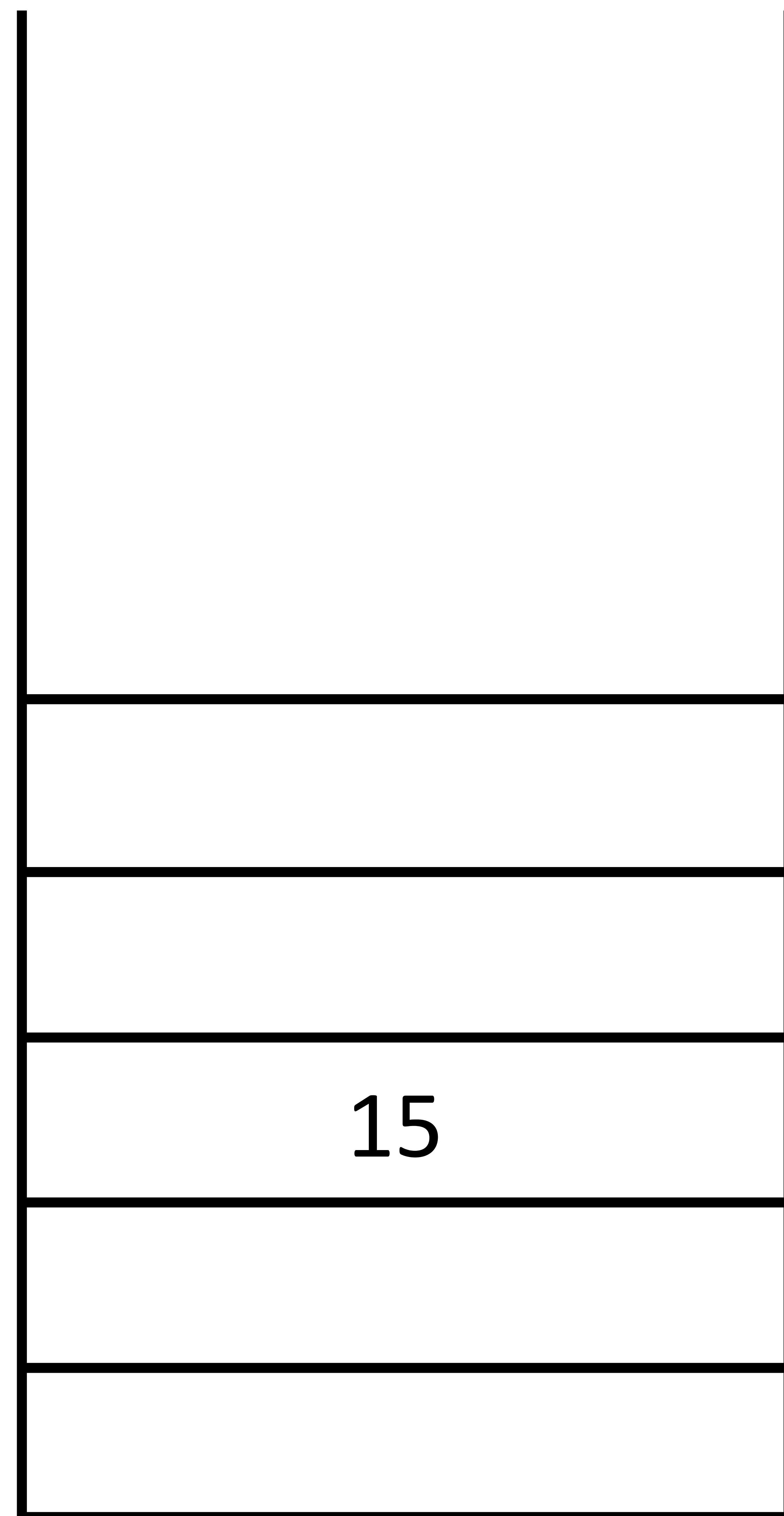
instruction sequence:

```
get_local 2  
i64.const 2  
get_local 1  
i64.mul  
i64.add  
i64.const 1  
i64.add  
set_local 2
```

memory:



# Operands are consumed from stack and put back onto stack



stack

top of stack



instruction sequence:

```
get_local 2  
i64.const 2  
get_local 1  
i64.mul  
i64.add  
i64.const 1  
i64.add  
set_local 2
```

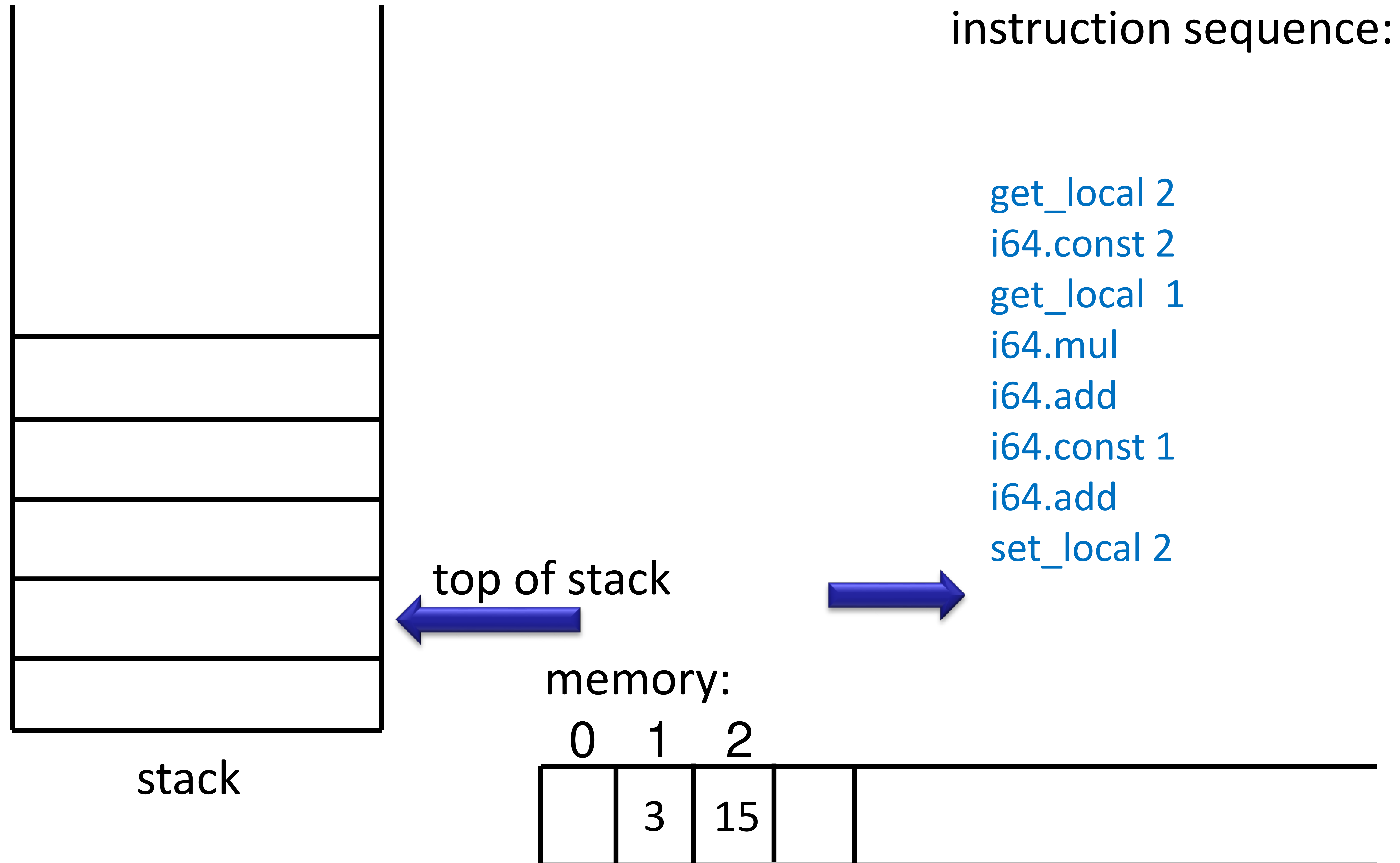


memory:

0 1 2



# Operands are consumed from stack and put back onto stack



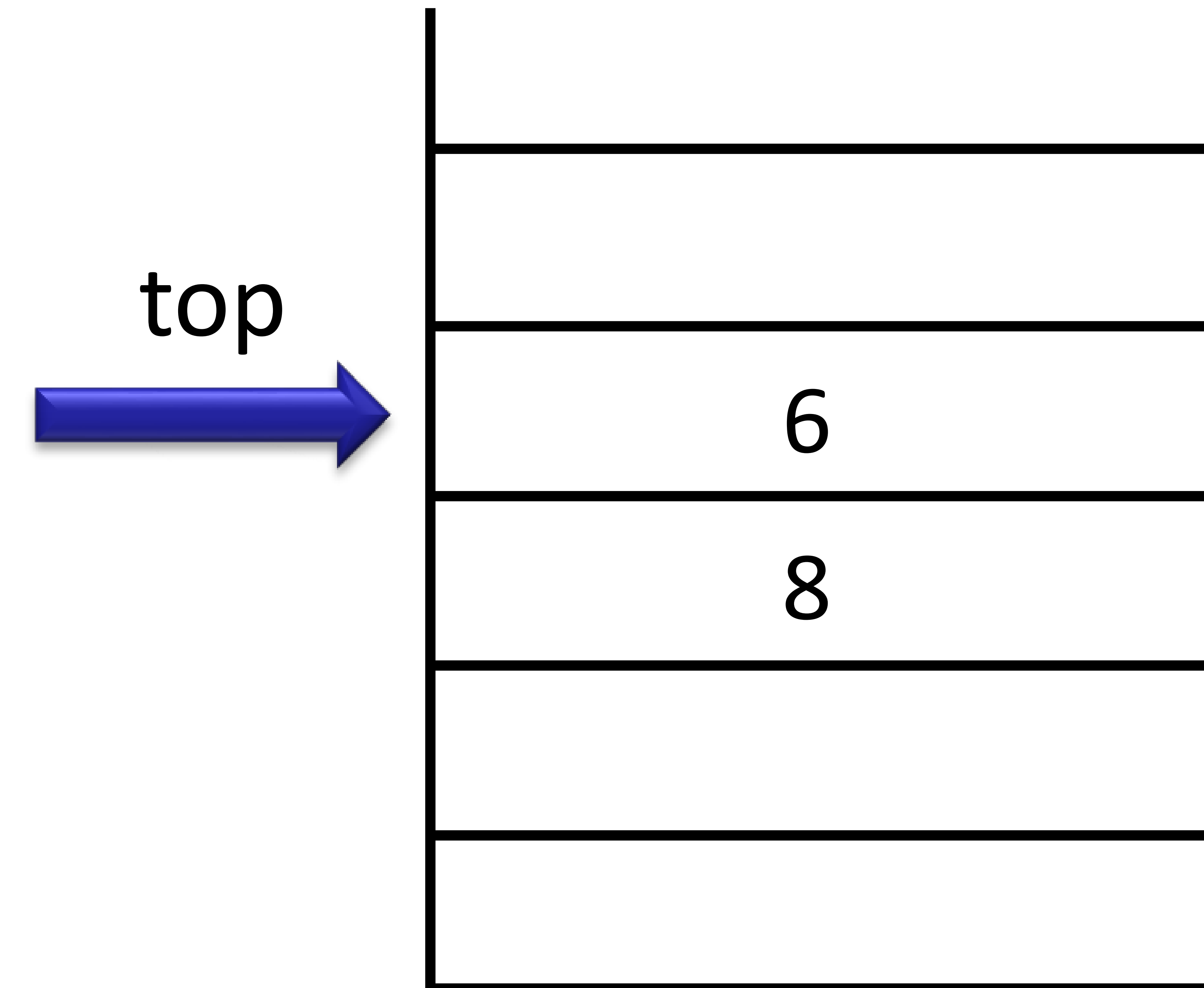


# Stack Machine Simulator

```
var code : Array[Instruction]
var pc : Int // program counter
var local : Array[Int] // for local variables
var operand : Array[Int] // operand stack
var top : Int
```

**while** (true) step

```
def step = code(pc) match {
  case ladd() =>
    operand(top - 1) = operand(top - 1) + operand(top)
    top = top - 1 // two consumed, one produced
  case lmul() =>
    operand(top - 1) = operand(top - 1) * operand(top)
    top = top - 1 // two consumed, one produced
```



# Stack Machine Simulator: Moving Data

```
case iconst(c) =>  
  operand(top + 1) = c // put given constant 'c' onto stack  
  top = top + 1  
case lgetlocal(n) =>  
  operand(top + 1) = local(n) // from memory onto stack  
  top = top + 1  
case lsetlocal(n) =>  
  local(n) = operand(top) // from stack into memory  
  top = top - 1 // consumed  
}  
if (notJump(code(n)))  
  pc = pc + 1 // by default go to next instructions
```

WebAssembly reference interpreter in ocaml:

<https://github.com/WebAssembly/spec/tree/master/interpreter>

# Selected Instructions

Reading and writing locals (and parameters):

- **get\_local**: read the current value of a local variable
- **set\_local**: set the current value of a local variable
- **tee\_local**: like set\_local, but also returns the set value

Arithmetic operations (take args from stack, put result on stack):

**i32.add**: sign-agnostic addition

**i32.sub**: sign-agnostic subtraction

**i32.mul**: sign-agnostic multiplication (lower 32-bits)

**i32.div\_s**: signed division (result is truncated toward zero)

**i32.rem\_s**: signed remainder (result has the sign of the dividend x in x%y)

**i32.and**: sign-agnostic bitwise and

**i32.or**: sign-agnostic bitwise inclusive or

**i32.xor**: sign-agnostic bitwise exclusive or



# Comparisons, stack, memory

**i32.eq**: sign-agnostic compare equal

**i32.ne**: sign-agnostic compare unequal

**i32.lt\_s**: signed less than

**i32.le\_s**: signed less than or equal

**i32.gt\_s**: signed greater than

**i32.ge\_s**: signed greater than or equal

**i32.eqz**: compare equal to zero (return 1 if operand is zero, 0 otherwise)

There are also: 64 bit integer operations **i64.\_** and floating point **f32.\_**, **f64.\_**

**drop**: drop top of the stack

**i32.const C**: put a given constant **C** on the stack

Access to memory (given as one big array):

**i32.load**: get memory index from stack, load 4 bytes (little endian), put on stack

**i32.store**: get memory address and value, store value in memory as 4 bytes

Can also load/store small numbers by reading/writing fewer bytes, see

<http://webassembly.org/docs/semantics/>

# Example: Area

```
int fact(int a, int b, int c) {  
    return ((c+a)*b + c*a) * 2;  
}
```

```
(module (type $type0 (func (param i32 i32 i32)  
                            (result i32)))  
  
  (table 0 anyfunc) (memory 1)  
  (export "memory" memory)  
  (export "fact" $func0)  
  
  (func $func0 (param $var0 i32)  
              (param $var1 i32)  
              (param $var2 i32) (result i32)  
  
    get_local $var2  
    get_local $var0  
    i32.add  
    get_local $var1  
    i32.mul  
    get_local $var2  
    get_local $var0  
    i32.mul  
    i32.add  
    i32.const 1  
    i32.shl           // shift left, i.e. *2  
  ))
```

# Towards Compiling Expressions: Prefix, Infix, and Postfix Notation



# Overview of Prefix, Infix, Postfix

Let  $f$  be a binary operation,  $e_1 e_2$  two expressions

We can denote application  $f(e_1, e_2)$  as follows

– in **prefix** notation  $f e_1 e_2$

– in **infix** notation  $e_1 f e_2$

– in **postfix** notation  $e_1 e_2 f$

- Suppose that each operator (like  $f$ ) has a known number of arguments. For nested expressions
  - infix requires parentheses in general
  - prefix and postfix do not require any parantheses!

# Expressions in Different Notation

For infix, assume \* binds stronger than +

There is no need for priorities or parens in the other notations

<b>arg.list</b>	$+(x,y)$	$+(* (x,y),z)$	$+(x,* (y,z))$	$*(x,+(y,z))$
<b>prefix</b>	$+ x y$	$+ * x y z$	$+ x * y z$	$* x + y z$
<b>infix</b>	$x + y$	$x * y + z$	$x + y * z$	$x * (y + z)$
<b>postfix</b>	$x y +$	$x y * z +$	$x y z * +$	$x y z + *$

Infix is the only problematic notation and leads to ambiguity

Why is it used in math? Ambiguity reminds us of algebraic laws:

$x + y$  looks same from left and from right (commutative)

$x + y + z$  parse trees mathematically equivalent (associative)

# Convert into Prefix and Postfix

**prefix**

**infix**       $((x + y) + z) + u$        $x + (y + (z + u))$

**postfix**

draw the trees:

Terminology:

prefix = Polish notation

(attributed to Jan Lukasiewicz from Poland)

postfix = Reverse Polish notation (RPN)

Is the sequence of characters in postfix opposite to one in prefix if we have binary operations?

What if we have only unary operations?



# Compare Notation and Trees

<b>arg.list</b>	$+(x,y)$	$+(* (x,y),z)$	$+(x,* (y,z))$	$*(x,+(y,z))$
<b>prefix</b>	$+ x y$	$+ * x y z$	$+ x * y z$	$* x + y z$
<b>infix</b>	$x + y$	$x * y + z$	$x + y * z$	$x * (y + z)$
<b>postfix</b>	$x y +$	$x y * z +$	$x y z * +$	$x y z + *$

draw ASTs for each expression

How would you pretty print AST into a given form?

# Simple Expressions and Tokens

```
sealed abstract class Expr
```

```
case class Var(varID: String) extends Expr
```

```
case class Plus(lhs: Expr, rhs: Expr) extends Expr
```

```
case class Times(lhs: Expr, rhs: Expr) extends Expr
```

```
sealed abstract class Token
```

```
case class ID(str : String) extends Token
```

```
case class Add extends Token
```

```
case class Mul extends Token
```

```
case class O extends Token // (
```

```
case class C extends Token // )
```



# Printing Trees into Lists of Tokens

```
def prefix(e : Expr) : List[Token] = e match {  
  case Var(id) => List(ID(id))  
  case Plus(e1,e2) => List(Add()) ::: prefix(e1) ::: prefix(e2)  
  case Times(e1,e2) => List(Mul()) ::: prefix(e1) ::: prefix(e2)  
}  
  
def infix(e : Expr) : List[Token] = e match { // needs to emit parentheses  
  case Var(id) => List(ID(id))  
  case Plus(e1,e2) => List(O()) ::: infix(e1) ::: List(Add()) ::: infix(e2) ::: List(C())  
  case Times(e1,e2) => List(O()) ::: infix(e1) ::: List(Mul()) ::: infix(e2) ::: List(C())  
}  
  
def postfix(e : Expr) : List[Token] = e match {  
  case Var(id) => List(ID(id))  
  case Plus(e1,e2) => postfix(e1) ::: postfix(e2) ::: List(Add())  
  case Times(e1,e2) => postfix(e1) ::: postfix(e2) ::: List(Mul())  
}
```



# LISP: Language with Prefix Notation

- 1958 – pioneering language
- Syntax was meant to be abstract syntax
- Treats all operators as user-defined ones, so syntax does not assume the number of arguments is known
  - use parantheses in prefix notation: write  $f(x,y)$  as  $(f\ x\ y)$

```
(defun factorial (n)
  (if (<= n 1)
      1
      (* n (factorial (- n 1)))))
```

# PostScript: Language using Postfix

- .ps are ASCII files given to PostScript-compliant printers
- Each file is a program whose execution prints the desired pages
- <http://en.wikipedia.org/wiki/PostScript%20programming%20language>

PostScript language tutorial and cookbook

Adobe Systems Incorporated

Reading, MA : Addison Wesley, 1985

ISBN 0-201-10179-3 (pbk.)



# A PostScript Program

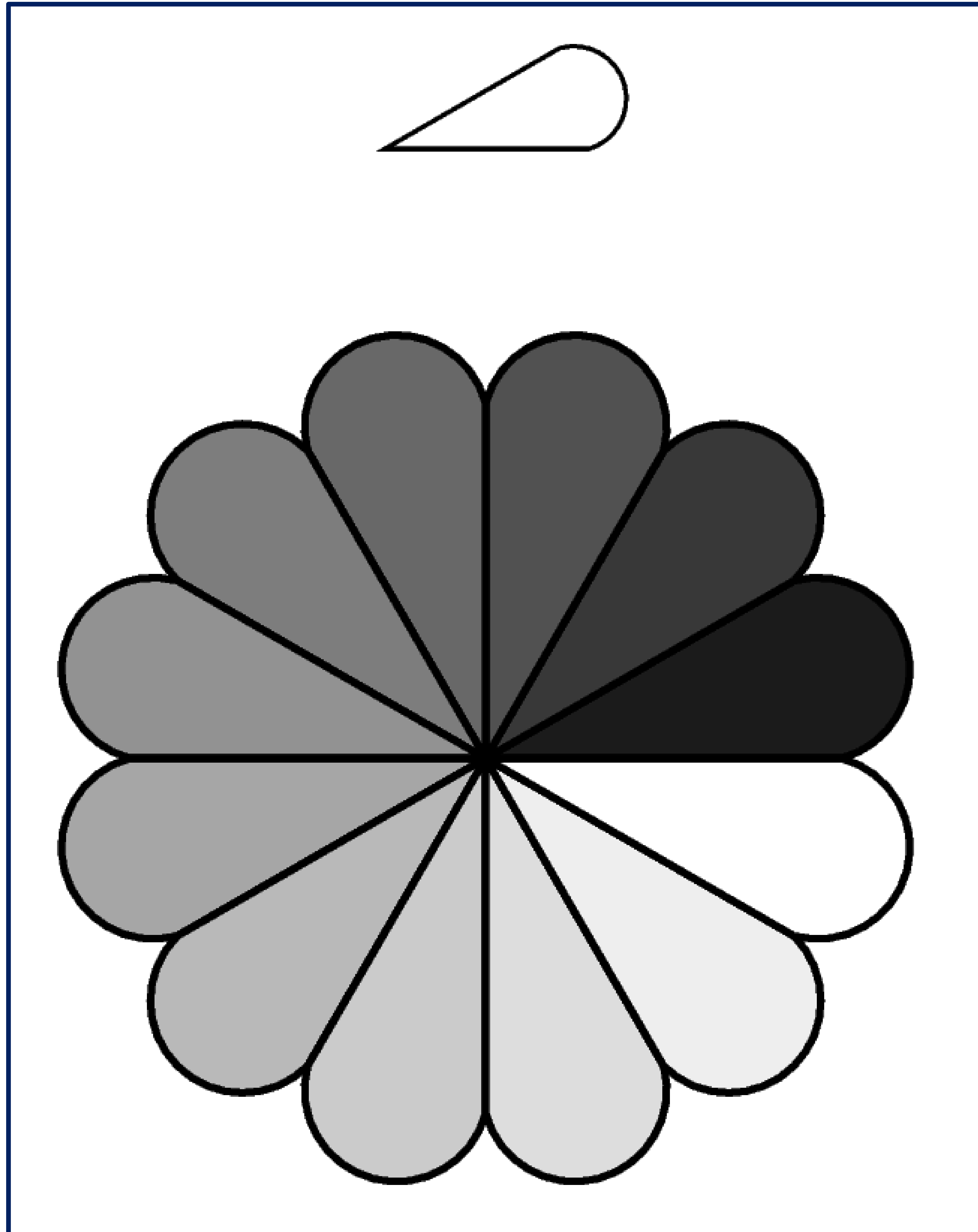
```
/inch {72 mul} def
/wedge
    { newpath
      0 0 moveto
      1 0 translate
      15 rotate
      0 15 sin translate
      0 0 15 sin -90 90 arc
      closepath
    } def
gsave
  3.75 inch 7.25 inch translate
  1 inch 1 inch scale
  wedge 0.02 setlinewidth stroke
grestore
gsave
```

```
4.25 inch 4.25 inch translate
1.75 inch 1.75 inch scale
0.02 setlinewidth
1 1 12
    { 12 div setgray
      gsave
        wedge
      gsave fill grestore
      0 setgray stroke
    grestore
    30 rotate
  } for
grestore
showpage
```

Related: [https://en.wikipedia.org/wiki/Concatenative\\_programming\\_language](https://en.wikipedia.org/wiki/Concatenative_programming_language)



If we send it to printer  
(or run GhostView viewer gv) we get



```
4.25 inch 4.25 inch translate
```

```
1.75 inch 1.75 inch scale
```

```
0.02 setlinewidth
```

```
1 1 12
```

```
{ 12 div setgray
```

```
gsave
```

```
wedge
```

```
gsave fill grestore
```

```
0 setgray stroke
```

```
grestore
```

```
30 rotate
```

```
} for
```

```
grestore
```

```
showpage
```

# Why postfix? Can evaluate it using stack

```
def postEval(env : Map[String,Int], pexpr : Array[Token]) : Int = { // no recursion!
  var stack : Array[Int] = new Array[Int](512)
  var top : Int = 0; var pos : Int = 0
  while (pos < pexpr.length) {
    pexpr(pos) match {
      case ID(v) => top = top + 1
                    stack(top) = env(v)
      case Add() => stack(top - 1) = stack(top - 1) + stack(top)
                    top = top - 1
      case Mul() => stack(top - 1) = stack(top - 1) * stack(top)
                    top = top - 1
    }
    pos = pos + 1
  }
  stack(top)
}
```

$x \rightarrow 3, y \rightarrow 4, z \rightarrow 5$

**infix:**  $x*(y+z)$

**postfix:**  $x y z + *$

Run 'postfix' for this env

# Evaluating Infix Needs Recursion

The recursive interpreter:

```
def infixEval(env : Map[String,Int], expr : Expr) : Int =  
expr match {  
  case Var(id) => env(id)  
  case Plus(e1,e2) => infix(env,e1) + infix(env,e2)  
  case Times(e1,e2) => infix(env,e1) * infix(env,e2)  
}
```

Maximal stack depth in interpreter = expression height



# Compiling Expressions

- Evaluating postfix expressions is like running a stack-based virtual machine on compiled code
- Compiling expressions for stack machine is like translating expressions into postfix form

# Expression, Tree, Postfix, Code

infix:  $x*(y+z)$

postfix:  $x\ y\ z\ +\ *$

bytecode:

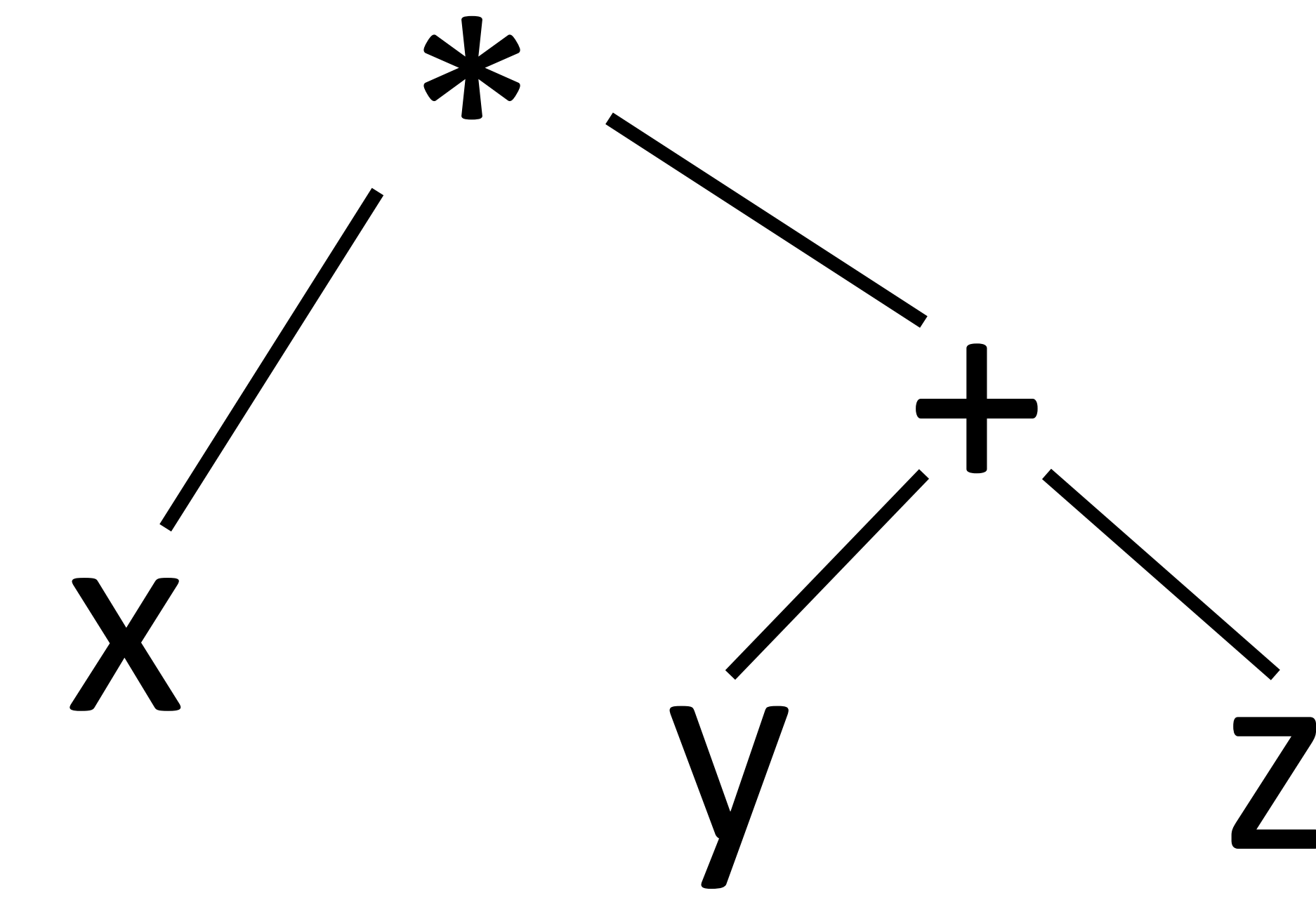
get\_local 1  $x$

get\_local 2  $y$

get\_local 3  $z$

i32.add  $+$

i32.mul  $*$



# Show Tree, Postfix, Code

infix:  $(x*y + y*z + x*z)*2$  tree:

postfix: bytecode:



# “Printing” Trees into Bytecodes

To evaluate  $e_1 * e_2$  interpreter

- evaluates  $e_1$
- evaluates  $e_2$
- combines the result using  $*$

Compiler for  $e_1 * e_2$  emits:

- code for  $e_1$  that leaves result on the stack, followed by
- code for  $e_2$  that leaves result on the stack, followed by
- arithmetic instruction that takes values from the stack and leaves the result on the stack

```
def compile(e : Expr) : List[Bytecode] = e match { // ~ postfix printer
  case Var(id) => List(lgetlocal(slotFor(id)))
  case Plus(e1,e2) => compile(e1) ::: compile(e2) ::: List(ladd())
  case Times(e1,e2) => compile(e1) ::: compile(e2) ::: List(lmul())
}
```

# Local Variables

- Assigning indices (called *slots*) to local variables using function  
slotOf : VarSymbol → {0,1,2,3,...}
- How to compute the indices?
  - assign them in the order in which they appear in the tree

```
def compile(e : Expr) : List[Bytecode] = e match {  
  case Var(id) => List(igetlocal(slotFor(id)))  
  ...  
}  
  
def compileStmt(s : Stmt) : List[Bytecode] = s match {  
  // id=e  
  case Assign(id,e) => compile(e) ::: List(iset_local(slotFor(id)))  
  ...  
}
```



# Compiler Correctness

If we execute the compiled code, the result is the same as running the interpreter.

$$\text{exec}(\text{env}, \text{compile}(\text{expr})) == \text{interpret}(\text{env}, \text{expr})$$

**interpret** : Env x Expr -> Int

**compile** : Expr -> List[Bytecode]

**exec** : Env x List[Bytecode] -> Int

Assume 'env' in both cases maps var names to values.

Can prove correctness of entire compiler:

[CompCert - A C Compiler whose Correctness has been Formally Verified](#)

CakeML project: <https://cakeml.org/>



# A simple proof with two quantifiers

A simple case of proof for (non-negative int  $y, x$ )

$$\forall y \forall x P(x, y)$$

is: *let  $y$  be arbitrary*, and then fix  $y$  throughout the proof.

Suppose that we prove

$$\forall x P(x, y)$$

by induction. We end up proving

$$P(0, y) \quad \text{for some arbitrary } y$$

$$P(x, y) \text{ implies } P(x+1, y) \quad \text{for arbitrary } x, y$$

# Induction with Quantified Hypothesis

Prove  $P$  holds for all non-negative integers  $x, y$ :

$$\forall x \forall y P(x, y) \quad \text{i.e.} \quad \forall x Q(x)$$

$\underbrace{\quad}_{Q(x)}$  where  $Q(x)$  denotes  $\forall y P(x, y)$

Induction on  $x$  means we need to prove:

1.  $Q(0)$  that is,  $\forall y P(0, y)$

2.  $Q(x)$  implies  $Q(x+1)$

If  $\forall y_1 P(x, y_1)$  then  $\forall y_2 P(x+1, y_2)$   $x, y_2$  arbit.

We can instantiate  $\forall y_1 P(x, y_1)$  multiple times when proving that, for any  $y_2$ ,  $P(x, y_2)$  holds

One can instantiate  $y_1$  with  $y_2$  but not only

$\text{exec}(\text{env}, \text{compile}(\text{expr})) ==$   
 $\text{interpret}(\text{env}, \text{expr})$

Attempted proof by induction:

$\text{exec}(\text{env}, \text{compile}(\text{Times}(e1, e2))) ==$   
 $\text{exec}(\text{env}, \text{compile}(e1) :: \text{compile}(e2) :: \text{List}('*'))$

We need to know something about behavior of  
intermediate executions.

$\text{exec} : \text{Env} \times \text{List}[\text{Bytecode}] \rightarrow \text{Int}$

$\text{run} : \text{Env} \times \text{List}[\text{Bytecode}] \times \text{List}[\text{Int}] \rightarrow \text{List}[\text{Int}]$

**// stack as argument and result**

$\text{exec}(\text{env}, \text{bcodes}) == \text{run}(\text{env}, \text{bcodes}, \text{List}()).\text{head}$



# run(env,bcodes,stack) = newStack

Executing sequence of instructions

**run** : Env x List[Bytecode] x List[Int] -> List[Int]

Stack grows to the right, top of the stack is last element

Byte codes are consumed from left

Definition of run is such that

- $\text{run}(\text{env}, \text{'*'} :: L, S ::: \text{List}(x1, x2)) == \text{run}(\text{env}, L, S ::: \text{List}(x1 * x2))$
- $\text{run}(\text{env}, \text{'+'} :: L, S ::: \text{List}(x1, x2)) == \text{run}(\text{env}, L, S ::: \text{List}(x1 + x2))$
- $\text{run}(\text{env}, \text{lLoad}(n) :: L, S) == \text{run}(\text{env}, L, S ::: \text{List}(\text{env}(n)))$

By induction one shows:

- $\text{run}(\text{env}, L1 ::: L2, S) == \text{run}(\text{env}, L2, \text{run}(\text{env}, L1, S))$

execute instructions L1, then execute L2 on the result

# New correctness condition

`exec` : `Env x List[Bytecode] -> Int`

`run` : `Env x List[Bytecode] x List[Int] -> List[Int]`

Old condition:

`exec(env, compile(expr)) == interpret(env, expr)`

New condition:

`run(env, compile(expr), S) == S:::List(interpret(env, expr))`

shorthands:

`env` – `T`, `compile` – `C`, `interpret` – `I`, `List(x)` – `[x]`

**$\forall e \forall S \text{ run}(T, C(e), S) == S:::[I(T, e)]$**



By induction on e,

$$\forall S \quad \text{run}(T, C(e), S) == S ::: [I(T, e)]$$

One case (multiplication):

$$\begin{aligned} & \text{run}(T, C(\text{Times}(e1, e2)), S) == \\ & \text{run}(T, C(e1) ::: C(e2) ::: [\text{`*`}], S) == \\ & \text{run}(T, [\text{`*`}], \text{run}(T, C(e2), \text{run}(T, C(e1), S))) == \\ & \text{run}(T, [\text{`*`}], \text{run}(T, C(e2), S ::: [I(T, e1)])) == \quad (\forall S !) \\ & \text{run}(T, [\text{`*`}], S ::: [I(T, e1)] ::: [I(T, e2)]) == \\ & S ::: [I(T, e1) * I(T, e2)] == \\ & S ::: [I(T, \text{Times}(e1, e2))] \end{aligned}$$



# Shorthand Notation for Translation

$[ e_1 + e_2 ] =$

$[ e_1 ]$

$[ e_2 ]$

**add**

$[ e_1 * e_2 ] =$

$[ e_1 ]$

$[ e_2 ]$

**mul**

# Code Generation for Control Structures

# Sequential Composition

How to compile statement sequence?

`s1; s2; ... ; sN`

- Concatenate byte codes for each statement!

```
def compileStmt(e : Stmt) : List[Bytecode] = e match {  
  ...  
  case Sequence(sts) =>  
    for { st <- sts; bcode <- compileStmt(st) }  
      yield bcode  
}
```

i.e. `sts flatMap compileStmt`

that is: `(sts map compileStmt) flatten`



# Compiling Control: Example

```
int count(int counter,  
          int to,  
          int step) {  
    int sum = 0;  
    do {  
        counter = counter + step;  
        sum = sum + counter;  
    } while (counter < to);  
    return sum; }
```

We need to see how to:

- translate boolean expressions
- generate jumps for control

```
(func $func0  
  (param $var0 i32) (param $var1 i32)  
  (param $var2 i32) (result i32)  
  (local $var3 i32)  
  i32.const 0  
  set_local $var3  
  loop $label0  
    get_local $var3  
    get_local $var0  
    get_local $var2  
    i32.add  
    tee_local $var0  
    i32.add  
    set_local $var3  
    get_local $var0  
    get_local $var1  
    i32.lt_s  
    br_if $label0  
  end $label0  
  get_local $var3 )
```

# Representing Booleans

“All comparison operators yield 32-bit integer results with 1 representing true and 0 representing false.” – WebAssembly spec

Our generated code uses 32 bit int to represent boolean values in: **local variables, parameters, and intermediate stack values.**

**1**, representing true

**0**, representing false

i32.eq: sign-agnostic compare equal

i32.ne: sign-agnostic compare unequal

i32.lt\_s: signed less than

i32.le\_s: signed less than or equal

i32.gt\_s: signed greater than

i32.ge\_s: signed greater than or equal

i32.eqz: compare equal to zero (return 1 if operand is zero, 0 otherwise) // not

# Truth Values for Relations: Example

```
int test(int x, int y){  
    return (x < y);  
}
```

```
(func $func0  
  (param $var0 i32)  
  (param $var1 i32)  
  (result i32)  
  
  get_local $var0  
  get_local $var1  
  i32.lt_s  
)
```



# Comparisons, Conditionals, Scoped Labels

```
int fun(int x, int y){  
    int res = 0;  
    if (x < y) {  
        res = (y / x);  
    } else res = (x / y);  
    return res+x+y;  
}
```

```
(local $var2 i32)  
block $label1 block $label0  
    get_local $var0  
    get_local $var1  
    i32.ge_s  
    br_if $label0 // to else branch  
    get_local $var1  
    get_local $var0  
    i32.div_s  
    set_local $var2  
    br $label1 // done with if  
end $label0 // else branch  
    get_local $var0  
    get_local $var1  
    i32.div_s  
    set_local $var2  
end $label1 // end of if  
    get_local $var1  
    get_local $var0  
    i32.add  
    get_local $var2  
    i32.add
```

# Main Instructions for Labels

- **block**: the beginning of a block construct, a sequence of instructions with a **label at the end**
- **loop**: a block with a label at the **beginning** which may be used to form loops
- **br**: branch to a given label in an enclosing construct
- • **br\_if**: conditionally branch to a given label in an enclosing construct
- **return**: return zero or more values from this function
- **end**: an instruction that marks the end of a block, loop, if, or function

# Compiling If Statement

Notation for compilation:

```
[ if (cond) tStmt else eStmt ] =  
    block $nAfter block $nElse  
    [ !cond ]  
    bf_if $nElse  
    [ tStmt ]  
    br $nAfter
```

```
end $nElse:  
    [ eStmt ]
```

```
end $nAfter:
```

```
block $label1 block $label0  
    (negated condition code)  
    br_if $label0 // to else branch  
    (true case code)  
    br $label1 // done with if  
end $label0 // else branch  
    (false case code)  
end $label1 // end of if
```

Is there alternative without negating condition?



# How to introduce labels

- For forward jumps to \$label: use **block \$label**  
...  
**end \$label**
- For backward jumps to \$label: use **loop \$label**  
...  
**end \$label**