

All Arrays of Given Result Become One Class

Array Assignment Updates Given Array at Given Index

```
class Array {  
  int length;  
  data : int[]  
}  
a[i] = x
```

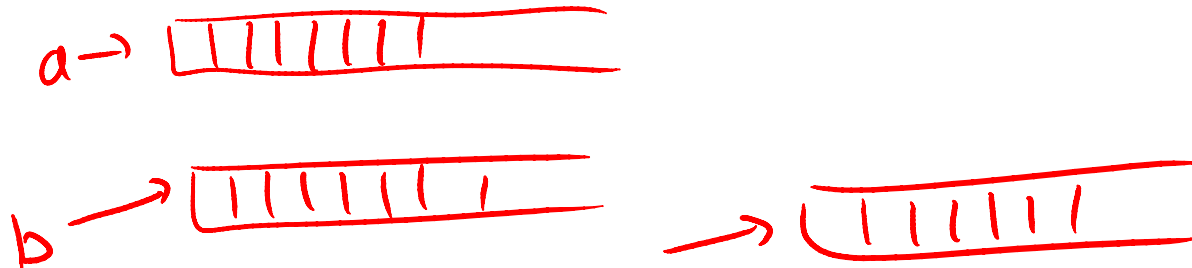
length : Array -> int

data : Array -> (Int -> Int)

or simply: Array x Int -> Int

➔ a.data[i] = x

➔ data = data((a,i):= x)



Assignments to Java arrays:
Now including All Assertions
(safety ensured, or your models back)

```
class Array {  
  int length;  
  data : int[]  
}
```

length : Array -> int

data : Array -> (Int -> Int)

or simply: Array x Int -> Int

a[i] = x

→ assert (a ≠ null);
assert (0 ≤ i ∧ i < length(a));
data = data((a,i) := x)

y = a[i]

→ assert (a ≠ null);
assert (0 ≤ i ∧ i < length(a))
y = data((a,i))

Variables in C and Assembly

Can this assertion fail in C++ (or Pascal)?

```
void funny(int& x, int& y) {  
    x= 4;  
    y= 5;  
    assert(x==4);  
}  
int z;  
funny(z, z);
```

Memory Model in C

Just one global array of locations:

mem : int \rightarrow int // one big array

each variable x has address in memory, xAddr, which is &x

We map operations to operations on this array:

int x;

int y;

int* p;

y = x \rightarrow mem[yAddr] = mem[xAddr]

x = y + z \rightarrow mem[xAddr] = mem[yAddr] + mem[zAddr]

y = *p \rightarrow mem[yAddr] = mem[mem[pAddr]]

p = &x \rightarrow mem[pAddr] = xAddr

*p = x \rightarrow mem[mem[pAddr]] = mem[xAddr]

Variables in C and Assembly

Can this assertion fail in C++ (or Pascal)?

```
void funny(int& x, int& y) {  
    x= 4;  
    y= 5;  
    assert(x==4);  
}  
int z;  
funny(&z, &z);
```

```
void funny(xAddr, yAddr) {  
    mem[xAddr]= 4;  
    mem[yAddr]= 5;  
    assert(mem[xAddr]==4);  
}  
zAddr = someNiceLocation  
funny(zAddr, zAddr);
```

Disadvantage of Global Array

In Java:

$\text{wp}(x=E, y > 0) =$

In C:

$\text{wp}(x=E, y > 0) =$

Disadvantage of Global Array

In Java:

$$\text{wp}(x=E, y > 0) = y > 0$$

In C:

$$\begin{aligned} \text{wp}(x=E, y > 0) &= \\ \text{wp}(\text{mem}[x\text{Addr}]=E', \text{mem}[y\text{Addr}]>0) &= \\ \text{wp}(\text{mem}=\text{mem}(x\text{Addr}:=E'), \text{mem}(y\text{Addr})>0) &= \\ (\text{mem}(y\text{Addr})>0)[\text{mem}:=\text{mem}(x\text{Addr}:=E')] &= \\ (\text{mem}(x\text{Addr}:=E'))(y\text{Addr}) > 0 & \end{aligned}$$

Each assignment can interfere with each value!

This is a problem with the language, not our model

More About Allocation

New Objects Point Nowhere

```
class C { int f; C next; C prev; }
```

this should work:

```
x = new C();
```

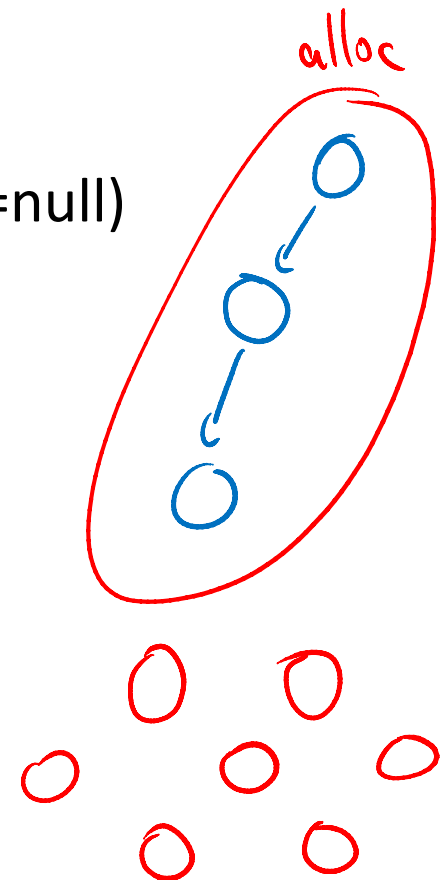
```
assert(x.f==0 && c.next==null && c.prev==null)
```

```
x = new C(); →
```

1) use assignment
f = f(x := 0)

2) use assume

```
havoc(x)  
assume(x != alloc)  
alloc = alloc ∪ {x}  
assume(f(x) == 0 ∧  
next(x) = null ∧  
prev(x) = null);
```



If you are new, you are known by few

```
class C { int f; C next; C prev; }
```

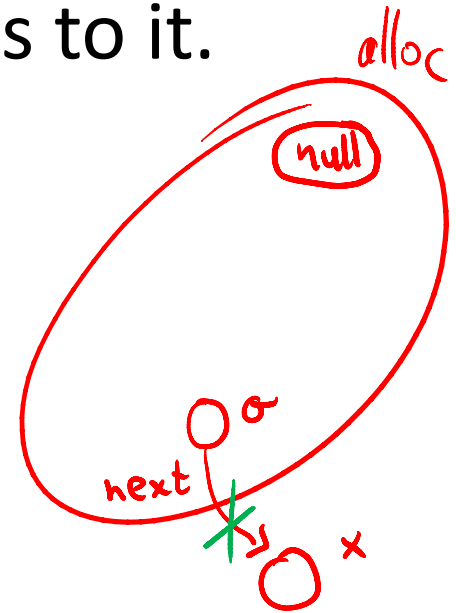
Assume C is the only class in the program

Lonely object: no other object points to it.

Newly allocated objects are lonely!

$x = \text{new } C();$ \rightarrow

$\forall \sigma, \theta \in \text{alloc} \rightarrow \text{next}(\sigma) \neq x$



$\forall \sigma. \sigma \in \text{alloc} \rightarrow \text{next}(\sigma) \in \text{alloc} \wedge \text{prev}(\sigma) \in \text{alloc}$

Remember our Model of Java Arrays

```
class Array {  
  int length;  
  data : int[]  
}
```

$a[i] = x$

$y = a[i]$

length : Array \rightarrow int

data : Array \rightarrow (Int \rightarrow Int)

or simply: Array x Int \rightarrow Int

\rightarrow assert $(a \neq \text{null})$;
assert $(0 \leq i \wedge i < \text{length}(a))$;
data = data((a,i) := x)

\rightarrow assert $(a \neq \text{null})$;
assert $(0 \leq i \wedge i < \text{length}(a))$
 $y = \text{data}(a, i)$

Allocating New Array of Objects

```
class oArray {  
  int length;  
  data : Object[]  
}
```

```
x = new oArray[100] →
```

$length = length(x := E)$

$havoc(x);$
 $assume(x \notin alloc);$
 $alloc = alloc \cup \{x\};$
 $assume(length(x) = E_{(100)}) \wedge$

$\forall i. 0 \leq i < E \rightarrow$
 $data(x, i) = null \wedge$

$\forall \sigma \in alloc. \wedge f(\sigma) \neq x$
 $f \in fields(coll)$

Procedure Contracts

Suppose there are fields and variables f_1, f_2, f_3 (denoted f)

procedure $\text{foo}(x)$:

requires $P(x, f)$

modifies f_3

ensures $Q(x, \text{old}(f), f)$

$\text{foo}(E) \rightarrow$

$\text{assert}(P(E, f));$

$\text{old}_f = f;$

$\text{havoc}(f_3);$

$\text{assume } Q(E, \text{old}_f, f)$

Modification of Objects

Suppose there are fields and variables f_1, f_2, f_3 (denoted f)

```
procedure foo(x):  
  requires P(x,f)  
  modifies x.f3  
  ensures Q(x,f,f')
```

$$x.f_3 = y \quad \rightsquigarrow \quad f_3 = f_3(x := y)$$

foo(E) →

```
assert(P(E,f));
```

```
old_f = f; ←  $\begin{cases} \text{old}_f.f_1 = f_1 \\ \text{old}_f.f_3 = f_3 \end{cases}$ 
```

```
havoc(x.f3);
```

```
→ havoc(f3); assume  $\forall z \neq x. f_3(z) = \text{old}_f.f_3(z)$ 
```

```
assume Q(E,old_f, f)
```

Example

```
class Pair { Object first; Object second; }  
void printPair(p : Pair) { ... }  
void printBoth(x : Object, y : Object)  
modifies first, second // ?  
{  
  Pair p = new Pair();  
  p.first = x;  
  p.second = y;  
  printPair(p);  
}
```

printBoth(x1,y1)

Allowing Modification of Fresh Objects

Suppose there are fields and variables f_1, f_2, f_3 (denoted f)

procedure $\text{foo}(x)$:

requires $P(x, f)$

modifies $x.f_3$

ensures $Q(x, f, f')$

$\text{foo}(E) \rightarrow$

assert($P(E, f)$);

old_f = f; $\text{old_alloc} = \text{alloc};$

havoc $f_3, f_2, f_1, \text{alloc}$

assume $\forall z \in \text{old_alloc} . f_1(z) = \text{old_}f_1(z) \wedge f_2(z) = \text{old_}f_2(z)$

assume $Q(E, \text{old_}f, f)$ $(z \neq x \rightarrow f_3(z) = \text{old_}f_3(z))$

assume ($\text{old_alloc} \subseteq \text{alloc}$)

Data remains same if: 1) existed and 2) not listed in m.clause