

$$[[S]]_{in} = S_{use} \cup ([[S]]_{out} \setminus S_{df})$$