

$$r_* = \bigcup_{k \geq 0} m^k(\emptyset)$$