

$$r = (\bigcup_{i=1}^N d_{r1}^i, \bigcup_{i=1}^N d_{r2}^i, \dots, \bigcup_{i=1}^N d_{r31}^i)$$