

$$\forall x_1, \dots, x_n, y_1, \dots, y_n. \bigwedge_{i=1}^n (x_i, y_i) \in \bigcap S$$