$r \subseteq S \times S$