$$r_{n+1} \subseteq r_*$$