

$$[[S]]_{out} = \bigcup_{X \in succ(S)} [[X]]_{in}$$