

$$(x, y) \in \bigcap S \wedge (y, z) \in \bigcap S \rightarrow (x, y) \in r_1, r_2 \wedge (y, z) \in r_1, r_2$$