

$$Q_S = \{q \in Q \mid \exists s \in S. q_0sq\}$$