

$$S = \bigcup_{i \in I} \{i + 0k \mid k \in \mathbb{N}\} \cup \bigcup_{j \in J} \{j + vk \mid k \in \mathbb{N}\}.$$