

$$\bigcup_i S_i(a, b) = S$$