**Proof:** By induction, for each

