

$$\forall v. \text{fact}_{i+1}(v) \rightarrow \text{fact}_i(v)$$