

$$r_{\text{ex}} = \{(x, y) | x \leq y\} \cup \{(a, b)\}$$