

$$\lambda_x \cap S_3 \neq \emptyset \Rightarrow S_1 \subseteq S_2$$