

$$\mathit{bigscup}_{n \geq 0} G^n(\perp) = \mathit{bigscup}_{n \geq 1} G^n(\perp) \sqcup \perp = \mathit{bigscup}_{n \geq 1} G^n(\perp)$$