

$$C^{i+1}(s) \cap T^2 = C(C^i(s) \cap T^2) \cap T^2$$