$g_{init}:V\to 2^S$