

$$\exists p_1, \dots, p_M \cdot \bigwedge_{F \in S} F$$