

$$PS = S \times \{\text{true}, \text{false}\}$$