

$$S_{y,f} \cup S_{x,f} \subseteq S_{x_1}$$