

$$(d_{r1}, d_{r2}, \dots, d_{r31}), d_* \in 2^S$$