

$$m(r_*) = m(\bigcup_{i \geq 0} r_n) = \bigcup_{i \geq 0} m(r_n) = \bigcup_{i \geq 0} r_{n+1} = r_*$$