

## Exercise 1

Convert the following grammar to Chomsky normal form:

$$E \rightarrow E + E \mid E * E \mid ( E ) \mid id$$

## Exercise 2

Convert the following grammar to Chomsky normal form:

$$S \rightarrow a S b \mid \varepsilon$$

Then, apply the CYK algorithm on the following inputs:

a a b b

a b b

## Exercise 3

Convert the following grammar to Chomsky normal form:

$$S \rightarrow P ;$$

$$P \rightarrow I \mid I ; P$$

$$I \rightarrow \text{if } E \text{ then } P R \mid \text{print } E$$

$$R \rightarrow \text{else } P \mid \varepsilon$$

$$W \rightarrow \text{while } E \text{ do } P$$

$$E \rightarrow L \mid E \text{ or } E \mid C$$

$$C \rightarrow C \text{ and } E \mid E \text{ and } C$$

$$L \rightarrow \text{true} \mid \text{false}$$

Then, apply the CYK algorithm on the following inputs:

if true print true ;

print true or false or true ;

if true then print true ; print false ;

In each case, how many different parse trees do you obtain ?

How many parse trees are there for the following inputs ?  
You do not need to execute CYK to answer this question.

`if true or false or true then print true or false or true ;`

`if true then if false then print true else print false ;`

`if true then print true ; print false ; print true ;`