

# Data-flow analysis exercises

Draw the control-flow graph for the following program,  
then perform range analysis.

All integer range [-128...127]

prog1:

```
var a = input()
```

```
var b = 50-a
```

```
var c = -1
```

```
if(a > b && a > c) {
```

```
    c = a
```

```
} else if(b > c) {
```

```
    c = b
```

```
}
```

```
var c = 100/c
```

prog2:

```
var a = input()
```

```
var c = 1
```

```
val r = 1
```

```
while(c < a) {
```

```
    if( a % c == 0 ) r = c
```

```
    c = c + 1
```

```
}
```

```
r = 64/(64-r)
```

prog3:

```
var x = 2
```

```
var y = input()
```

```
if (x == y) {
```

```
    do {
```

```
        y = y + 1
```

```
        x = x + y + 3
```

```
    } while (y < 4)
```

```
} else if (y <= -1 && y >= -7) {
```

```
    y = y * y
```

```
} else {
```

```
    y = x - 3
```

```
}
```

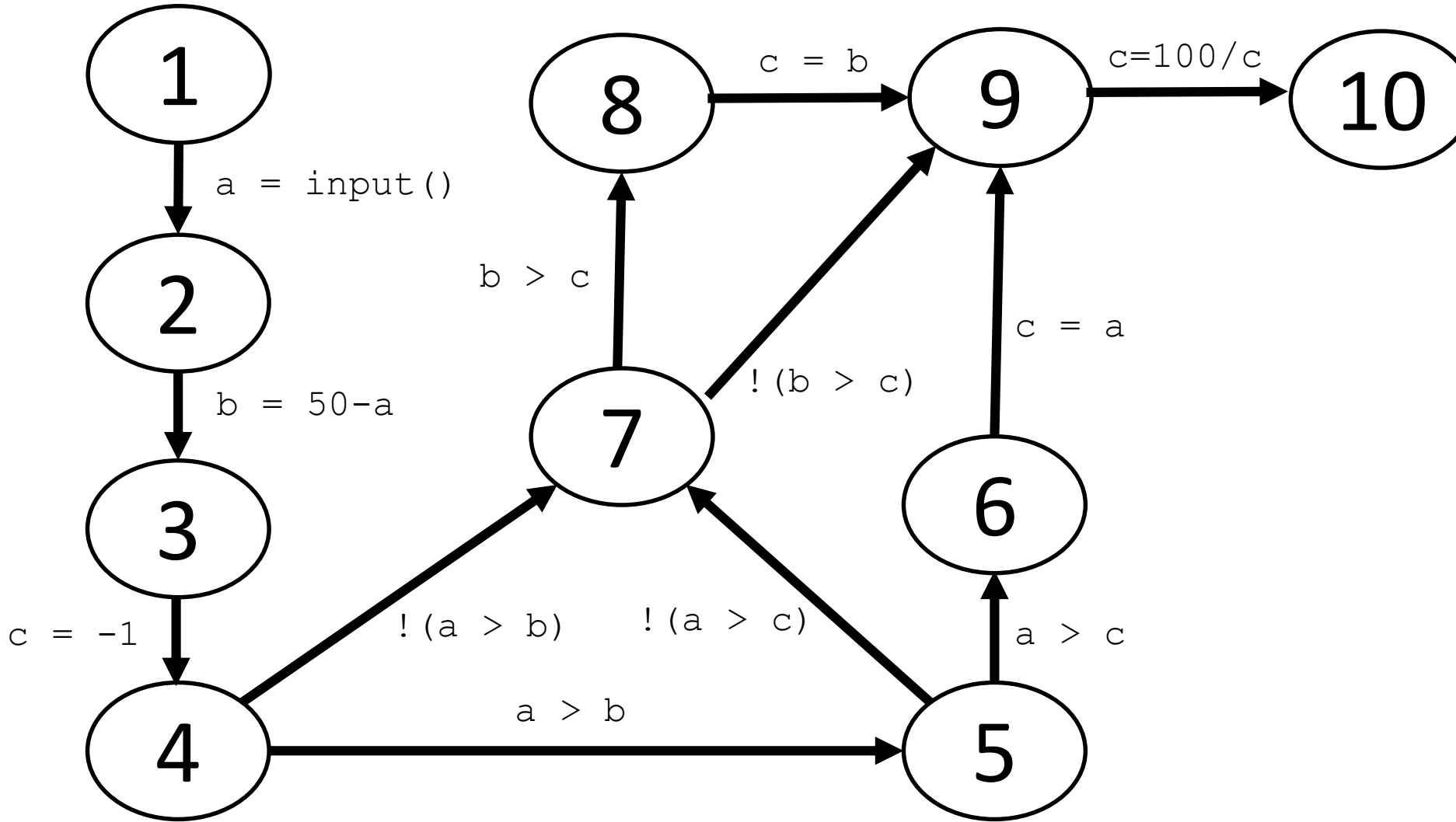
```
val z = x/y
```

1. Draw the control-flow graph for the following program, then perform range analysis.

All integer range [-128...127]

```
var a = input()
var b = 50-a
var c = -1
if(a > b && a > c) {
    c = a
} else if(b > c) {
    c = b
}
var c = 100/c
```

# 1. Solution



# 1. Range analysis

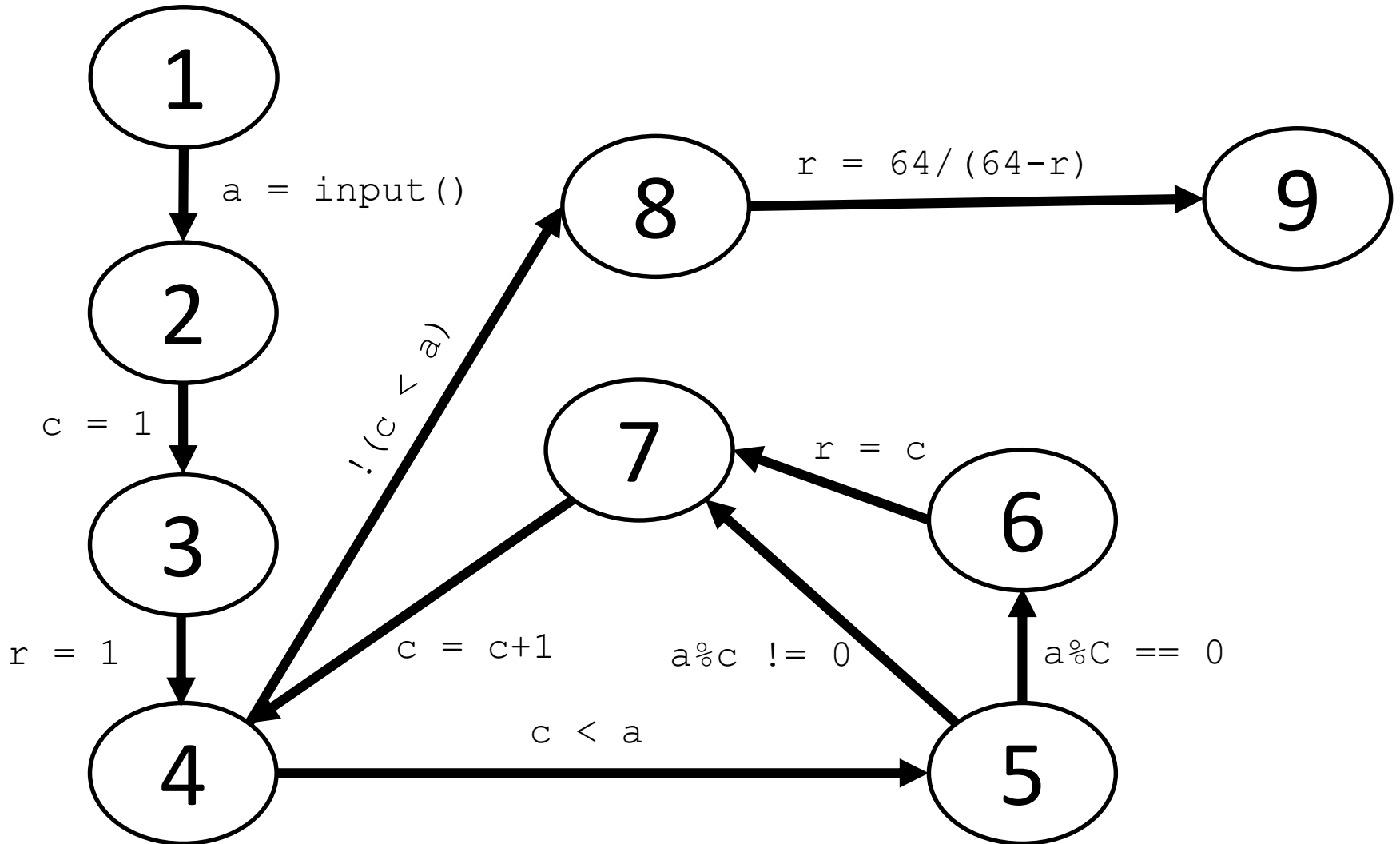
|     | a             | b           | c                            |
|-----|---------------|-------------|------------------------------|
| 1:  | bottom        | bottom      | bottom                       |
| 2:  | $[-128, 127]$ | bottom      | bottom                       |
| 3:  | $[-128, 127]$ | $[-77;127]$ | bottom                       |
| 4:  | $[-128, 127]$ | $[-77;127]$ | $[-1]$                       |
| 5:  | $[-76, 127]$  | $[-77;126]$ | $[-1]$                       |
| 6:  | $[0, 127]$    | $[-77;126]$ | $[-1]$                       |
| 7:  | $[-128, 127]$ | $[-77;127]$ | $[-1]$                       |
| 8:  | $[-128, 127]$ | $[0;127]$   | $[-1]$                       |
| 9:  | $[0, 127]$    | $[-77;127]$ | $[0, 127]$                   |
| 10: | $[0, 127]$    | $[-77;127]$ | <b><math>[0, 100]</math></b> |

2. Draw the control-flow graph for the following program, then perform range analysis.

All integer range [-128,127]

```
var a = input()
var c = 1
val r = 1
while(c < a) {
    if( a % c == 0 ) r = c
    c = c + 1
}
r = 64 / (64 - r)
```

## 2. Solution





## 2. Range analysis

|    | a             | c      | r      |
|----|---------------|--------|--------|
| 1: | bottom        | bottom | bottom |
| 2: | $[-128, 127]$ | bottom | bottom |
| 3: | $[-128, 127]$ | $[1]$  | bottom |
| 4: | $[-128, 127]$ | $[1]$  | $[1]$  |
| 5: | $[2, 127]$    | $[1]$  | $[1]$  |
| 6: | $[2, 127]$    | $[1]$  | $[1]$  |
| 7: | $[2, 127]$    | $[1]$  | $[1]$  |
| 8: | $[-128, 1]$   | $[1]$  | $[1]$  |
| 9: | $[-128, 1]$   | $[1]$  | $[1]$  |

## 2. Range analysis

|    | a                    | c                 | r                 |
|----|----------------------|-------------------|-------------------|
| 1: | bottom               | bottom            | bottom            |
| 2: | $[-128, 127]$        | bottom            | bottom            |
| 3: | $[-128, 127]$        | $[1]$             | bottom            |
| 4: | $[-128, 127]$        | $[1, \mathbf{2}]$ | $[1]$             |
| 5: | $[2, 127]$           | $[1, \mathbf{2}]$ | $[1]$             |
| 6: | $[2, 127]$           | $[1, \mathbf{2}]$ | $[1]$             |
| 7: | $[2, 127]$           | $[1, \mathbf{2}]$ | $[1, \mathbf{2}]$ |
| 8: | $[-128, \mathbf{2}]$ | $[1, \mathbf{2}]$ | $[1, \mathbf{2}]$ |
| 9: | $[-128, \mathbf{2}]$ | $[1, \mathbf{2}]$ | $[1]$             |

## 2. Range analysis

|    | a                    | c                 | r                 |
|----|----------------------|-------------------|-------------------|
| 1: | bottom               | bottom            | bottom            |
| 2: | $[-128, 127]$        | bottom            | bottom            |
| 3: | $[-128, 127]$        | $[1]$             | bottom            |
| 4: | $[-128, 127]$        | $[1, \mathbf{3}]$ | $[1, \mathbf{2}]$ |
| 5: | $[2, 127]$           | $[1, \mathbf{3}]$ | $[1, \mathbf{2}]$ |
| 6: | $[2, 127]$           | $[1, \mathbf{3}]$ | $[1, \mathbf{2}]$ |
| 7: | $[2, 127]$           | $[1, \mathbf{3}]$ | $[1, \mathbf{3}]$ |
| 8: | $[-128, \mathbf{3}]$ | $[1, \mathbf{3}]$ | $[1, \mathbf{3}]$ |
| 9: | $[-128, \mathbf{3}]$ | $[1, \mathbf{3}]$ | $[1]$             |

## 2. Range analysis

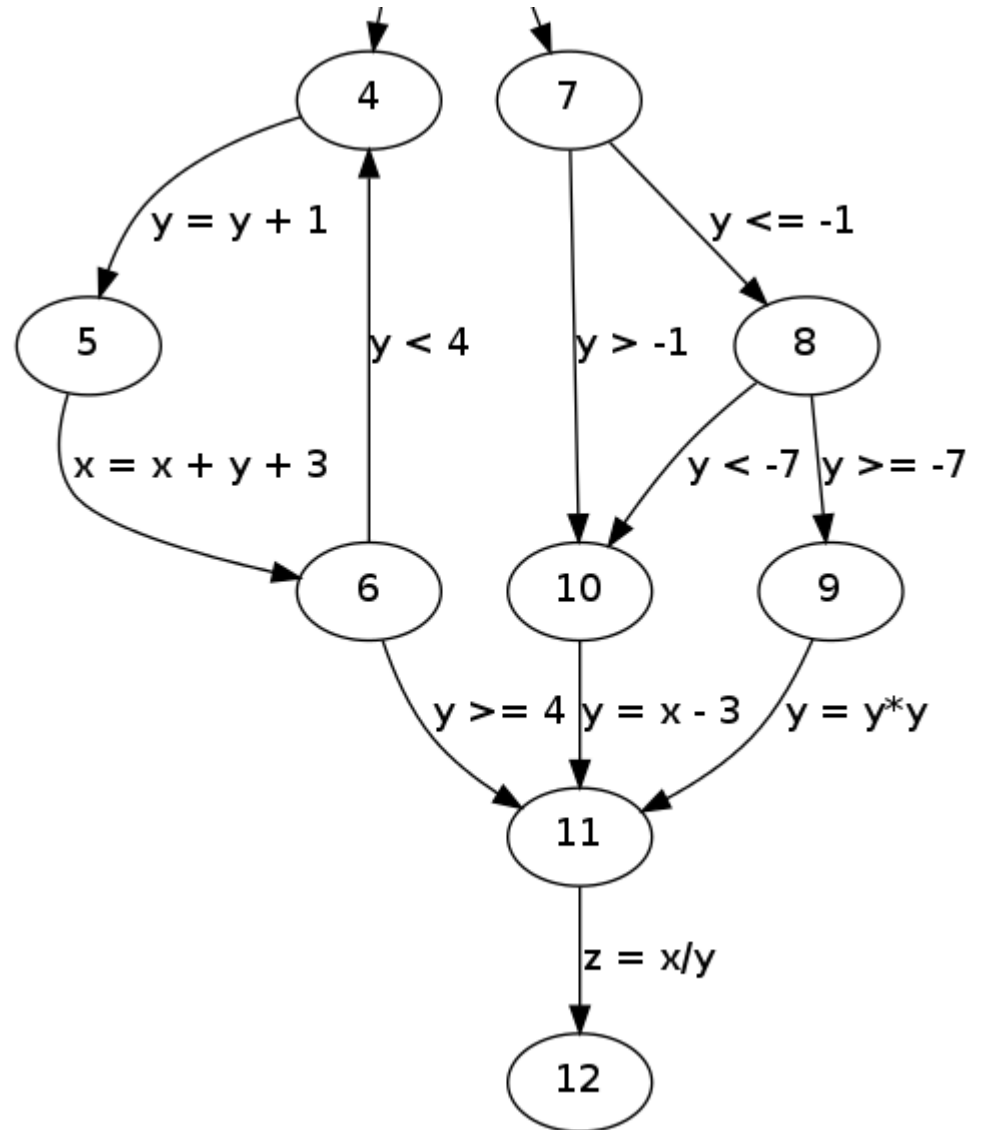
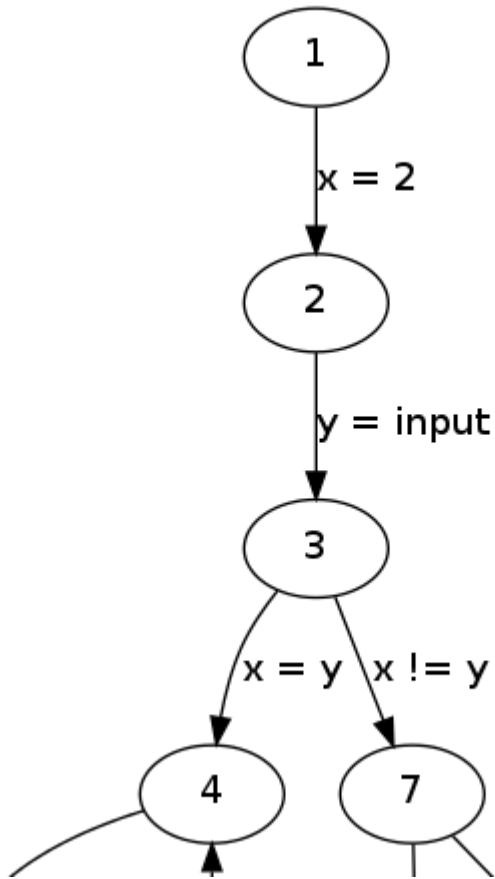
|    | a                      | c                   | r                           |
|----|------------------------|---------------------|-----------------------------|
| 1: | bottom                 | bottom              | bottom                      |
| 2: | $[-128, 127]$          | bottom              | bottom                      |
| 3: | $[-128, 127]$          | $[1]$               | bottom                      |
| 4: | $[-128, 127]$          | $[1, \mathbf{127}]$ | $[1, \mathbf{126}]$         |
| 5: | $[2, 127]$             | $[1, \mathbf{126}]$ | $[1, \mathbf{126}]$         |
| 6: | $[2, 127]$             | $[1, \mathbf{63}]$  | $[1, \mathbf{63}]$          |
| 7: | $[2, 127]$             | $[1, \mathbf{126}]$ | $[1, \mathbf{126}]$         |
| 8: | $[-128, \mathbf{127}]$ | $[1, \mathbf{126}]$ | $[1, \mathbf{126}]$         |
| 9: | $[-128, \mathbf{127}]$ | $[1, \mathbf{127}]$ | $[\mathbf{0}, \mathbf{64}]$ |

### 3. Draw the control-flow graph for the following program, then perform range analysis.

All integer range [-128,127]

```
var x = 2
var y = input()
if (x == y) {
  do {
    y = y + 1
    x = x + y + 3
  } while (y < 4)
} else if (y <= -1 && y >= -7) {
  y = y * y
} else {
  y = x - 3
}
val z = x/y
```

# 3. Solution



# 3. Range analysis

| x   |          | y           |      |
|-----|----------|-------------|------|
| 1:  | bottom   | bottom      |      |
| 2:  | [2, 2]   | [-128, 127] |      |
| 3:  | [2, 2]   | [-128, 127] |      |
| 4:  | [2, 127] | [2, 3]      |      |
| 5:  | [2, 127] | [3, 4]      |      |
| 6:  | [8, 127] | [3, 4]      |      |
| 7:  | [2, 2]   | [-128, 127] |      |
| 8:  | [2, 2]   | [-128, -1]  |      |
| 9:  | [2, 2]   | [-7, -1]    |      |
| 10: | [2, 2]   | [-128, 127] |      |
| 11: | [2, 127] | [-1, 49]    |      |
| 12: | [2, 127] | [-1, 49]    | z: T |